



**HERSCHEL / PLANCK**

**Planck PLM RF Performance Analysis**

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## 1. INTRODUCTION

## 2. INTRODUCTION

### 2.1 Purpose of this note

This note updates the CDR analysis.

### 2.2 Applicable documents.

[AD 1] System requirements specification – SCI – PR-RS-05991- issue 3/ 0- 27 july 2004

[AD 2] H-P-3-ASPI-SP-0274 -issue 1 - rev 0 -Planck Telescope optical and RF system specification.

### 2.3 Reference documents

[RD 1] Planck RF expertise Phase B - WP4 - RF calculation report : Incident RF power exchange between detector and structural elements - October, 2002 - S-1117-07

[RD 2] H-P-1-ASP-RP 1248 01/02/2007 ISSUE 1.

[RD 3] NIL

[RD 4] Planck RF expertise model verification & computations WP 2 & WP3 - November , 2003 -TICRA - s-1188-03

[RD 5] Update of the inputs for the RF numerical model - H-P-3-ASP-TN-0564 - issue 1 - rev 0 - 16/09/2003

[ RD 6 ] H-P-3-ASPI-TN-0517 -issue 1 - rev 0 - Planck LFI detector data processing.

[ RD 7 ] H-P-3-ASPI-TN-0559 -issue 1 - rev 2 - HFI detector data processing.

[RD 8] Planck RF expertise - Manual for computations of far out side lobe patterns - November, 2003 - s1188-04

[RD 9] Reflector quilting analysis – H-P-3-ASP-TN-1015 – issue 1 – 10/01/2007.

[RD 10] Planck RFQM evaluation report H-P-3-ASP-TR-1144 - issue 1 - 10/02/2007

[RD 11] NIL.

[RD 12] NIL

[RD 13] NIL

[RD 14] Analysis of the diffusion by primary reflector using the MAP method - H-P-3-ASP-TN-0528 - issue 1 - rev 0 - 11/06/2003.

[RD 15] Dust contamination analysis - H-P-3-TN-0468 - issue 1 - rev 0 - 27 /05 /2003

[RD 16] H-P-3-ASP-TN-0821 Revisited dust analysis answer to CDR RID POEI-03 – issue 1 – 22/07/2004



[RD 17] NIL

[RD 18] NIL

[RD 19] NIL

[RD 20] Planck Optical Analysis, Inputs for WFE and Gain Budgets, H-P-3-ASPI-AN-0742 issue 1 Rev 0 20/04/2004

[RD 21] Planck Reflector Global Shape data SCI-PT/041726 issue 1 07/04/2006

[RD 22] Planck Reflector Interface Position data SCI-PT/042052 issue 2 02/05/2006]

[RD 23] Planck Payload Optical Performance Analysis, H-P-3-ASPI-TN-0331, issue 2 Apr. 2004.

[RD 24] Planck alignment plan H-P-3-ASPI-PL-0078 issue 3 rev 0 04/2004

[RD 25] Planck Telescope alignment in operational environment-computation results H-P-3-ASP-TN-1117  
11/05/2006

[RD 26] Planck Telescope FM alignment determination logic ASP-04-OS /1/1/99

[RD 27] Planck Payload FM Optical WFE Budget H-P-3-ASP-BD-1151 11/2006



### 3. SELF SPACECRAFT EMISSION ANALYSIS.

#### 3.1 Scope

This section presents the analysis of the self spacecraft emission level.

The analysis starts with the understanding of the requirement. Then the sensitivity analysis method is explained and applied. This sensitivity analysis allows to identify the most critical surface element wrt to the performance.

The last phase is the performance budget based upon the results of the thermal analysis.

The main update wrt the CDR analysis are the following :

- Fourier transform of the updated temporal thermal





### 3.2 Self spacecraft emission requirement

The self spacecraft emission requirement is defined in the System Requirement Specification (requirement ref SPER 065 P).

\*\*\*\*\*

The ASD ( in Watts /  $\sqrt{\text{Hz}}$  ) of each frequency component between 0.01 Hz and 100 Hz shall be such that :

Frequency [ GHz ]	ASD [ Watt / $\sqrt{\text{Hz}}$ ]
30	< 3.4 E-18 X
100 ( LFI )	< 1.1 E-17 X
100 ( HFI )	< 2.1 E-18 X
353	< 1.8 E-18 X
857	< 2.2 E-17 X

**Note :**

X is equal to one for any frequency component  $f_0$  of the fluctuation source synchronous with the Planck S/C spinning rate ( i.e. multiple of  $f_{\text{spin}} = 1 / 60$  Hz ).

Otherwise ,  $X = ( B * t_{\text{obs}} * \Delta f )$  , where  $\Delta f = f_0 - k * f_{\text{spin}}$  and k is chosen to minimise  $\Delta f$  .  
 $t_{\text{obs}} = 3600 * \text{FWHM} / 2.5 \text{ arcmin}$  , and FWHM is the angular resolution of the antenna radiation pattern in arc minutes .

\*\*\*\*\*

The above requirement is derived in order to obtain for any component  $f_0$  of the fluctuating source, the maximum allowed level of ASD.

$\Delta f$  is the difference between the fluctuating component  $f_0$  and the nearest multiple of the spin frequency. Then  $(\Delta f)_{\text{max}}$  is equal to  $f_{\text{spin}}/2$ .

If  $f_0 = k * f_{\text{spin}}$  then  $X = 1$ .

If  $f_0$  different from  $f_{\text{spin}}$  X is a linear function varying with  $f_0$ . X is a periodic function. The period is  $f_{\text{spin}}$ .

For  $f_0$  varying from  $k * f_{\text{spin}}$  to  $k * (f_{\text{spin}} + f_{\text{spin}}/2)$ , X is linearly increasing from 1 up to  $\text{PI} * t_{\text{obs}} * f_{\text{spin}}/2$ .

For  $f_0$  varying from  $k * (f_{\text{spin}} + f_{\text{spin}}/2)$  to  $(k + 1) * f_{\text{spin}}$ , X is linearly decreasing from  $\text{PI} * t_{\text{obs}} * f_{\text{spin}}/2$  down to 1.

The following table details for each frequency the ASD allowed deviation. The Second column is obtained from the computation of the telescope main lobe. The fourth column is the requirement to be multiplied by X function of  $f_0$ .



In this table (Table 3.2-1) the most stringent requirement is only applicable to spin-synchronous fluctuating sources. The most relaxed requirement is applicable to sources fluctuating at  $f = k \cdot 3/2 \cdot f_{spin}$ .

Central frequency (GHz)	FWHM (arcmin)	PI*t_obs(s)	Quantity (to multiplied by X)	X_max	ASD_min (W/Hz <sup>-0.5</sup> ) = ASD * 1	ASD_min (dBW/Hz <sup>-0.5</sup> )	ASD_max (W/Hz <sup>-0.5</sup> )	ASD_max (dBW/Hz <sup>-0.5</sup> )
30	33	149288.48	3.40E-18	1244.07	3.40E-18	-174.69	4.23E-15	-143.74
100 (LFI)	10	45238.93	1.10E-17	376.99	1.10E-17	-169.59	4.15E-15	-143.82
100 (HFI)	10	45238.93	2.10E-18	376.99	2.10E-18	-176.78	7.92E-16	-151.01
353	5.0	22619.47	1.80E-18	188.50	1.80E-18	-177.45	3.39E-16	-154.69
857	5.0	22619.47	2.20E-17	188.50	2.20E-17	-166.58	4.15E-15	-143.82

Table 3.2-1 : Minimum and Maximum amplitude deviations of the ASD.

The Figure 3.2-1 presents all the five curves on the same plot. The maxima of the LFI 30 LFI 100 and HFI 857 are almost the same. The three corresponding curves appear merged. The most stringent requirement is the one for the HFI 353 GHz channel.

The Figure 3.2-2 and Figure 3.2-6 present the requirements curves one by one for each specified frequency.

The curves are plotted for the first few multiples of the spin frequency. Due to the wide dynamic variation, the ordinate is plotted as  $10 \cdot \log_{10}(ASD)$ . Hence the linear behaviour of the requirement is plotted as a logarithmic curve instead of a linear curve.

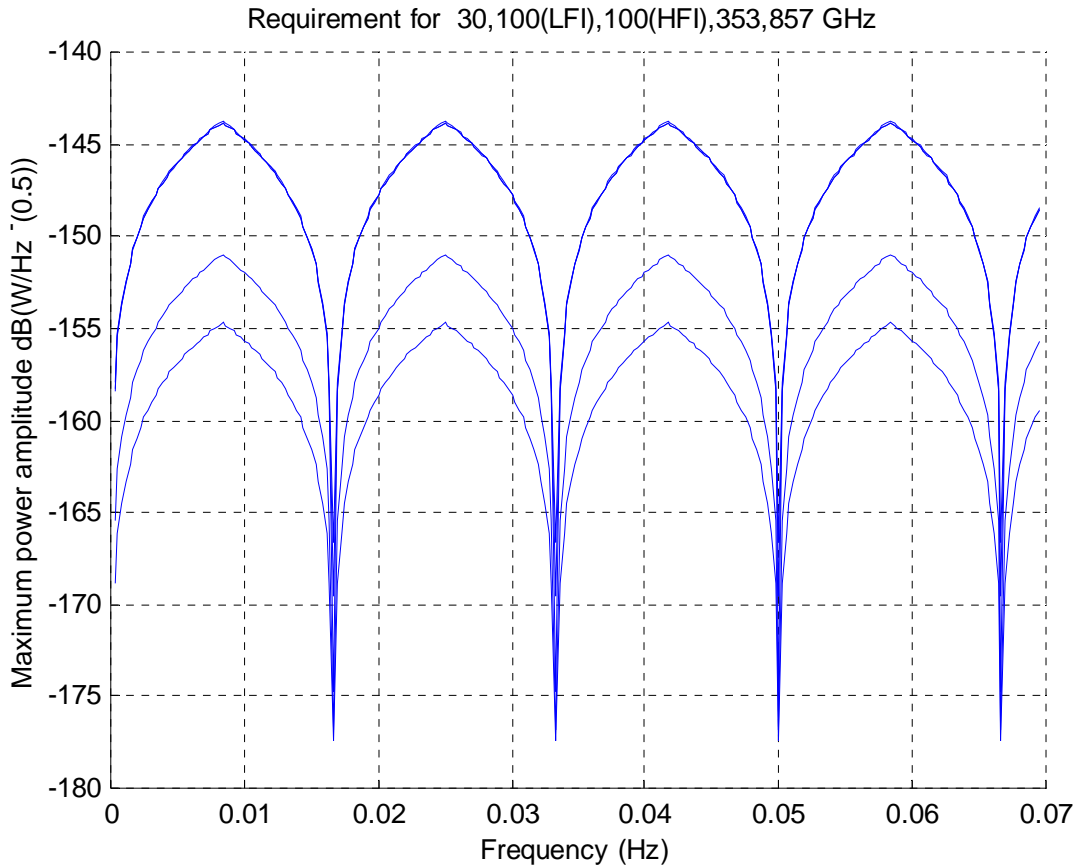


Figure 3.2-1 : All 5 curves from top : LFI 30,HFI 100,HFI 857 (merged), HFI 100 then HFI 353

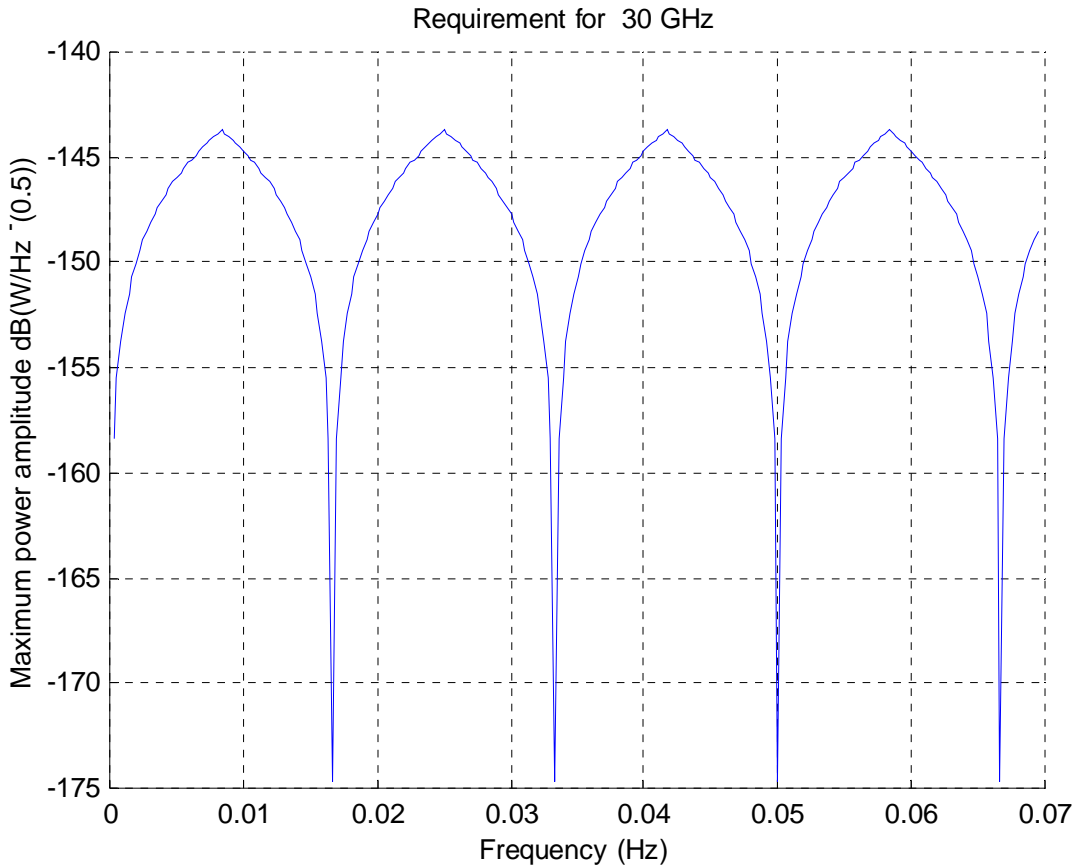


Figure 3.2-2 : 30 GHz requirement curve.

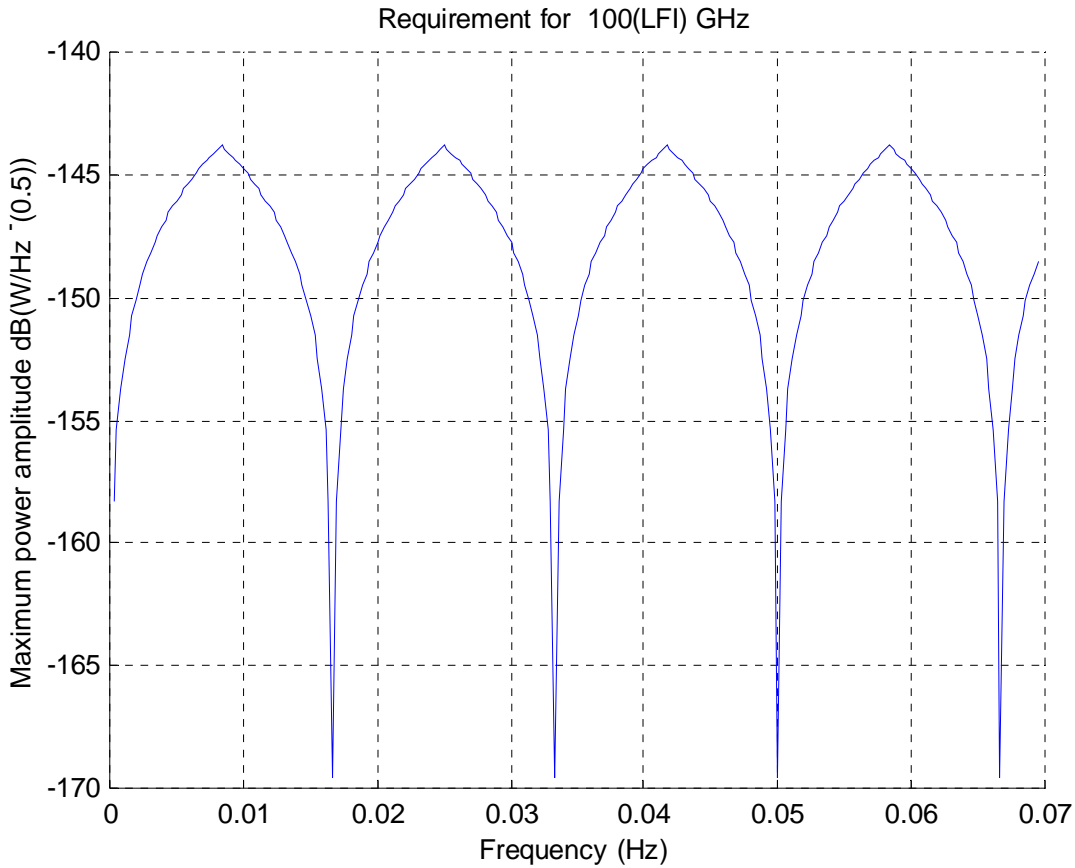


Figure 3.2-3 :100 GHz LFI requirement curve.

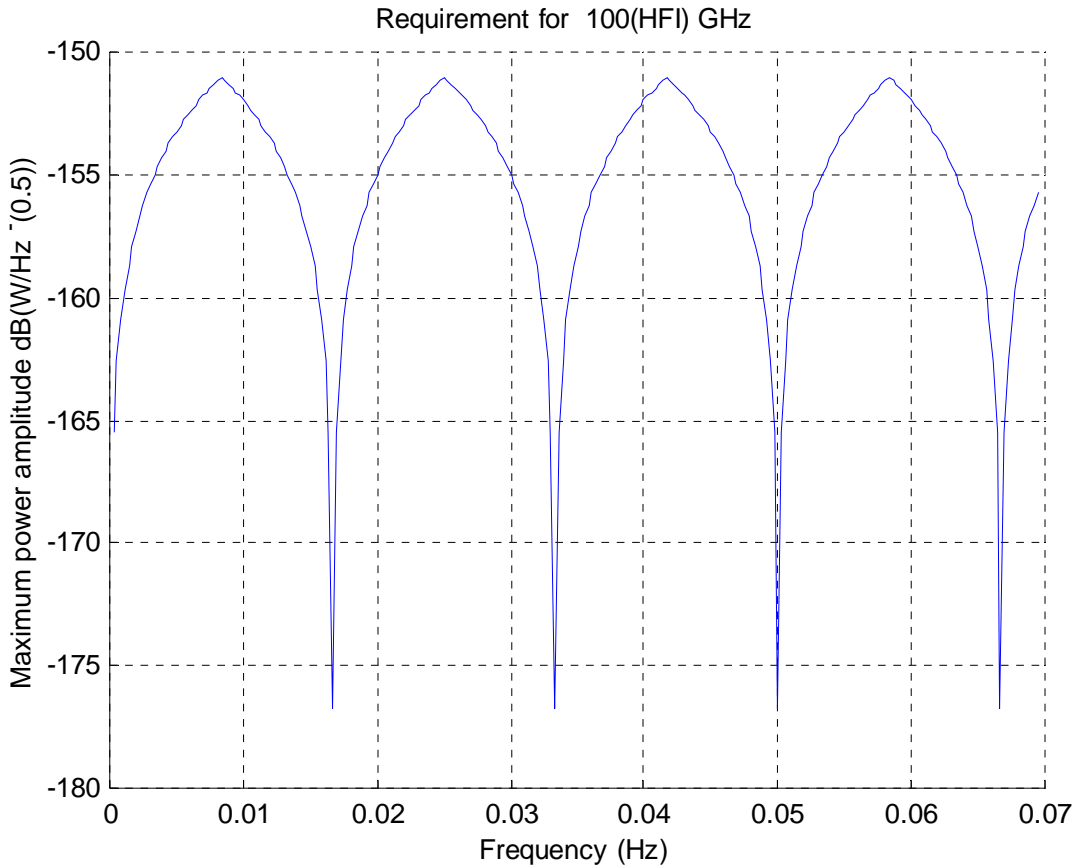


Figure 3.2-4 : 100 GHz HFI requirement curve.

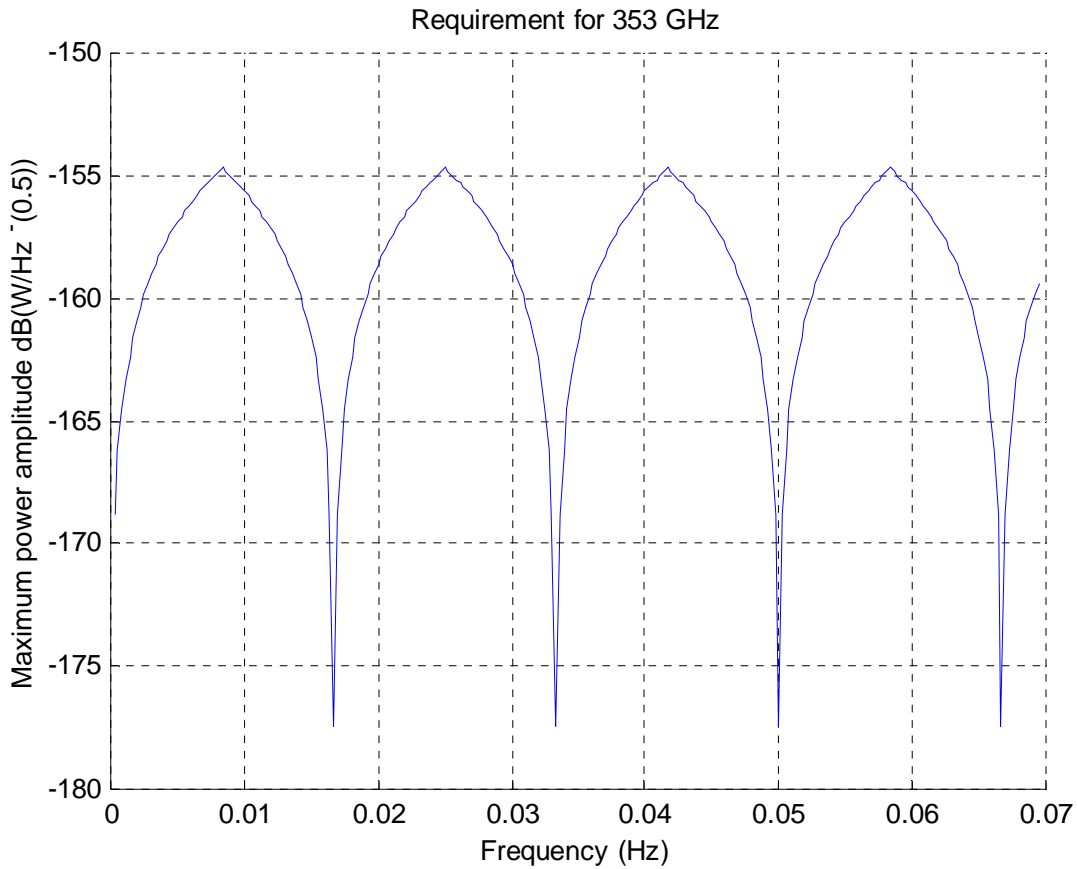


Figure 3.2-5 : 353 GHz HFI requirement curve.

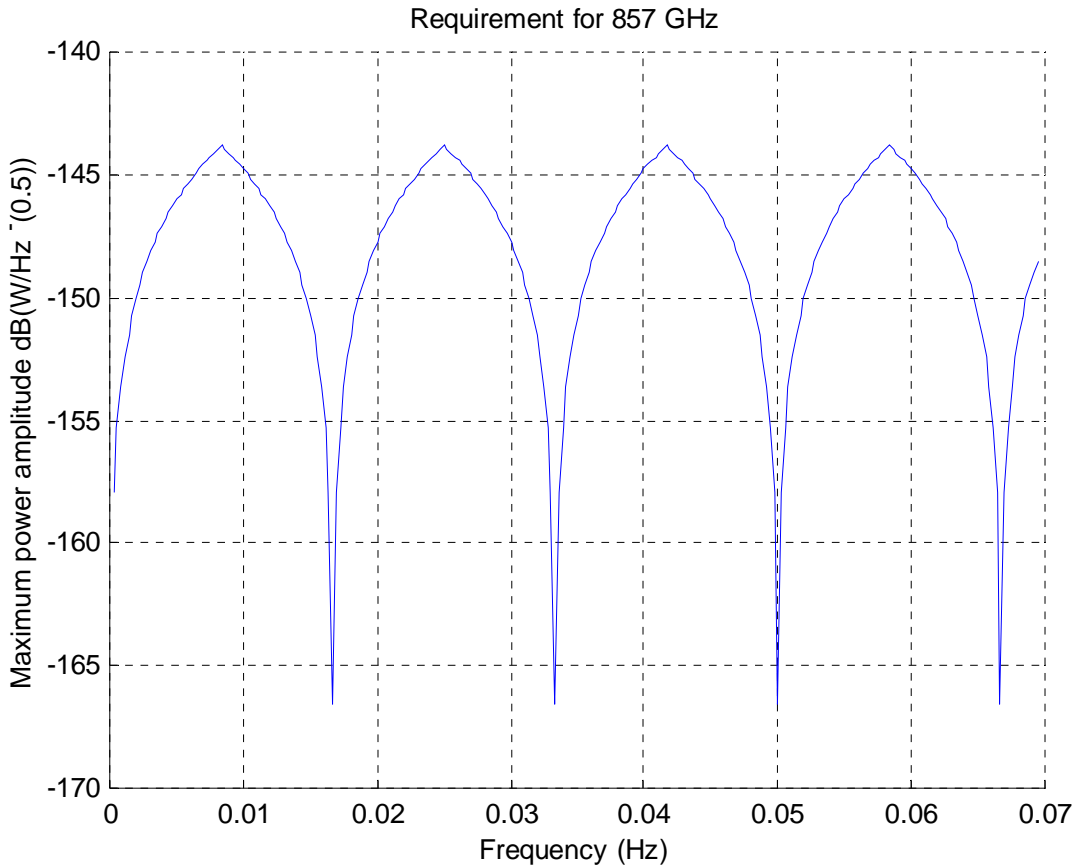


Figure 3.2-6 : 857 GHz HFI requirement curve.





### 3.3 Conversion of the temperature fluctuation law into power fluctuation law.

The SPER 065 P requirement is expressed in terms of power fluctuation. The input for the analysis is provided as temperature deviation. Hence it is necessary to convert the temperature fluctuation law into a power fluctuation law. The conversion is detailed here below.

The received power by a detector is :

$$P = \frac{A_r}{2} \int_{f_1}^{f_2} \iint_{4p} B(q, j, f, T) f_n(q, j) d\Omega df \quad [1]$$

$$B(q, j, f, T) = \frac{\left(\frac{2 \cdot h}{c^2}\right) \cdot f^3}{\exp\left(\frac{h \cdot f}{k \cdot T}\right) - 1} \quad [2] \text{ is the spectral brightness of a black body (Planck's law)}$$

T : black body temperature

$f_n$  : normalised power radiation pattern of the detector

$f_1, f_2$  : bandwidth limit

$A_r$  : effective area of horn

The power fluctuations are :

$$\Delta P = \frac{\partial P}{\partial T} * \Delta T \quad [3]$$

then

$$\frac{\partial P}{\partial T} = \frac{A_r}{2} \int_{f_1}^{f_2} \iint_{4p} f_n(q, j) \frac{\partial B(q, j, f, T)}{\partial T} d\Omega df \quad [4]$$

$$\frac{\partial}{\partial T} (B(q, j, f, T)) = \left(\frac{2 \cdot h^2 \cdot f^4}{k \cdot c^2 \cdot T^2}\right) \cdot \frac{\exp\left(\frac{h \cdot f}{k \cdot T}\right)}{\left(\exp\left(\frac{h \cdot f}{k \cdot T}\right) - 1\right)^2} \quad [5]$$

$$\Delta P = \frac{A_r}{2} \Delta T \iint_{4p} f_n(q, j) \left(\int_{f_1}^{f_2} \frac{\partial B(q, j, f, T)}{\partial T} df\right) \cdot d\Omega \quad [6]$$

Let consider :

$$I(T(q, j)) = \int_{f_1}^{f_2} \frac{\partial B(q, j, f, T)}{\partial T} df \quad [7]$$

The fluctuating surface considered as a black body is seen by the horn inside a solid angle  $\Omega_s$ , then  $I(\theta, \varphi) = 0$  outside  $\Omega_s$  :

$$\Delta P = \Delta T \cdot \frac{A_r}{2} \iint_{\Omega_p} f_n(q, j) \cdot I(T(q, j)) \cdot d\Omega = \Delta T \cdot \frac{A_r}{2} \cdot I \cdot \iint_{\Omega_s} f_n(q, j) \cdot d\Omega \quad [8]$$

The effective area is defined by :

$$A_r = \frac{|^2}{\iint_{\Omega_p} f_n(q, j) \cdot d\Omega} \quad [9]$$

Then

$$\Delta P = \frac{\Delta T}{2} \cdot |^2 \cdot I \cdot \frac{\iint_{\Omega_s} f_n(q, j) \cdot d\Omega}{\iint_{\Omega_p} f_n(q, j) \cdot d\Omega} \quad [10]$$

The following IP quantity is the incident power computed with grasp8.

$$IP = \frac{\iint_{\Omega_s} f_n(q, j) \cdot d\Omega}{\iint_{\Omega_p} f_n(q, j) \cdot d\Omega} \quad [11]$$

On final the power fluctuation is expressed as

$$\Delta P = \frac{\Delta T}{2} * |^2 * I * IP \quad [12]$$

The detector efficiency and the surface emissivity have to be taken into account ( $\eta=1$  for the LFI and  $\eta=0.3$  for the HFI)

$$\Delta P = \frac{\Delta T}{2} * |^2 * I * IP * h * e \quad [13]$$

The integral I is numerically computed as follow :

$$I = \int_{f_1}^{f_2} \frac{\partial B(q, j, f, T)}{\partial T} df = \sum_{i=1}^N \frac{\partial}{\partial T} (B(q, j, f, T)) \cdot \Delta f \quad [14] \text{ with } \begin{cases} \Delta f = \frac{f_2 - f_1}{N} \\ f_i = f_1 + i \cdot \Delta f \end{cases}$$

Numerical computation of I.

$$I = \sum_{i=1}^N \frac{\partial}{\partial T} (B(q, j, f, T)) \Delta f \quad [15]$$

The former quantity is computed for all frequencies and for different average surface temperatures (fig 3-1).

Central frequency (GHz)	Lowest frequency (GHz)	Highest frequency (GHz)	Temperature (K)	I (ISU)
30	27	30	50	1.6646E-09
30	27	30	80	1.6647E-09
30	27	30	150	1.6647E-09
100	90	110	50	6.1608E-08
100	90	110	80	6.1638E-08
100	90	110	150	6.1652E-08
353	317.7	388.3	50	2.6857E-06
353	317.7	388.3	80	2.7016E-06
353	317.7	388.3	150	2.7090E-06
857	771.3	942.7	50	3.6656E-05
857	771.3	942.7	80	3.7948E-05
857	771.3	942.7	150	3.8559E-05

Figure 3.3-1 : Numerical integration results.

The numerical result is varying with the frequency but not with the average temperature. This is explained by looking at the Planck's law behavior and at its associated derivative. The derivative curves are quasi identical over the Planck average temperature range. (see fig 3-2 to 3-5)

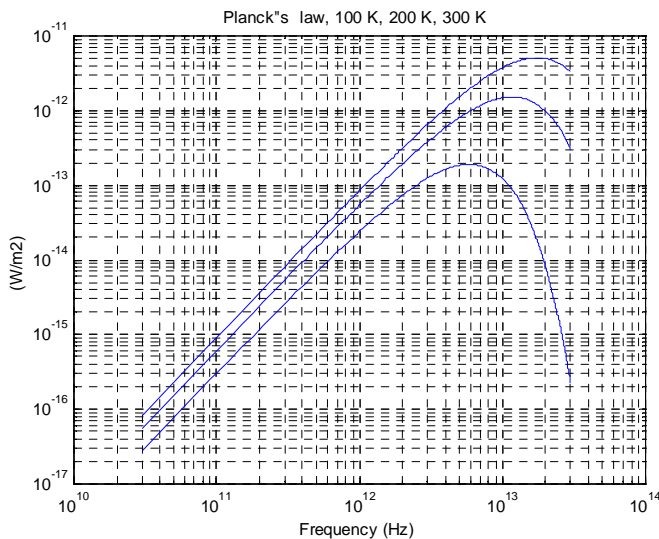


Figure 3.3-2 : Planck's law over a wide frequency domain.

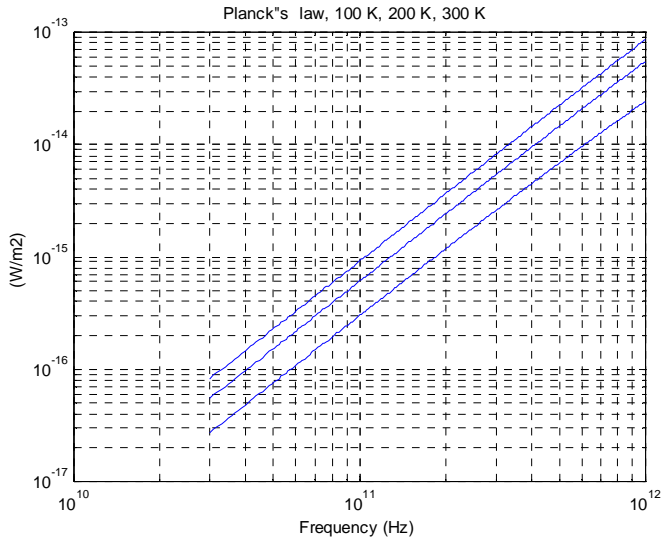


Figure 3.3-3 : Planck's law over the 30 -1000 GHz domain for 100, 200 and 300 K.

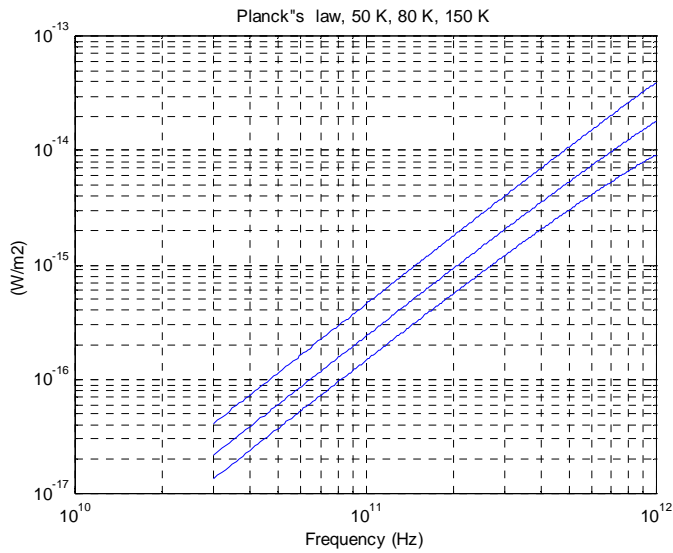


Figure 3.3-4 : Planck's law over the 30 -1000 GHz domain for 50, 80 and 150 K.

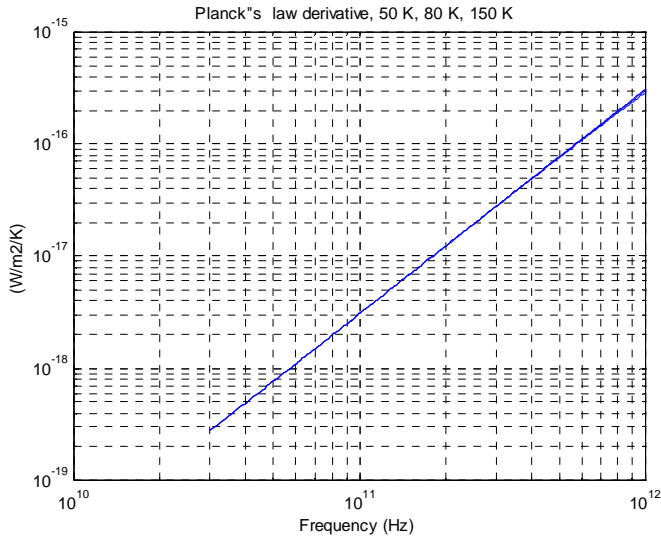


Figure 3.3-5 : Planck's law derivative over the 30 –1000 GHz domain for 50, 80 and 150 K

As a conclusion the power reaching a detector is expressed as :

$$\Delta P = \frac{\Delta T}{2} * \eta^2 * I * IP * h * \epsilon$$

where  $\eta$  is the detector efficiency ( $\eta=1$  for the LFI and  $\eta=0.3$  for the HFI )

IP is the incident power of RF coupling factor from the thermal source to the detector.

$\epsilon$  is the surface emissivity of the thermal source

$\lambda$  is the wavelength of the observation channel

$\Delta T$  is the physical thermal deviation of the thermal source.

I is the Numerical integration over the channel bandwidth of the thermal derivative of the Planck's law.

Central frequency (GHz)	I (ISU)
30	1.6646E-09
100	6.1652E-08
353	2.7090E-06
857	3.8559E-05



### 3.4 Sensitivity analysis method of the temperature fluctuation.

The former section has shown how to convert a temperature fluctuation into power fluctuation. Now it is necessary to perform the conversion for each surface of the spacecraft and to sum up all contribution.

The sensitivity analysis is performed so as to determine what are the most critical surface element wrt the performance. The first phase is then to compute the maximum theoretical fluctuation allowed for each surface considered alone.

The second phase is to weight all the obtain temperature so as to obtain a total power performance equal to the requirement

#### 3.4.1 first phase : method to compute the maximum theoretical fluctuation temperature for each surface element.

The total power reaching a detector is the linear sum of all the elementary power of each surface of the spacecraft.

$$\Delta P_{total} = \sum_{i=1}^{n\_surface} \Delta P_{surface(i)} \quad [1]$$

$$\Delta P_{total} = \sum_{i=1}^{n\_surface} \frac{\Delta T_{surface(i)}}{2} * |^2 * I * IP_{surface(i)} * h * e_{surface(i)} \quad [2]$$

n\_surface : number of fluctuating surfaces considered on the spacecraft.

Under this assumption the power allocation for each surface is the following :

$$\Delta P_{surface(i)} = a_i * \Delta P_{total} \quad [3]$$

$$\text{with } \sum_{i=1}^{n\_surface} a_i = 1$$

The temperature allocation consists in computing the temperature of each considered surface alone. This means that the considered surface will induce a power at detector level equal to the requirement.

The procedure is then :



$$\Delta P_{total} = \frac{ASD_{requirement}}{\sqrt{t_{obs}}} \quad [4]$$

$$\text{with } t_{obs} = 3600 \cdot \frac{FWHM[arc\ min]}{2.5\ arc\ min} \quad [5]$$

Then

$$\Delta T_{surface\_alone} = 2 * \Delta P_{total} / (l^2 * I * IP_{surface} * h * e_{surface}) \quad [6]$$

Then in order to take into account the other surfaces, this temperature has to be weighted.

3.4.2 second phase : method to weight the maximum theoretical fluctuation temperature for each surface element.

The sum of each individual surface contribution has to generate an amount of power at detector level lower than the requirement. Hence the weighted temperature fluctuation of each surface is

$$\Delta T_{surface} = a_i * \Delta T_{surface\_alone} \quad [7]$$

$$\text{with } \sum_{i=1}^{n\_surface} a_i = 1$$

Rem the weighting coefficient are the same as the one used in former section:



### 3.5 RF coupling factor evaluation

#### 3.5.1 Overall amount of relative power evaluation.

The TICRA RF expertise study (reference document [RD 1]) is producing the incident power or RF coupling factor from the structural element to the detector. The computed values are detailed in table 2-1. Those RF coupling factor have not been recomputed for the new baffle configuration as far as the values are already very low and provide significant margin. Anyhow those value are an update wrt the PDR configuration.

The values presented in these tables correspond to the relative incident power exchanged between the detector and the corresponding element. The computation have been performed at 30 and 100 GHz only. At 857 GHz there's numerically no RF power exchanged between the detector and any of the spacecraft elements. This is due to the location in the center of the Focal plane unit of the 857 GHz and to its gaussian radiation pattern. Hence there's no self spacecraft emission at 857 GHz.

As a worst case the 353 GHz incident power numerical value are considered to be the ones at 100 GHz.

The following table shows a significant difference between the relative power exchanged with a structural element inside or outside the baffle cavity.





Structural element	Method used in analysis	Total relative power. Field from the 30 GHz LFI27 feed.	Total relative power. Field from the HPI_100_1 feed at 100 GHz
Baffle A	1	0.000168	0.000457
Baffle B	1	0.000310	0.000536
Baffle C	1	0.000249	0.000220
Baffle D	1	0.000081	0.000111
Baffle E	1	0.000183	0.000164
Baffle F	1	0.000674	0.000404
Baffle G	1	0.000417	0.000304
Baffle H	1	0.000085	0.000178
FPU	1	0.000047	0.000124
Hexagon side 2	1	0.000002	7.4E-7
Groove 3	1 and 2	1.09E-7 (Method 1)	1.95E-8 (Method 1)
Solar array	2	5.5E-13	1.1E-14
SVM shield	2	4E-13	3.5E-15
Side A of the SVM box	2	8.6E-15	2.4E-18

table 2-3.5-1 : output of the TICRA RF expertise.



### 3.5.2 Relative power evaluation passing through the MLI.

The SVM is covered by a MLI for thermal purposes. This MLI is composed of 15 layers made of Aluminium with a thickness of 800 angströms (0.08<sup>e</sup>-6 m). From the RF point of view these successive layers of thin metallic sheet have a frequency dependent behavior wrt the frequency range. The MLI has a transmission coefficient decreasing with the frequency.

This sub section introduces the detailed computation of the relative power passing through the MLI and going to the structural top of the SVM. In that case the emissivity of the structural element is 0.95.

The first step consists in computing the equivalent number of skin depth (thickness) at each frequency.

Frequency (GHz)	30	100	353	857
skin depth (m)	4.770E-07	2.610E-07	1.390E-07	8.900E-08
MLI thickness	8.00E-08	8.00E-08	8.00E-08	8.00E-08
Number of layer	15	15	15	15
total thickness (m)	1.20E-06	1.20E-06	1.20E-06	1.20E-06
Equivalent number of thickness	2.52	4.60	8.63	13.48

The second step consists in computing the RF power attenuation knowing that for 1 skin depth the attenuation is  $10 \cdot \log(e) = 10 / \ln(10) = 4.3$  dB.

Power attenuation for 1 skin depth (dB)	4.3	4.3	4.3	4.3
Total power attenuation (dB)	10.82	19.77	37.12	57.98

On final each relative power is computed through the MLI.

Rem : The relative power at 353 GHz is assumed to be the same as the one at 100 GHz (conservative approach).

	30 GHz	100 GHz	353 GHz
<b>Solar Array</b>			
Solar array top of MLI	5.50E-13	1.10E-14	1.10E-14
Solar array structural face (below the MLI)	4.56E-14	1.16E-16	2.13E-18
<b>SVM shield</b>			
SVM shield top of MLI	4.00E-13	3.50E-15	3.50E-15
SVM shield structural face (below the MLI)	3.31E-14	3.69E-17	6.79E-19
<b>SVM walls</b>			
Side A of SVM box top of MLI	8.60E-15	2.40E-18	2.40E-18
Side A of SVM structural face (below the MLI)	7.12E-16	2.53E-20	4.66E-22



### 3.6 Self spacecraft emission evaluation

#### 3.6.1 Methodology to check the compliance with the specifications.

To check compliance with the specifications, which are given in terms of ASD [ $W/Hz^{1/2}$ ], the following must be compared:

$$\Delta P_{\text{detector}} < \frac{ASD}{\sqrt{t_{\text{obs}}}} \qquad \Delta P = \frac{\Delta T}{2} * l^2 * I * IP * h * e$$

where:

$$t_{\text{obs}} = 3600 \cdot \frac{FWHM [\text{arc min}]}{2.5 \text{ arc min}}$$

$\Delta T$  is obtained by computing the ASD of the temporal thermal law over 7200 s.

$$\text{Then } \Delta T = \frac{ASD(T(t))}{\sqrt{t_{\text{obs}}}}$$

Hence the following value has to be compared to the requirements.

$$ASD(\text{Power}) = \frac{1}{2} * l^2 * I * IP * h * e * ASD(T(t))$$



### 3.6.2 Self spacecraft emission for Planck .

For each structural element of the SVM a time domain thermal law has been computed and Fourier transformed for the QR. The reference documents RD2 contain the thermal QR analysis..

For the PLM elements, the direct component at 1/60 Hz has been used.

The following table displays the comparison of the computed thermal deviation obtained at 1/60 Hz. The ASD thermal performance expressed in  $K/Hz^{1/2}$  is divided by the observation defined for each channel. Then the corresponding  $\Delta T$  at 1/60Hz is displayed for each channel.

In the following table the input for the PLM elements (PR, SR , groove 3) are not changed since the CDR. The other ones have been updated according to [RD 2].

	ASD	ASD	DT	DT	DT	DT
	requirement	performance	1/60 Hz	1/60 Hz	1/60 Hz	1/60 Hz
	at 1/60 Hz	at 1/60 Hz	30 GHz	100 GHz	353 GHz	857GHz
	(K/Hz <sup>1/2</sup> )	(K/Hz <sup>1/2</sup> )	(mK)	(mK)	(mK)	(mK)
PR circular central part			0.2	0.2	0.2	0.2
PR Upper part (moon limited part)			1.3	1.3	1.3	1.3
PR circular outer part			1.1	1.1	1.1	1.1
SR		6.00E-07	2.89E-03	5.00E-03	7.07E-03	7.07E-03
BAFFLE			45	5.00E-03	5.00E-03	45
GROOVE 3 (baffle floor inside the optical cavity)			45	45	45	45
MLI OF THE SVM UPPER PANEL (+X Face)	0.01	1.48E-06	6.78E-03	1.23E-02	1.74E-02	1.74E-02
GROOVE 3 (outside the optical cavity)	0.01	1.10E-04	5.05E-01	9.17E-01	1.30E+00	1.30E+00
MLI of the SVM lateral panel (side of SVM box)	0.01	1.02E-07	4.68E-04	8.50E-04	1.20E-03	1.20E-03
Solar array +X face of the MLI	0.01	2.81E-07	1.29E-03	2.34E-03	3.31E-03	3.31E-03

Table 3.6-1 : spacecraft temperature results from thermal analysis (see RD2)



The following tables display the ASD computed using the data coming from the thermal analysis. Only the surface element inside the optical cavity are taken into account. This choice is justified because the impact of the element outside the optical cavity is many order of magnitude lower than the one inside the optical cavity.

A system contingency is defined as 20% of the requirement This system contingency is then summed up in order to obtain the total performance.

	F (GHz)	$\lambda$ mm	Eta	I(SI)	tobs (s)
	30	10	1	1.66E-09	47520
		DT	Emissivity		ASD
		Performance	of the	IP	Performance
		at 1/60 Hz	surface		(W/Hz <sup>0,5</sup> )
		$\mu$ K			
PR circular central part		0.2000	0.02	2.58E-01	4.67E-20
PR Upper part		1.3000	0.02	6.14E-04	7.22E-22
PR Circular outer part		1.1000	0.02	2.58E-01	2.57E-19
SR		0.0029	0.02	1.00E+00	2.62E-21
Baffle		45.0000	0.05	2.17E-03	8.83E-20
Groove 3 (baffle floor inside the optical cavity)		45.0000	0.05	2.00E-06	8.14E-23
system contingency (20%)					6.80E-19
TOTAL ASD (W/Hz <sup>0,5</sup> )					1.08E-18
ASD SPEC (W/Hz <sup>0,5</sup> )					3.40E-18

table 3.6-2 : 30 GHz channel ASD performance display (worst case component at 1/60 Hz).



	F (GHz)	l mm	Eta	l(SI)	tobs (s)
	100	3.00E+00	0.3	6.16E-08	14400
		DT	Emissivity		ASD
		Performance	of the	IP	Performance
		at 1/60 Hz	surface		(W/Hz <sup>0,5</sup> )
		mK			
PR circular central part		0.2	2.00E-02	0.258	1.14428E-19
PR Upper part		1.3	2.00E-02	0.000614	1.77009E-21
PR Circular outer part		1.1	2.00E-02	0.258	6.29355E-19
SR		0.005	0.02	1	1.1088E-20
Baffle		45	0.05	0.0021700	4.87234E-20
Groove 3 (baffle floor inside the optical cavity)		45	0.05	0.0000020	4.49064E-23
system contingency (20%)					4.2E-19
TOTAL ASD (W/Hz <sup>0,5</sup> )					1.22541E-18
ASD SPEC (W/Hz <sup>0,5</sup> )					2.1E-18

table 3.6-3 : 100 GHz HFI channel ASD performance display (worst case component at 1/60 Hz).

	F (GHz)	l mm	Eta	l(SI)	tobs (s)
	353	8.50E-01	0.3	2.70E-06	7200
		DT	Emissivity		ASD
		Performance	of the	IP	Performance
		at 1/60 Hz	surface		(W/Hz <sup>0,5</sup> )
		mK			
PR circular central part		0.2	2.00E-02	0.258	6.40588E-20
PR Upper part		1.3	2.00E-02	0.000614	9.90925E-22
PR Circular outer part		1.1	2.00E-02	0.258	3.52323E-19
SR		0.00707	0.02	1	8.77705E-21
Baffle		45	0.05	0.00217	1.21228E-19
Groove 3 (baffle floor inside the optical cavity)		45	0.05	0.000002	1.1173E-22
system contingency (20%)					4.2E-19
TOTAL ASD (W/Hz <sup>0,5</sup> )					9.67E-19
ASD SPEC (W/Hz <sup>0,5</sup> )					2.1E-18

table 3.6-4 : 353 GHz channel ASD performance display (worst case component at 1/60 Hz).

As far as there's no RF power exchanged between the detector and the spacecraft surfaces there's no self spacecraft emission level at 857 GHz from a numerical point of view.

As a conclusion the self spacecraft emission level is well below the requirements.



#### 4. SELF SPACECRAFT EMISSION LEVEL CONCLUSIONS.

The section 3.6.2 shows two main results. The first one is that the self spacecraft emission level is driven by the PLM elements contained inside the baffle cavity. The synthesis table (3.6-2 & 3.6-3 & 3.6-4) show a performance lower than the requirement which is recalled hereafter :

\*\*\*\*\*

The ASD ( in Watts /  $\sqrt{\text{Hz}}$  ) of each frequency component between 0.01 Hz and 100 Hz shall be such that :

Frequency [ GHz ]	ASD [ Watt / $\sqrt{\text{Hz}}$ ]
30	< 3.4 E-18 X
100 ( LFI )	< 1.1 E-17 X
100 ( HFI )	< 2.1 E-18 X
353	< 1.8 E-18 X
857	< 2.2 E-17 X

**Note :**

X is equal to one for any frequency component  $f_o$  of the fluctuation source synchronous with the Planck S/C spinning rate ( i.e. multiple of  $f_{\text{spin}} = 1 / 60$  Hz ).

Otherwise ,  $X = ( B * t_{\text{obs}} * \Delta f )$  , where  $\Delta f = f_o - k * f_{\text{spin}}$  and k is chosen to minimise  $\Delta f$  .

$t_{\text{obs}} = 3600 * \text{FWHM} / 2.5 \text{ arcmin}$  , and FWHM is the angular resolution of the antenna radiation pattern in arc minutes .



## 5. ANALYSIS OF THE RESULTS OF THE 4 PI COMPUTATIONS WITH THE BAFFLE EXTENSION USING INSTRUMENT FEED MODEL (4PI-EXT BAF-INST FEED)

This section presents the re-run of the TICRA grasp file where the gaussian feed models have been replaced by the computed radiation pattern of the actual feed (QM or FM). No other parameters have been changed. The feeds are located at the same position with the same polarization orientation at detector level for the polarized detector. In other word all geometrical elements are defined in [RD 5] and the RF feed models are defined in [RD 6] and [RD 7].

In addition for each frequency, two computations have been performed : one for each polarization of the detector in the focal plane in line with the detector orientation provided by the instruments.

Then the sub area where the Moon is located (half cone angle of  $32^\circ$  along the spacecraft spin axis) is extracted. The maximum directivity within this area is labelled the Edge of Cone (EOC) directivity. This directivity is then compared to the maximum on axis gain in order to obtain the achieved rejection.

The same process is applied for the Earth and Sun.

The modeling are performed using the up to date available data (see [RD 6] and [RD 7]). Hence the following data have been used :

- 30 GHz LFI detector radiation pattern (see [RD 6]) , dual orthogonal polarization
- 100 GHz HFI horn pattern (see [RD 7]) , dual orthogonal polarization
- 353 GHz HFI horn pattern (see [RD 7 ])
- 857 GHz no computation as far as multi moded horn characteristic is not available.

On final a table summarizes the performances for the rejection toward Earth Sun and Moon.



## 5.1 30 GHz Pattern analysis(4pi-ext baf-inst feed)

The following figure (fig 5.1-1) displays the 4 PI radiation pattern of the LFI 30 GHz radiation pattern inserted in the Planck geometry. The computation is performed as explained in (RD 8]. The numerical computation is performed as different sequence of ray combination or physical optics local computations. Then all elementary pattern are recombined so as to provide the 4 Pi radiation pattern. As visible on the following figure a sub pattern (see square shape) located between phi values of 90° to 105° and theta values of 97.5° to 122.5° is badly located. The error is not located in the computation itself but in the parameters setting of the different pattern window size. Unfortunately the investigation are not over for the release of this document.

Anyhow all pattern corresponding to all elementary ray combination are computed and ready to be recombined.

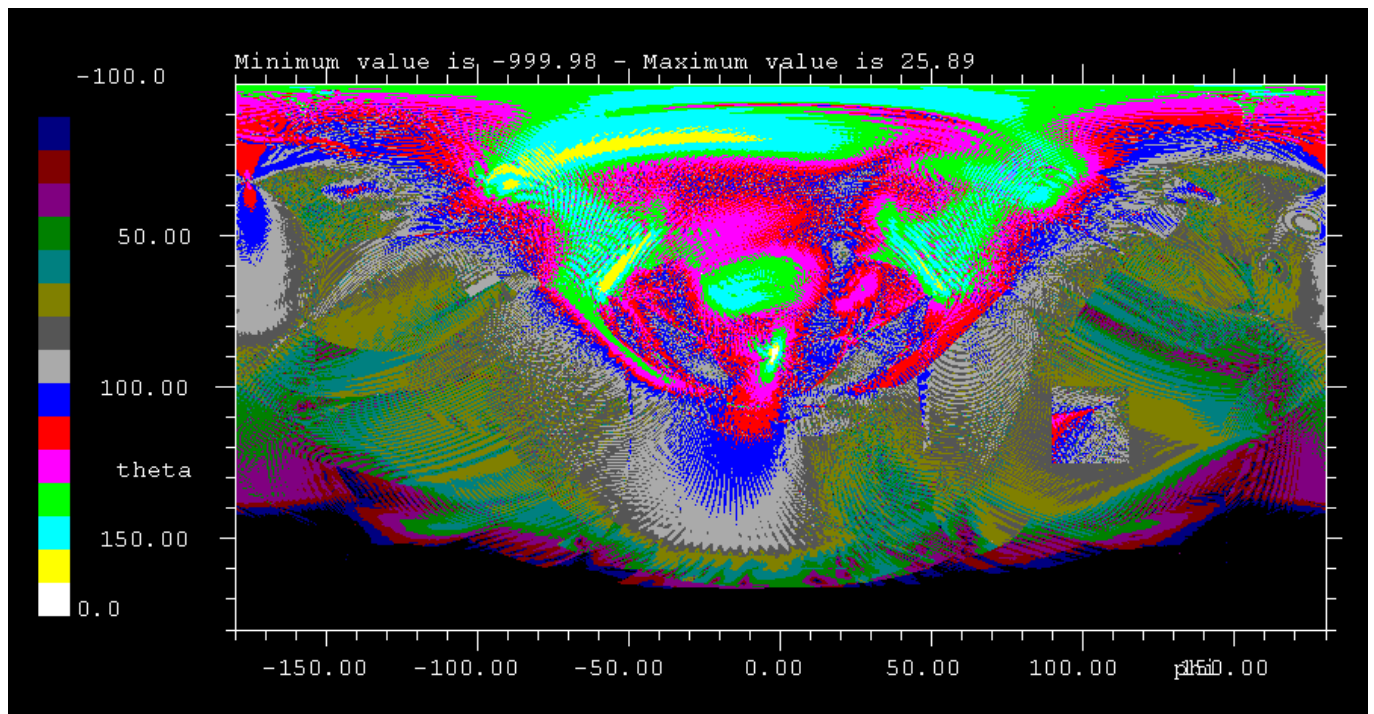


Figure 5.1-1 : 4PI diagram , phi : -180°, 180° / theta : 0,+180° / levels in directivity displayed from -100 dBi to +0 dBi (first component, Xpol)

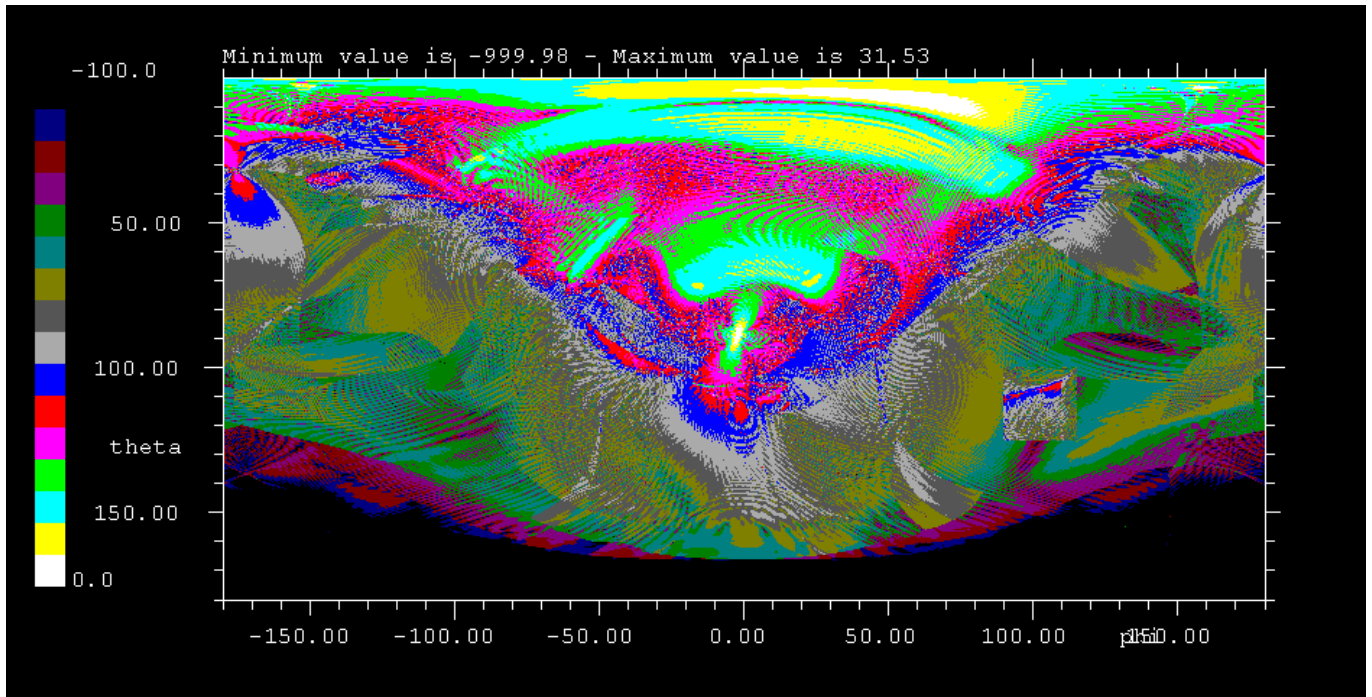


Figure 5.1-2 : 4PI diagram , phi :  $-180^{\circ}$ ,  $180^{\circ}$  / theta :  $0^{\circ}$ ,  $+180^{\circ}$  / levels in directivity displayed from -100 dBi to +0 dBi (second component, co-pol)

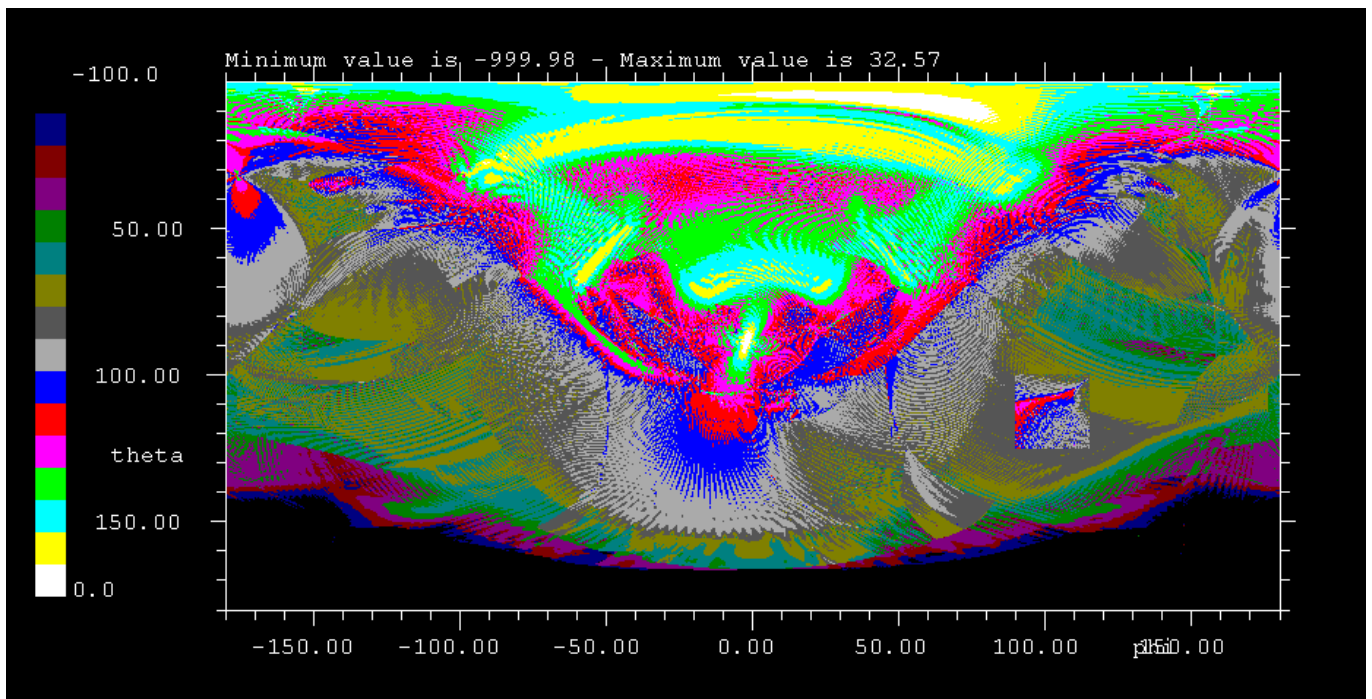


Figure 5.1-3 : 4PI diagram , phi :  $-180^{\circ}$ ,  $180^{\circ}$  / theta :  $0^{\circ}$ ,  $+180^{\circ}$  / levels in directivity displayed from -100 dBi to +0 dBi (local major/minor component)



## 5.2 100 GHz Pattern analysis(4pi-ext baf-inst feed) 1<sup>st</sup> detector polarisation orientation

The detector phase center is located in the RDP coordinate such that :

x:-47.57 mm, y:-32.966 mm, z: 14.847 mm

The X\_axis vector of the detector coordinate system is :

x\_axis (x: 0.99540745 , y:-0.00331985, z:-0.09567128)

The Y\_axis vector :

y\_axis (x:-0.00331985, y: 0.99760016 , z:-0.06915857)

The Z\_axis vector :

z\_axis : (x :0.09567128 , y: 0.06915857 , z:-0.99300760)

For the 1<sup>st</sup> detector polarization orientation, the polarization vector of the feed is oriented along the Y axis.

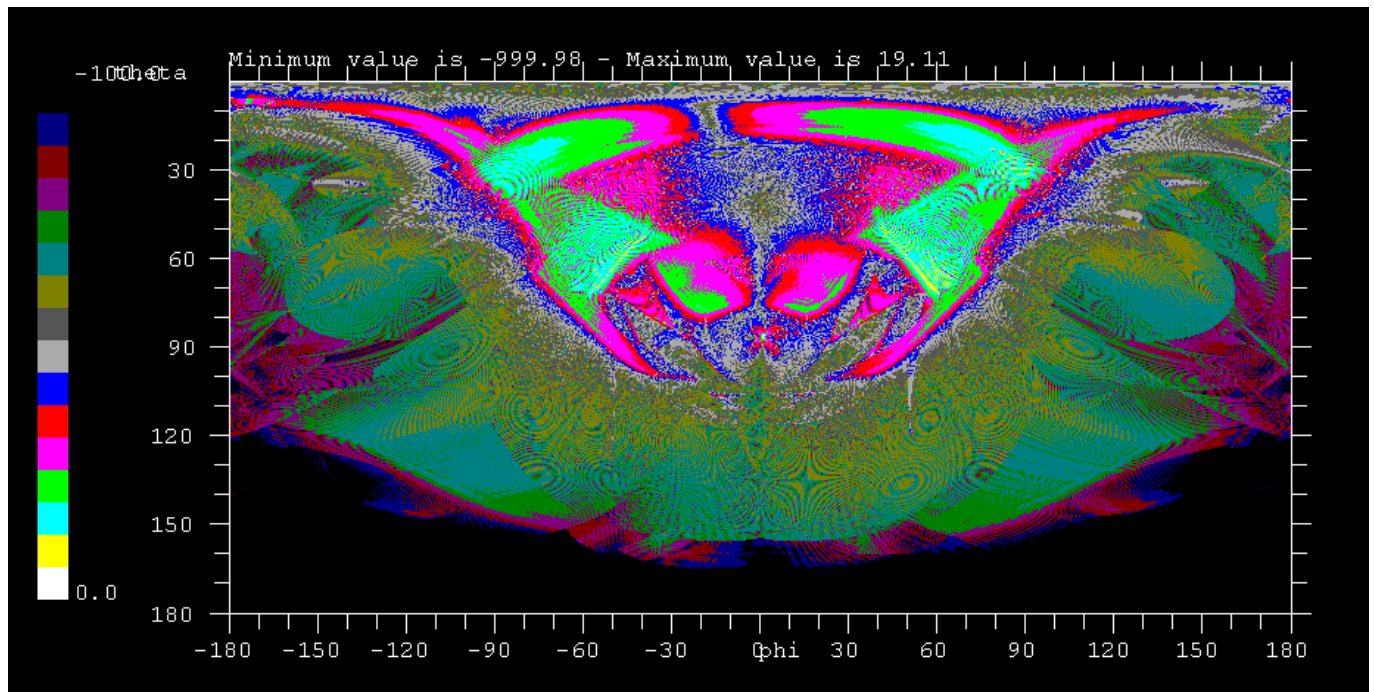


Figure 5.2-1 : 4PI diagram , phi : -180°, 180° / theta : 0,+180° / levels in directivity displayed from -100 dBi to +0 dBi (first component, Xpol)

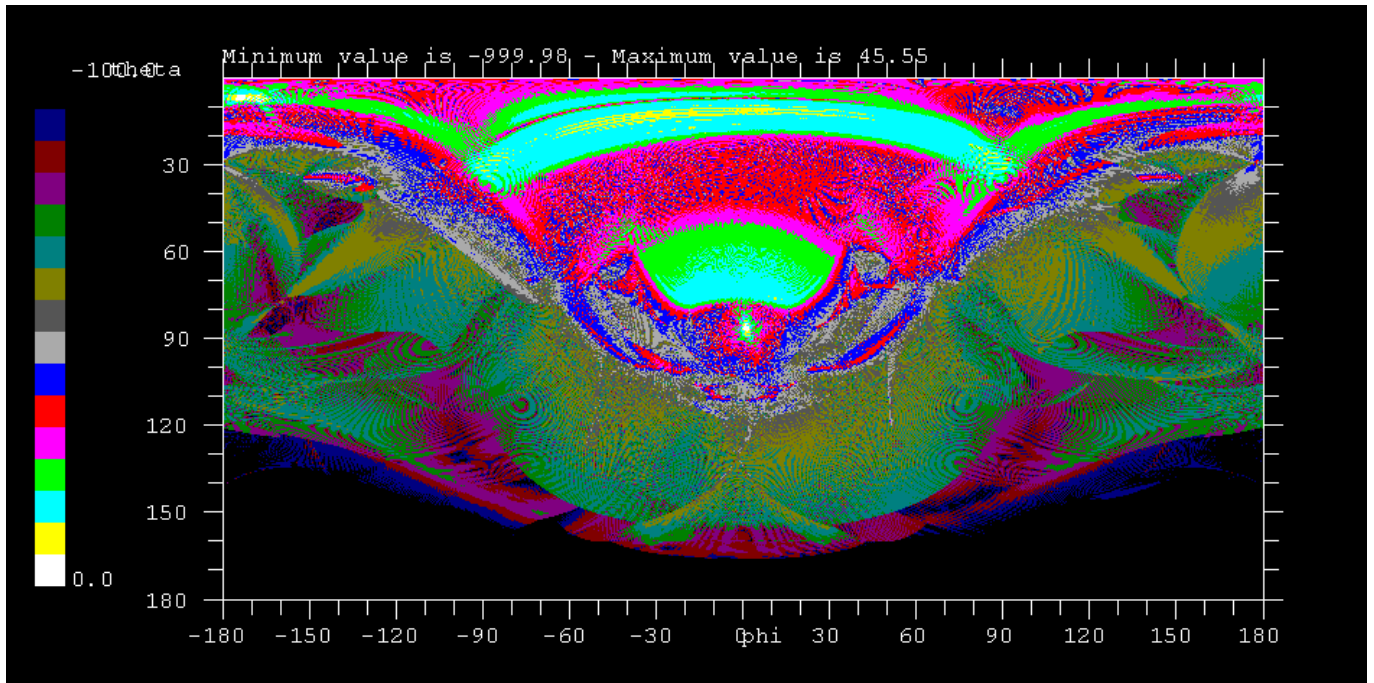


Figure 5.2-2 : 4PI diagram , phi : -180°, 180° / theta : 0,+180° / levels in directivity displayed from -100 dBi to +0 dBi (second component, co-pol)

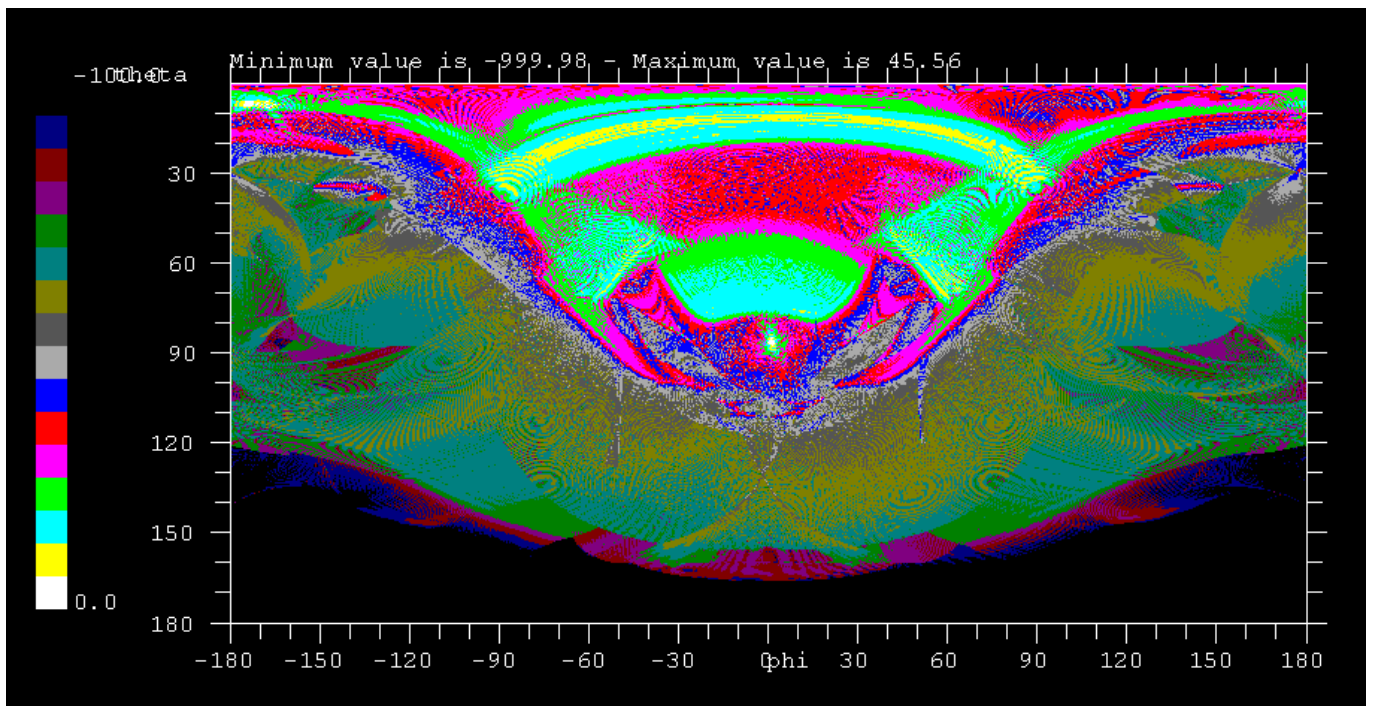


Figure 5.2-3 : 4PI diagram , phi : -180°, 180° / theta : 0,+180° / levels in directivity displayed from -100 dBi to +0 dBi (local major/minor component)

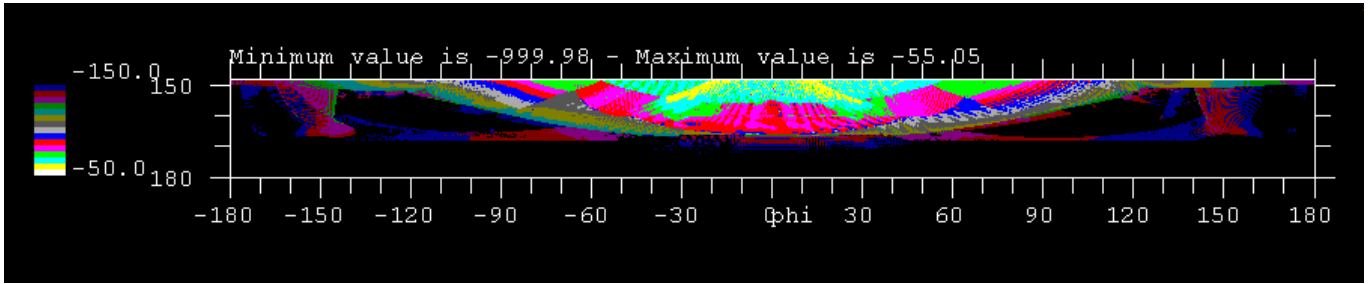


Figure 5.2-4 : Moon area phi : -180°, 180° / theta : +148°, +180° / levels in directivity displayed from -150 dBi to -50 dBi

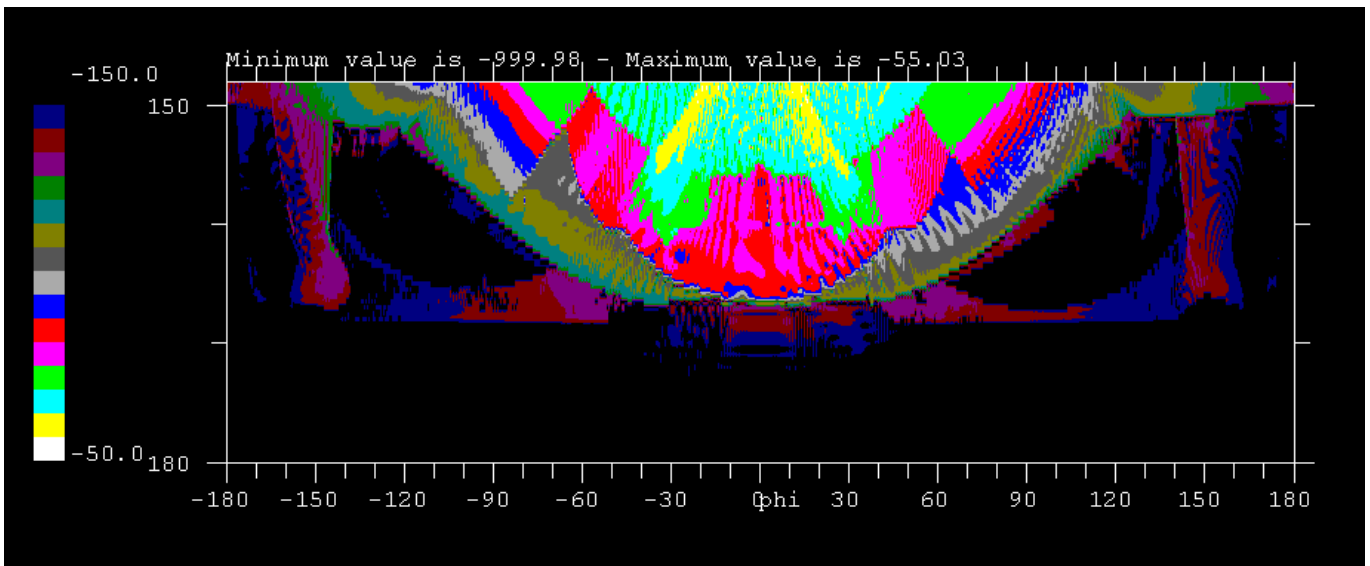


Figure 5.2-5 : enlarged Moon area phi : -180°, 180° / theta : +148°, +180° / levels in directivity displayed from -150 dBi to -50 dBi (local major/minor component)

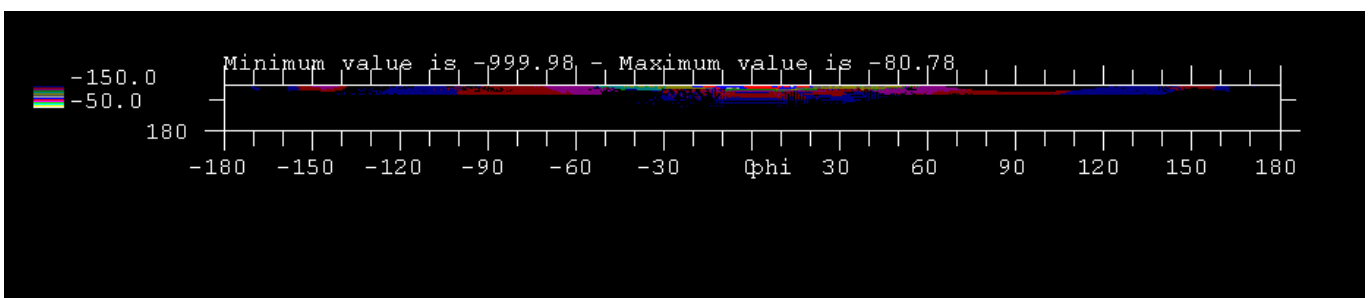


Figure 5.2-6 : Earth area phi : -180°, 180° / theta : +165°, +180° / levels in directivity displayed from -150 dBi to -50dBi (local major/minor component)

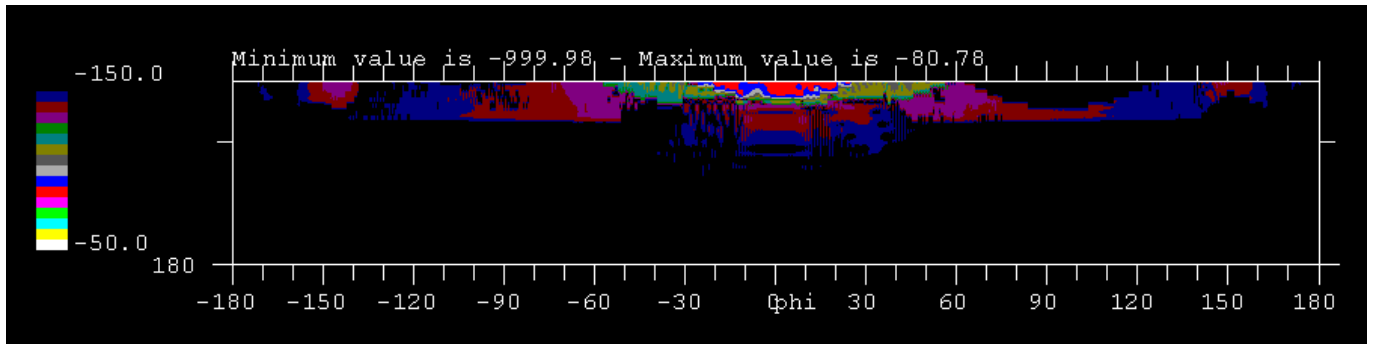


Figure 5.2-7 : Enlarged Earth area phi : -180°, 180° / theta : +165°, +180° / levels in directivity displayed from -150 dBi to -50dBi (local major/minor component)

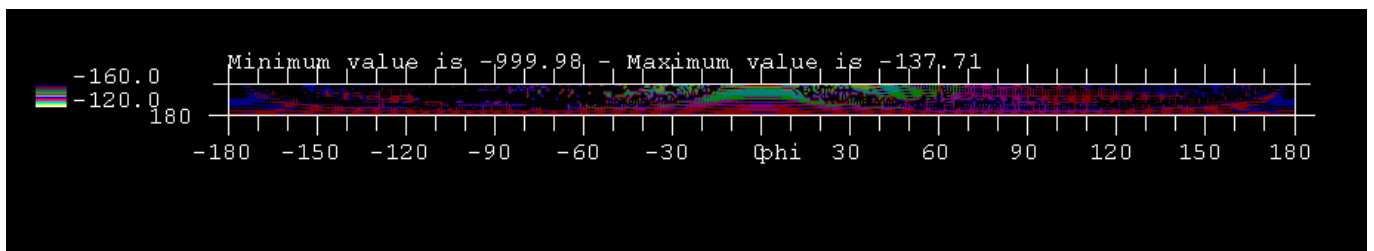


Figure 5.2-8 : Sun area phi : -180°, 180° / theta : +170°, +180° / levels in directivity displayed from -1600 dBi to -120dBi (local major/minor component)

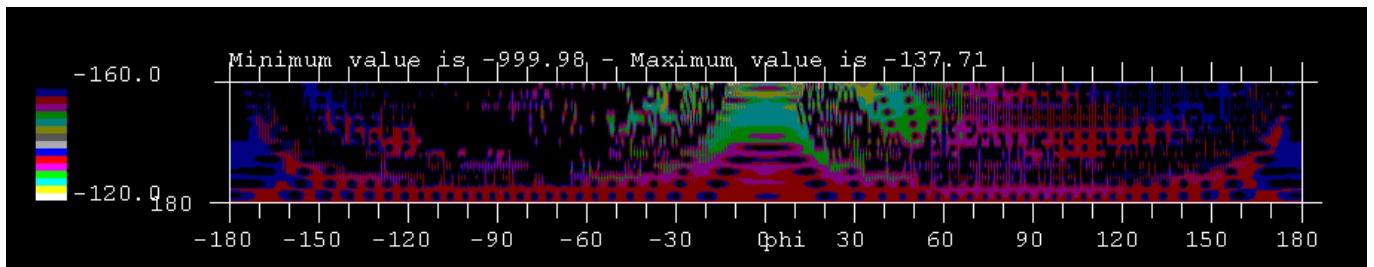


Figure 5.2-9 : Sun area phi : -180°, 180° / theta : +170°, +180° / levels in directivity displayed from -160 dBi to -120dBi (local major/minor component)

Only the main lobe area is over the -65 dB rejection.



### 5.3 100 GHz Pattern analysis(4pi-ext baf-inst feed) 2<sup>nd</sup> detector polarisation orientation

The detector phase center is located in the RDP coordinate such that :

x:-47.57 mm, y:-32.966 mm, z: 14.847 mm

The X\_axis vector of the detector coordinate system is :

x\_axis (x: 0.99540745 , y:-0.00331985, z:-0.09567128)

The Y\_axis vector :

y\_axis (x:-0.00331985, y: 0.99760016 , z:-0.06915857)

The Z\_axis vector :

z\_axis : (x :0.09567128 , y: 0.06915857 , z:-0.99300760)

For the 2<sup>nd</sup> detector polarization orientation, the polarization vector of the feed is oriented along the X axis.

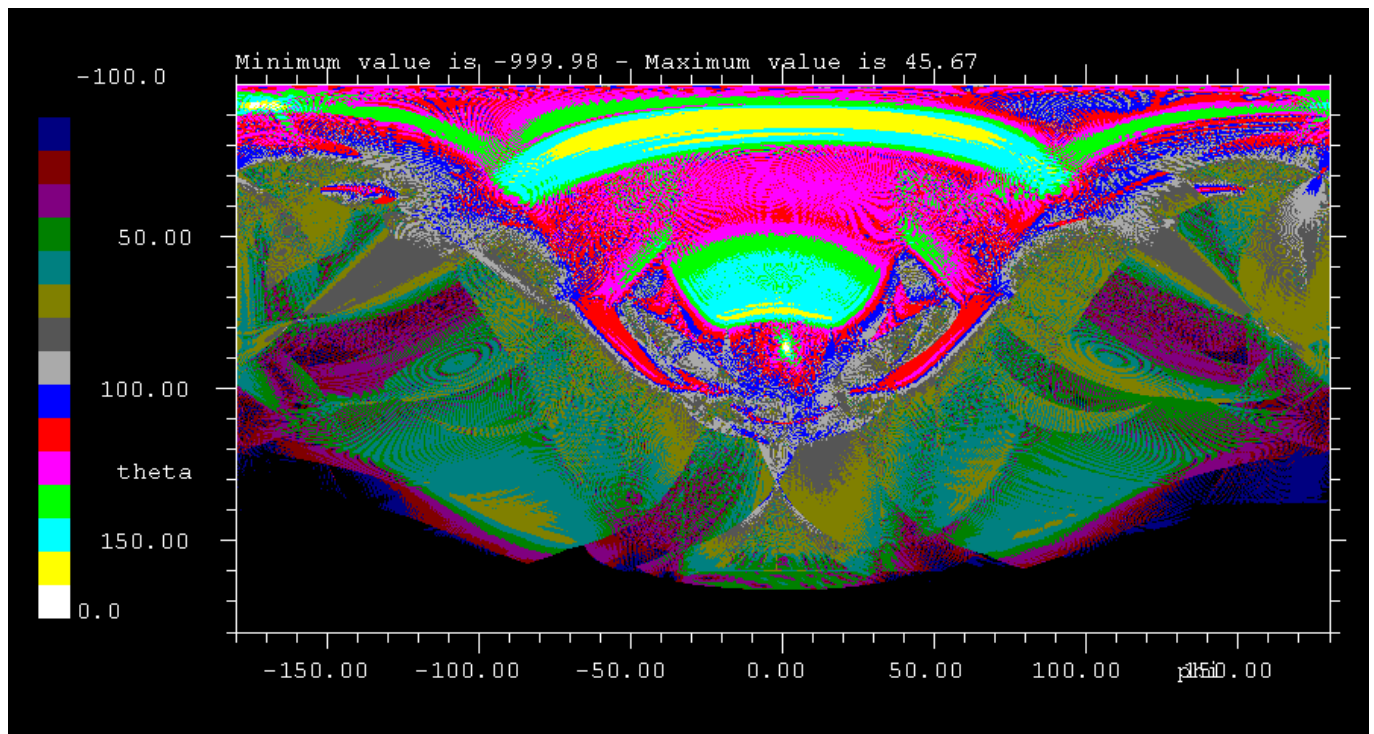


Figure 5.3-1 : 4PI diagram , phi : -180°, 180° / theta : 0,+180° / levels in directivity displayed from -100 dBi to +0 dBi (first component, Xpol)

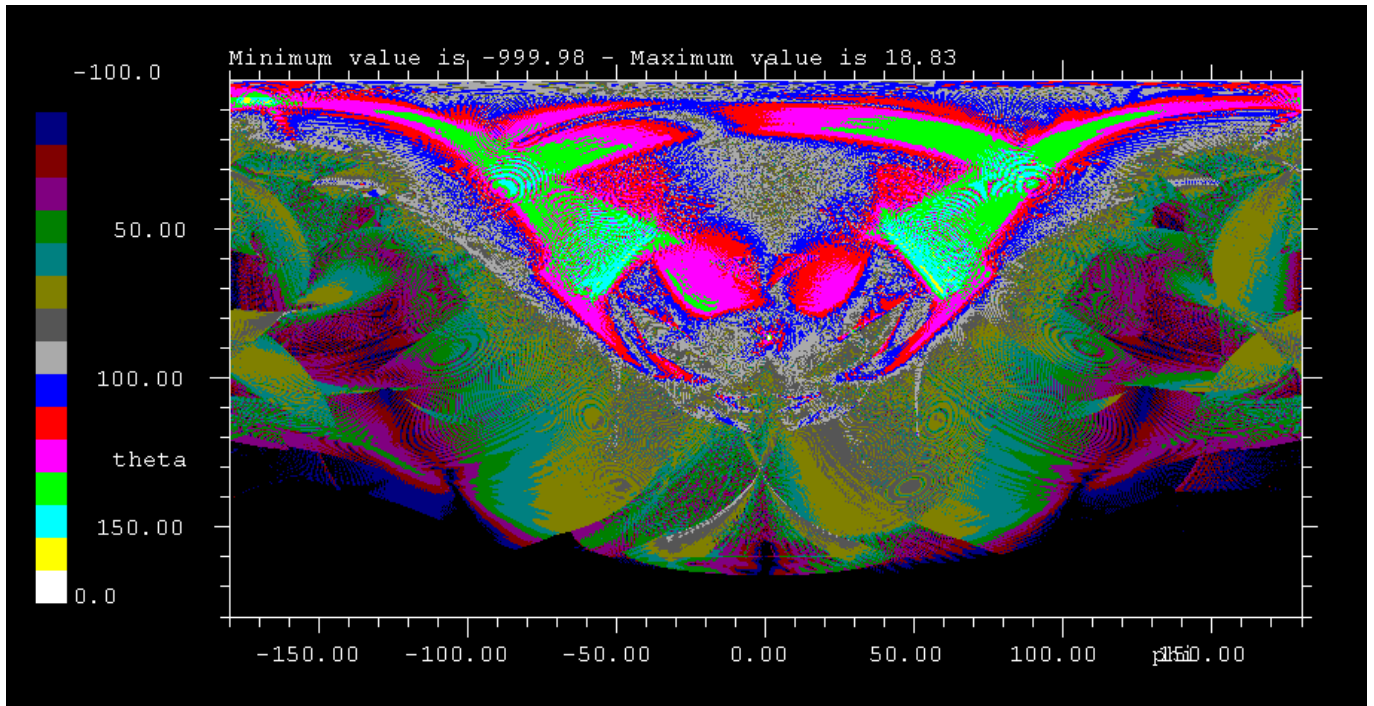


Figure 5.3-2 : 4PI diagram , phi : -180°, 180° / theta : 0,+180° / levels in directivity displayed from -100 dBi to +0 dBi (second component, co-pol)

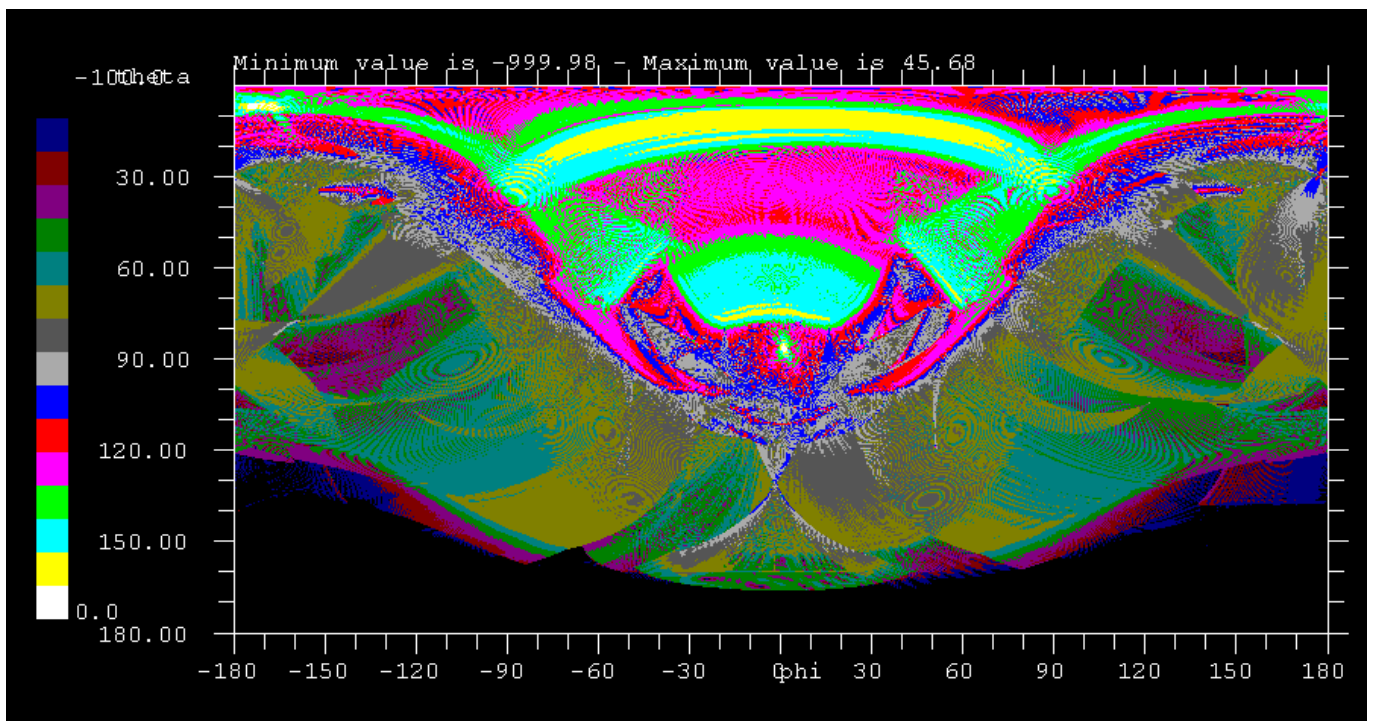


Figure 5.3-3 : 4PI diagram , phi : -180°, 180° / theta : 0,+180° / levels in directivity displayed from -100 dBi to +0 dBi (local major/minor component)



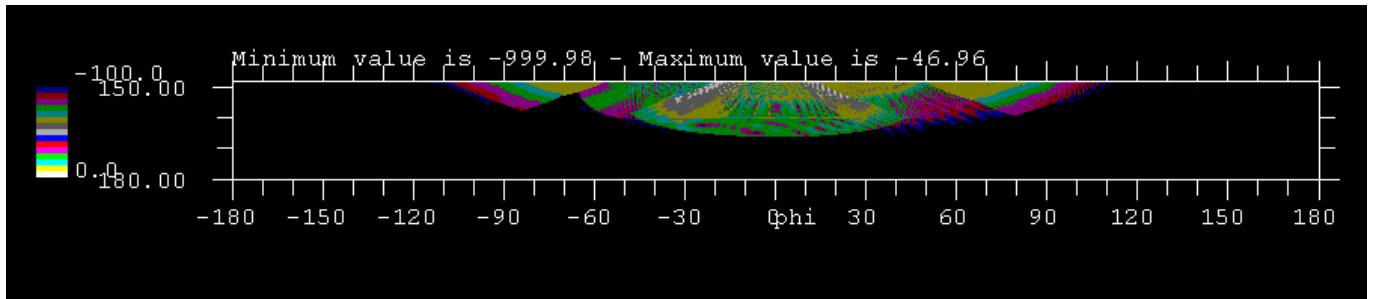


Figure 5.3-4 : Moon area phi : -180°, 180° / theta : +148°, +180° / levels in directivity displayed from -150 dBi to -50 dBi

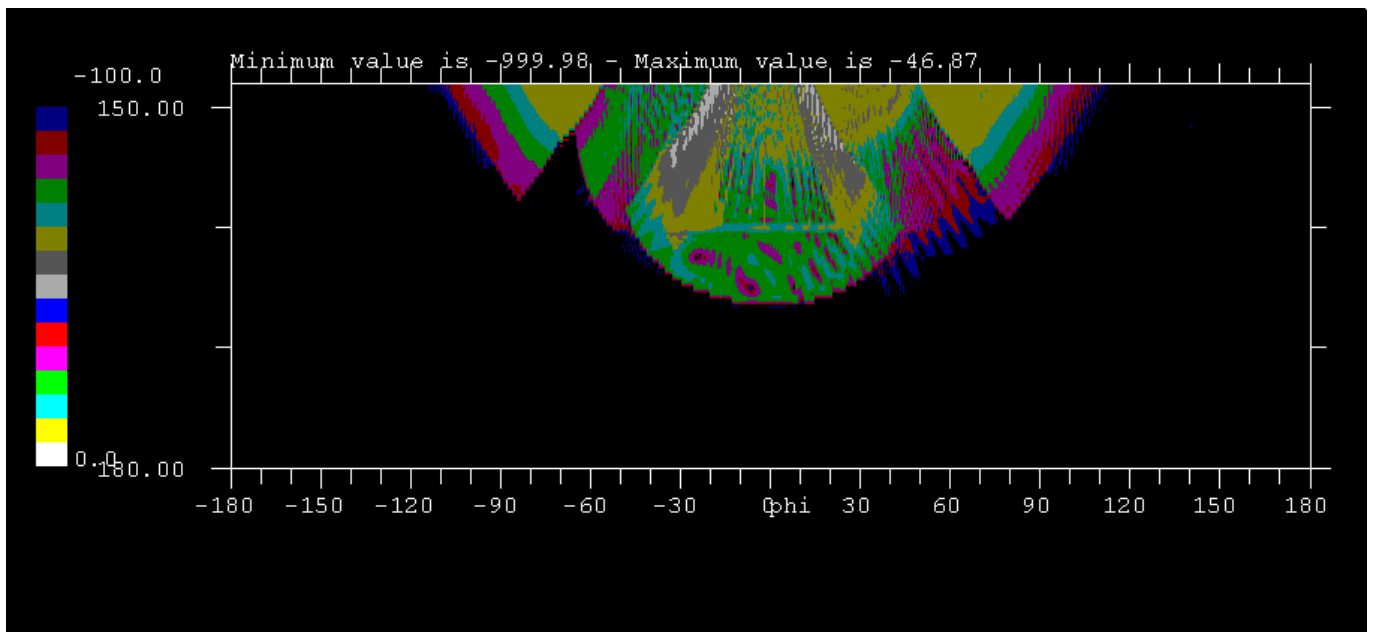


Figure 5.3-5 : enlarged Moon area phi : -180°, 180° / theta : +148°, +180° / levels in directivity displayed from -100 dBi to 0 dBi (local major/minor component)

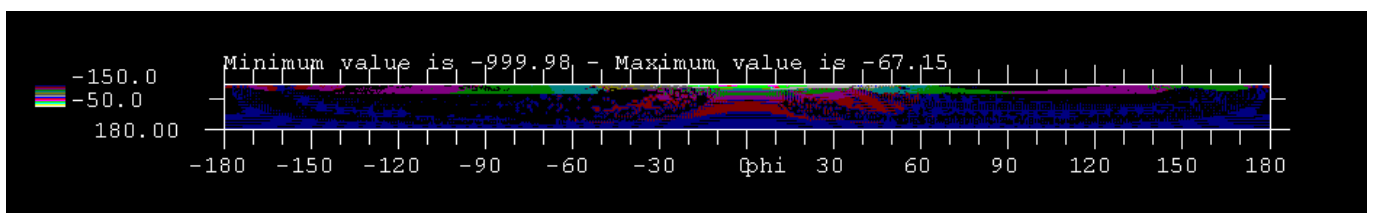


Figure 5.3-6 : Earth area phi : -180°, 180° / theta : +165°, +180° / levels in directivity displayed from -150 dBi to -50dBi (local major/minor component)

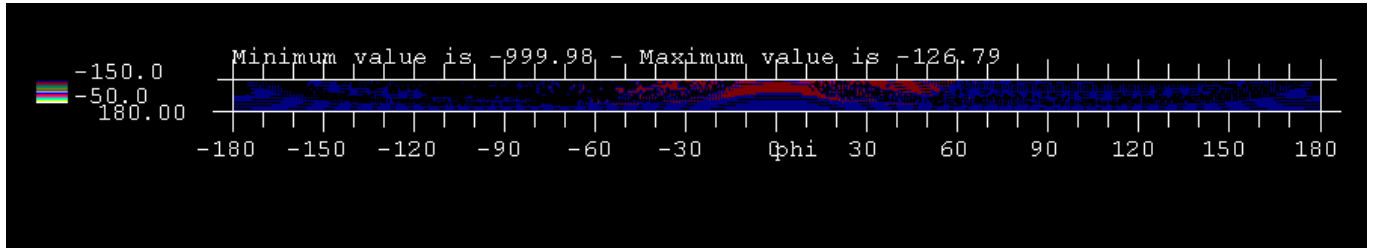


Figure 5.3-7 : Sun area phi : -180°, 180° / theta : +170°, +180° / levels in directivity displayed from -150 dBi to -50dBi (local major/minor component)



## 5.4 100 GHz pattern preliminary comparison

As far as the 100 GHz 4 pi pattern have been computed for two orthogonal polarization orientations at the focal plane level, it is then possible to compare the difference on the overall pattern.

The comparison is performed on the pattern expressed in local major/minor polarisation component. Only the major axis of polarisation ellipse is displayed and compared.

The comparison consists in computing the ratio between the major polarization axis of each pattern. The first pattern is computed as described in section 5.2 for the first polarization orientation of the detector. The second pattern is computed for the orthogonal polarization orientation (see section 5.3).

The pattern difference is performed by computing the linear ratio for each direction between the first and second pattern. Then the display is performed in dB. For graphical purpose the ratio has been performed twice (first / second) then (second / first). This is useful to obtain only coloured pixel of interest on the plots. For instance the pattern difference is plotted over a dB range (eg ratio variation from -20 dB to -10 dB and +10 dB to +20 dB). In both cases the values over the upper limit are plotted in black pixels and the values below the lower limit are plotted as red pixels. Then all red pixels have to be discarded or considered as black for graphical readability.

The figure 5.4-1 shows that very few pixels are impacted by more than 30 dB gain variation. Such variation can be attributed to the coarse meshing of  $0.5^\circ$  by  $0.5^\circ$ . The highest variation are obtained in the Earth Sun and Moon cone are (theta values varying from  $148^\circ$  to  $180^\circ$ ).

The figure 5.4-3 displays some quasi continuous area (not only isolated pixel) where the gain variation is between (+10 dB and +20 dB) and (-20 dB and -10 dB). This area is located between  $\phi = -150^\circ$  and  $\phi = -100^\circ$  and  $\theta = 70^\circ$  to  $\theta = 90^\circ$ .

On final the figure 5.4-4 and 5.4-5 show that almost all pattern direction are affected by the polarization detector orientation change by a value of 10 dB.

As a conclusion a raw result is that the detector polarization rotation by  $90^\circ$  generate a pattern global pattern difference of 10 dB on the far out side lobes.

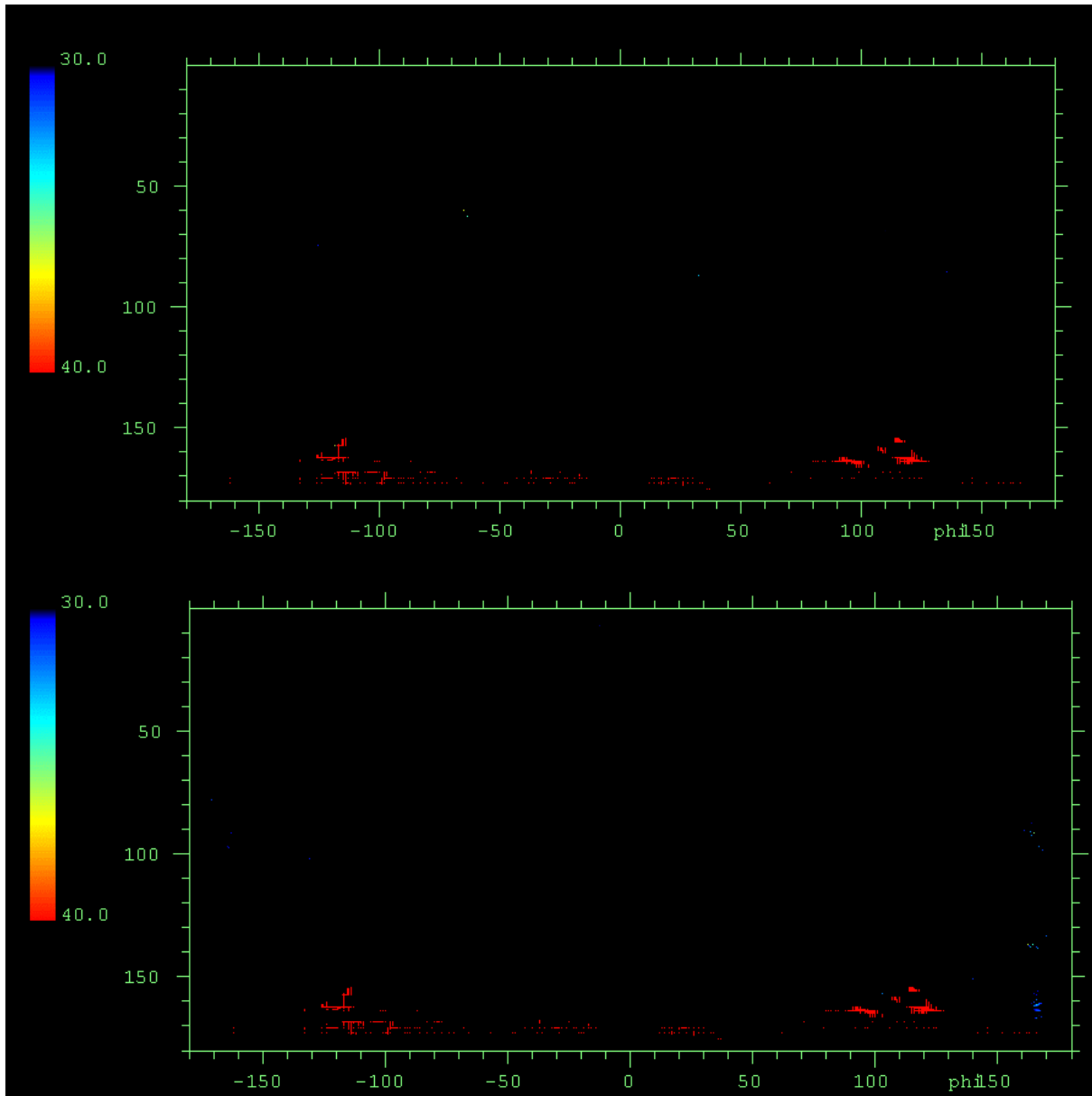


Figure 5.4-1 : local area modified by more than 30 dB (red pixels to be disregarded)

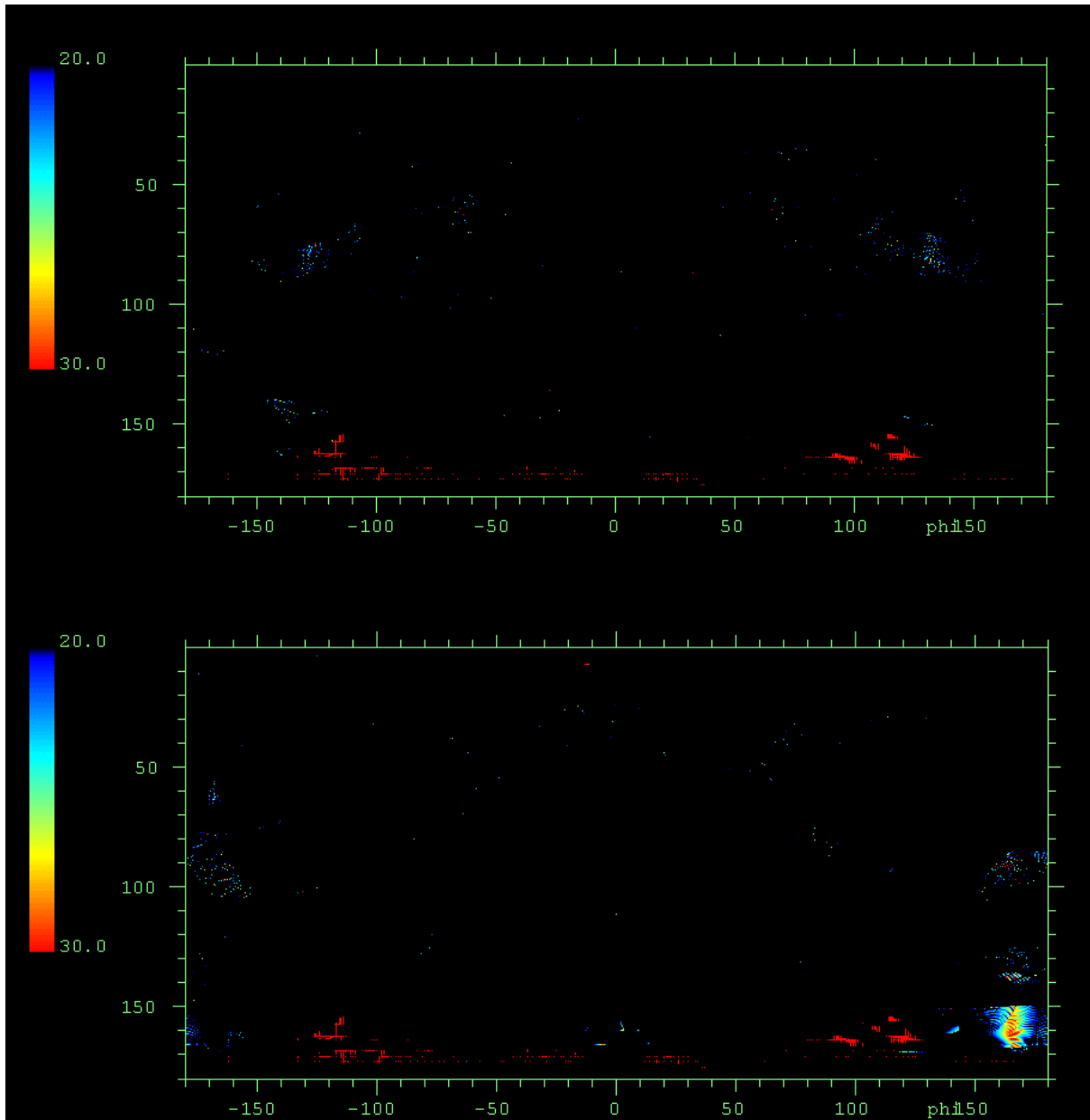


Figure 5.4-2 :local area modified by more than 20 dB (red pixels to be disregarded).

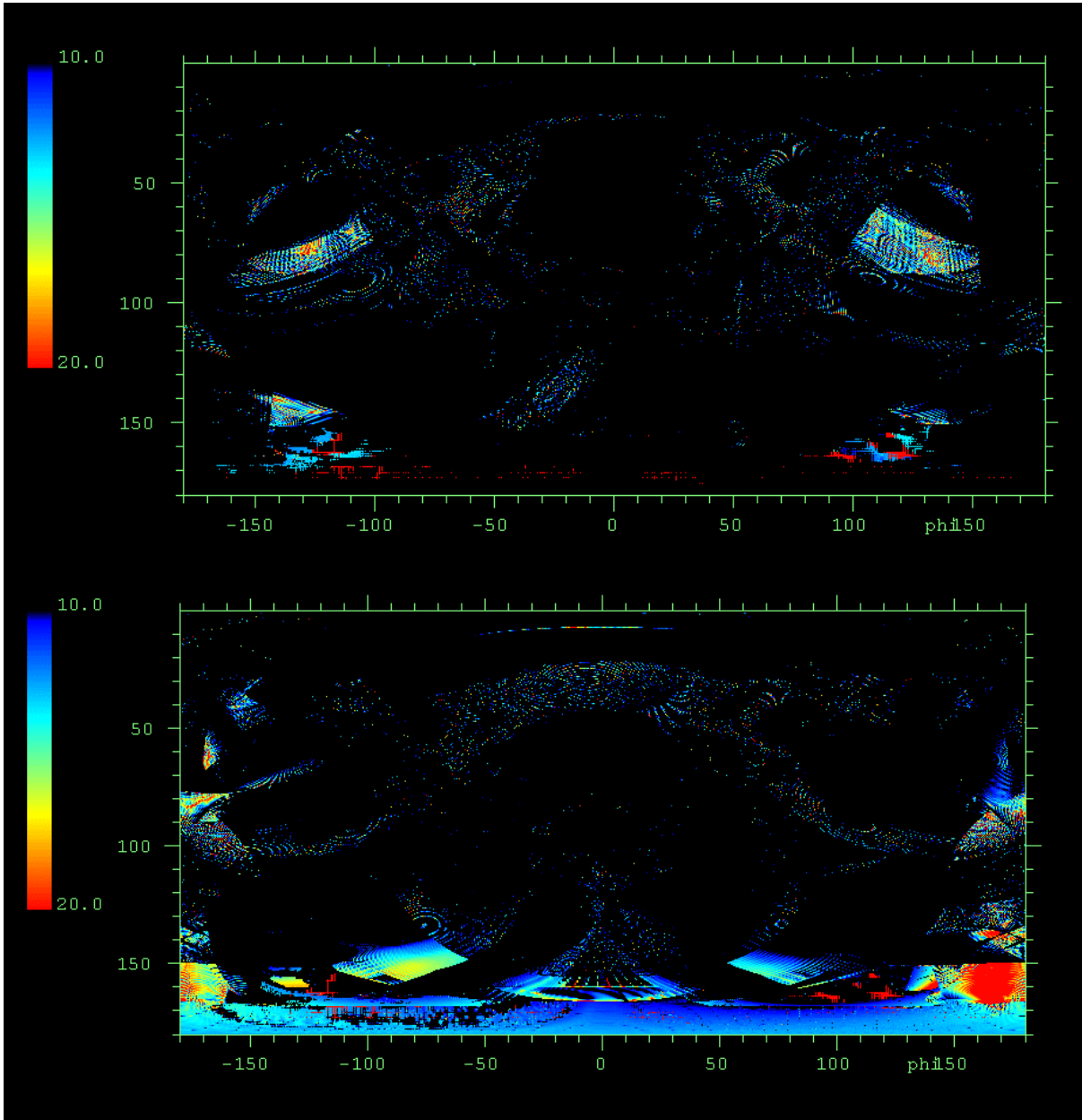


Figure 5.4-3 : local area modified by more than 10 dB and no more than 20 dB (red pixels to be discarded)

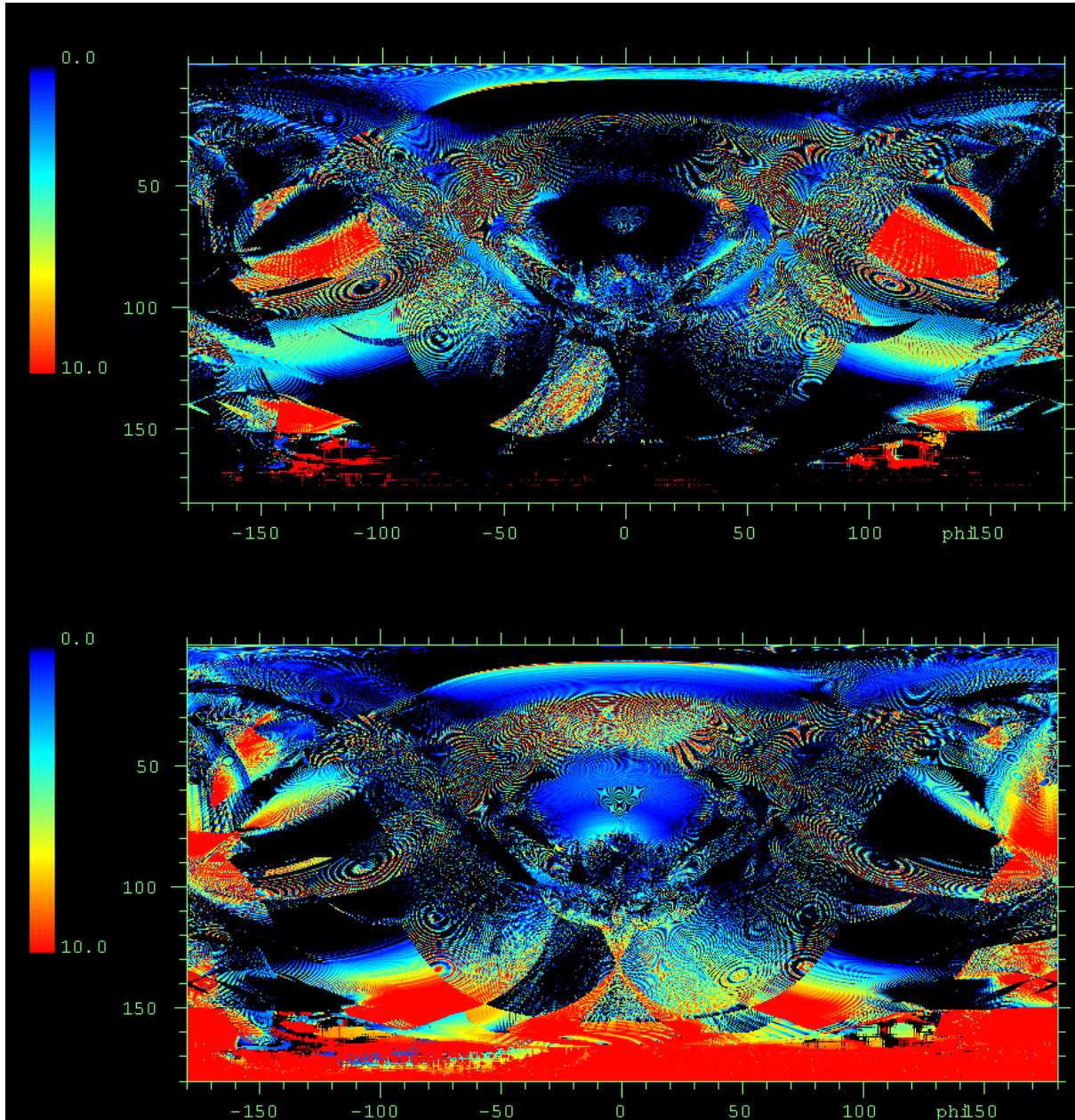


Figure 5.4-4 local area modified by more than 10 dB (red pixels to be disregarded).



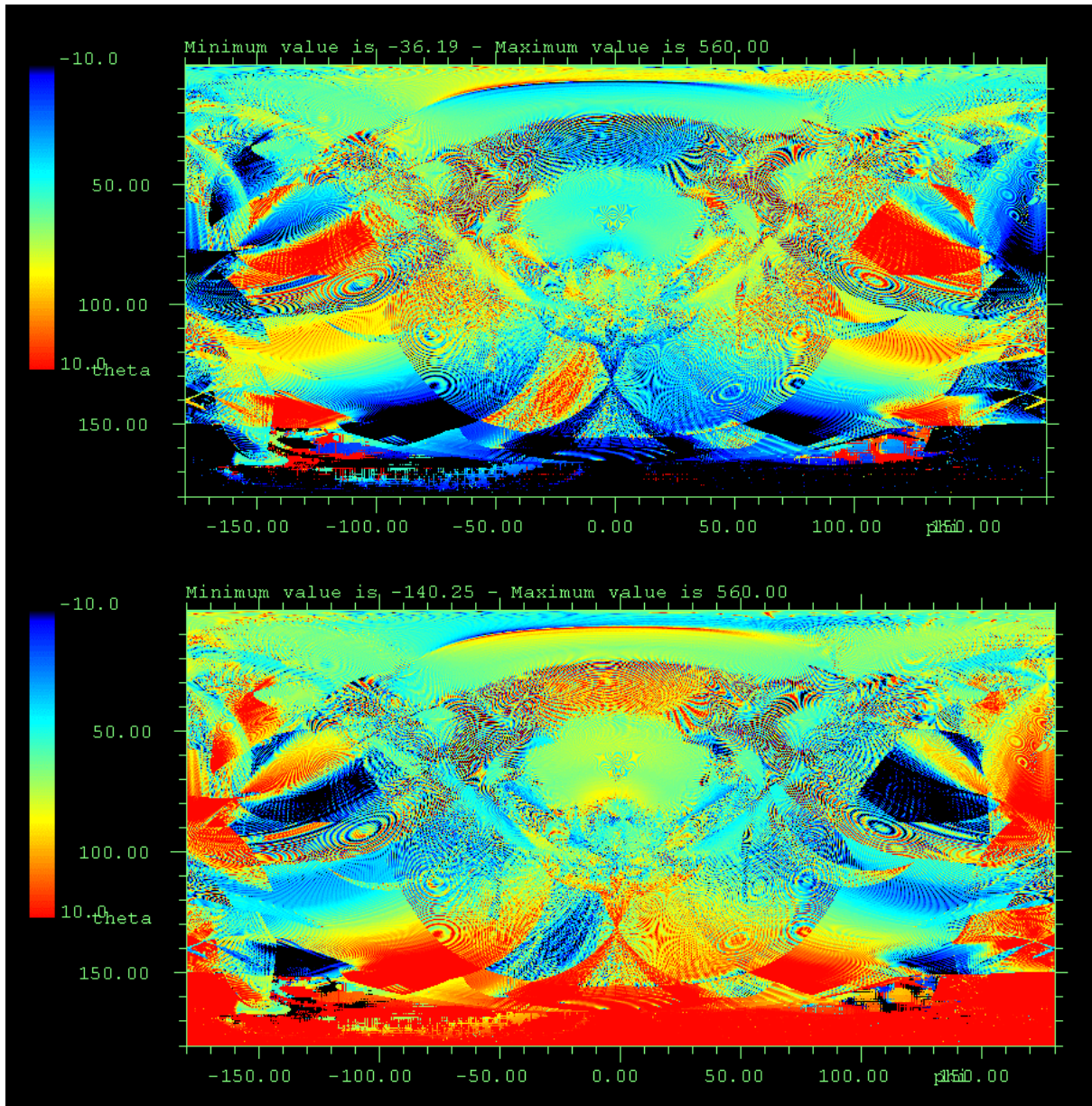


Figure 5.4-5 :local area modified by no more than 10 dB (red pixels to be disregarded).



### 5.5 353 GHz Pattern analysis(4pi-ext baf-inst feed)

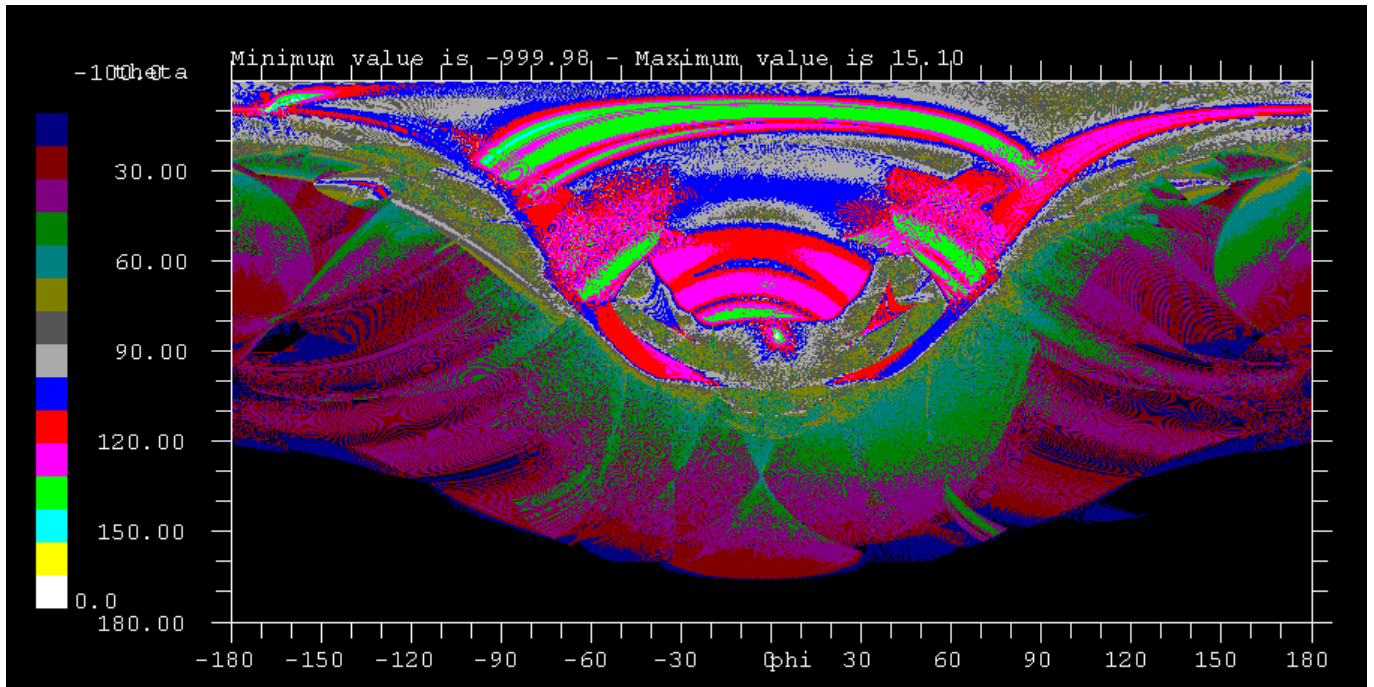


Figure 5.5-1 : 4PI diagram , phi : -180°, 180° / theta : 0,+180° / levels in directivity displayed from -100 dBi to +0 dBi (local major/minor component)

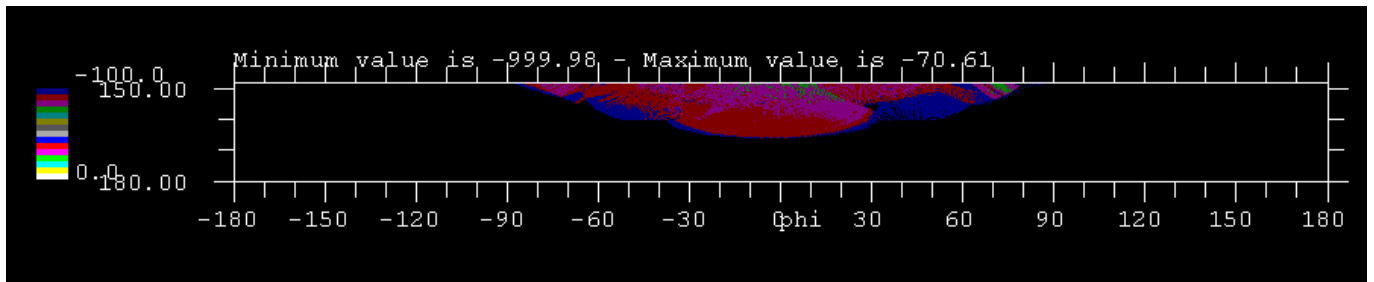


Figure 5.5-2 : Moon area phi : -180°, 180° / theta : +148°, +180° / levels in directivity displayed from -100 dBi to -0 dBi

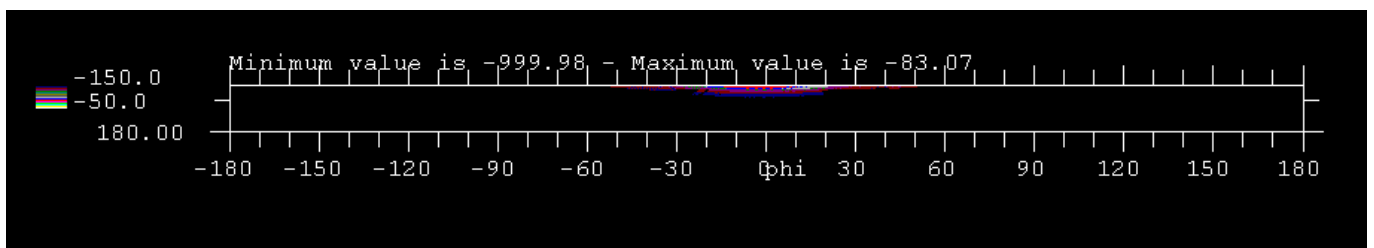


Figure 5.5-3 : Earth area phi : -180°, 180° / theta : +165°, +180° / levels in directivity displayed from -150 dBi to -50dBi (local major/minor component)

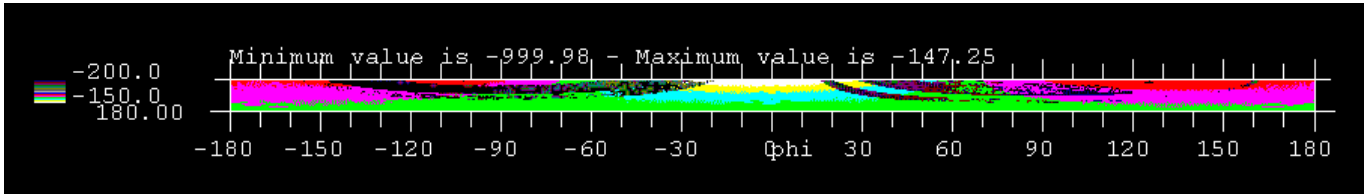


Figure 5.5-4 : Sun area phi : -180°, 180° / theta : +170°, +180° / levels in directivity displayed from -150 dBi to -50dBi (local major/minor component)



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## 6. FAR OUT SIDE LOBE PERFORMANCE SYNTHESIS.

### 6.1 Performance toward Earth Sun and Moon of the Planck Spacecraft with perfect reflector surfaces

The following table shows that a nice margin is obtained for the rejection toward the Earth Sun and Moon for the Planck spacecraft equipped with ideal ellipsoidal reflector with no dust and no moon illumination of the primary.

30 GHz	Rejection (dB)	Rejection (dB)
	with baffle extension & instrument feed models (polarization 1)	with baffle extension & instrument feed models (polarization 2)
Moon	-93	-83
Earth	-110	-107
Sun	-155	-147

100 GHz	Rejection (dB)	Rejection (dB)
	with baffle extension & instrument feed models polarization 1	with baffle extension & instrument feed models polarization 2
Moon	-116	-107
Earth	-141	-128
Sun	-198	-187

353 GHz	Rejection (dB)
	with baffle extension & instrument feed models
Moon	-139
Earth	-152
Sun	-216

857 GHz	Rejection (dB)	Rejection (dB)
	with baffle extension & gaussian feed	with baffle extension & instrument feed models
Moon	-170	NA(*)
Earth	-187	Na(*)
Sun	-259	NA(*)

(\*) not applicable because multi moded computation of the horn not available

Table 6.1-1 : rejection performance synthesis.



## 6.2 Quilting or Grating lobe impact on the far out side lobe level.

The [RD 9] contains the analysis of the reflector quilting. The quilting is a regular distortion of the reflectors surfaces. This is in fact a regular array of spacing higher than the wavelength hence the grating lobe are recombined in the real angular domain of the pattern. The quilting on the secondary reflector is equivalent to an array as well as the quilting of the primary. Hence it can be found two arrays of grating lobe around each main lobe.

The grating lobes induced by the reflector quilting have no impact on the rejection performance. The only visible grating are the ones close to the main beam 4<sup>th</sup> order of grating. For greater order the grating lobes are merged among the natural side lobe level.



### 6.3 Impact of dust contamination on the far out side lobe level.

All the details of the dust contamination analysis is provided in [RD 15] and revisited also in [RD 16]

This section presents only the performance budget and details the margins.

The numerical model in [RD 15] is based upon the computation of the BRDF and the BRDF variation with the incident angle. The BRDF values have been computed using a given contamination level as well as a given dust composition (see [RD 15]).

No computation have been performed at 30 GHz as far as the effect is negligible. In addition RF test on the RFDM and RFQM (see [RD 10] ) have shown no impact on the measurement.

The following table presents the rejection performance synthesis with the specification and also with the goals. It can be seen that even with the very worst case conservative dust model, the rejection requirements are met. Anyhow the goals toward the sun are not always met. Now the revisited model shows positive margins for all requirements (spec and goals). The measurement on the RFQM allow to obtain the minimum measurable signal in the rejection area at 320 and 100 GHz. As far as the levels measured in the CATR are lower than the modified level with the nominal dust, it is then possible to say that the first dust model described in [RD 15] is too pessimistic and can be disregarded for any further analysis. It is also possible to say that the revisited dust model is conservative .

For the contamination level of the reflector taking into account the contamination value of 225 ppm per day, for the polarization 1 campaign the reflectors had a level of  $225 \times 16 = 4000$  ppm and of 13000 ppm for the second polarization campaign. So the dust numerical model has been used with 5000 ppm and the minimum very low level signal have been measured at 320 GHz with the worst level of contamination. This means that the dust model is pessimistic even with best case input parameter. As a conclusion the dust contamination numerical model can be disregarded.

Spec (dB)	Margin worst case model of (RD 15) /spec (dB)	Margin with the revisited model (RD 16) / goals (dB)
-78	31	23
-85	26	28
-98	17	44
Goal (dB)	Margin worst case model of (RD 15) / Goal (dB)	Margin with the revisited model (RD 16) / Goal (dB)
-95	13	6
-109	1	4
-122	-7	20

Table 6.3-1 : margin @857 GHz wrt the requirements and the goals.

Spec (dB)	Margins worst case model of (RD 15) /spec (dB)	Margins with the revisited model (RD 16) / goals (dB)	Margins measured on the RFQM (see [RD 10]) (Nota constant level limited by the dynamic measured at -115 dB /max)
-72	31	31	43
-79	20	36	36
-92	5	48	23
Goal (dB)	Margins / Goal (dB)	Margins with the revisited model (RD 16) / Goal (dB)	
-81	22	22	34
-95	4	20	20
-108	-10	32	7

Table 6.3-2 : margin @353 GHz wrt the requirements and the goals.



Spec (dB)	Margins worst case model of (RD 15) /spec (dB)	Margins with the revisited model (RD 16) / goals (dB)	Margins measured on the RFQM (see [RD 10]) (Nota constant level limited by the dynamic measured at -110 dB /max)
-72	10	14	38
-79	17	19	31
-92	9	34	18
Goal (dB)	Margins / Goal (dB)	Margins with the revisited model (RD 16) / Goal (dB)	
-81	1	5	29
-95	1	3	15
-108	-7	18	2

Table 6.3-3 : margin @100 GHz wrt the requirements and the goals.





## 6.4 Final performance rejection toward Earth Sun and Moon.

The following table synthesizes all contributors to the rejection modification. The nominal performance is the one of the Planck spacecraft with ideal reflector, the baffle extension and the computed feed model. This nominal performance is degraded by different contributor. In fact the only contributor of importance is the dust contamination at the highest frequency. The far out side lobe are then dominated by the dust effect. In the following table the total rejection is obtained as the maximum of the different rejection computed alone (ie total rejection = max (rejection with no dust , rejection from dust model). As a conclusion, positive margin are obtained at all frequencies wrt the requirements and goals.

## 30 GHz

	Rejection with no dust (dB)	Rejection from dust model	Rejection from grating lobes	Total rejection (dB)	Rejection requirement (dB)		Margin / requirement (dB)
Moon	-83	NA	NA	-83	-71		12
Earth	-107	NA	NA	-107	-78		29
Sun	-147	NA	NA	-147	-91		56

## 100 GHz

	Rejection with no dust (dB)	Rejection from dust model	Rejection from grating lobes	Total rejection (dB)	Rejection requirement (dB)	Rejection goal (dB)	Margin / requirement (dB)	Margin / goal (dB)
Moon	-107	-107	NA	-107	-71.5	-73	36	34
Earth	-128	-110	NA	-110	-78.5	-86	32	24
Sun	-187	-126	NA	-126	-91.5	-99	35	27

## 353 GHz

	Rejection with no dust (dB)	Rejection from dust model	Rejection from grating lobes	Total rejection (dB)	Rejection requirement (dB)	Rejection goal (dB)	Margin / requirement (dB)	Margin / goal (dB)
Moon	-139	-115	NA	-115	-72	-81	43	34
Earth	-152	-115	NA	-115	-79	-95	36	20
Sun	-216	-140	NA	-140	-92	-108	48	32

## 857 GHz

	Rejection with no dust (dB) Gaussian feed	Rejection from dust model	Rejection from grating lobes	Total rejection (dB)	Rejection requirement (dB)	Rejection goal (dB)	Margin / requirement (dB)	Margin / goal (dB)
Moon	-170	-101	NA	-101	-78	-95	23	6
Earth	-187	-113	NA	-113	-85	-109	28	4
Sun	-259	-142	NA	-142	-98	-122	44	20

Table 6.4-1 : Final performance rejection comparison wrt to the requirements and the goals.



## 7. MAIN LOBE PERFORMANCE ANALYSIS

### 7.1 Introduction

The purpose of this chapter is to establish the Planck Telescope RF Performance analysis. This section is an update of the Planck CDR RF Analysis.

- In the first part the hypotheses and the input data used to perform the analysis are reviewed: telescope geometry, feed definitions, orientation and positions.
- In the second part, the hypotheses, the method of analysis applied for main lobes simulation is presented as well as discussions on convergence and on the performance estimation.
- The third part gives the description of the RF budget, which is based on two types of data: deterministic and random. The origin of these data are recalled as well as, in some cases, the process applied to convert them in a usable form for GRASP8.
- The fourth part gives the final budget of the telescope.

## 7.2 Hypotheses and data used for RF Budget

### 7.2.1 Planck telescope geometry

The geometry of the telescope is shown in Figure 7.2-1. The telescope is composed of two reflectors in a gregorian off-axis configuration. M1 and M2 are located at the vertex of the ellipsoids and the RDP is the coordinate system of the FPU (Focal Plane Unit). Two additional coordinate systems OM1C and OM2C are introduced and are the coordinates systems associated with the mechanical interface of the reflectors and are defined in [RD11].

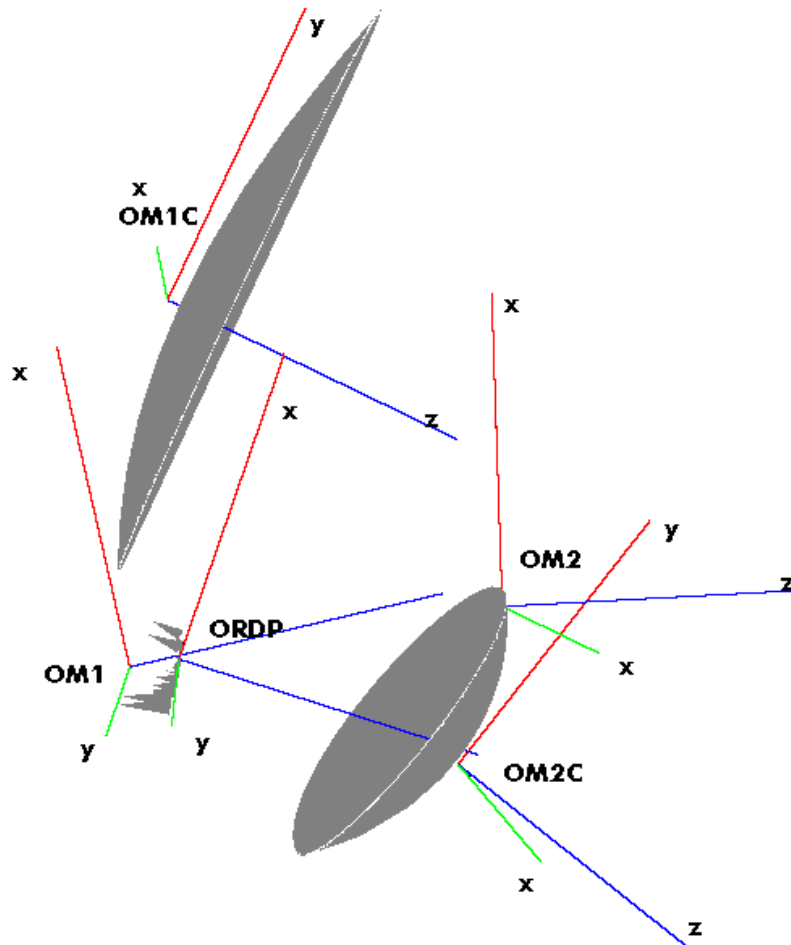


Figure 7.2-1 Planck Telescope coordinate systems



## 7.2.2 Horns definition

The FPU (focal plane unit) is composed of two type of horns: LFI (low frequency instruments) and HFI (High frequency instruments). The HFI horns are placed at the center of the FPU and are surrounded by the LFI horns.

The operating frequency of the horns is defined by their center frequency. LFI includes three types of horns defined by their center frequencies: 30, 44 and 70 and HFI includes six types defined by their center frequencies: 100, 143, 217, 353, 545 and 857 GHz.

For the analysis of the Planck performance, the feed model used is a gaussian beam defined by a far-field taper (apodization) as given in Table 7.2-1 :

Frequency	Angle 30 dB from Peak (°)
30 GHz (LFI-30-27 to LFI-30-28)	23.6
44 GHz (LFI-44-23 to LFI-44-26)	23.6
70 GHz (LFI-70-18 to LFI-70-22)	21.9
100 GHz (HFI-100-1 to HFI_100_4)	26.8
143 GHz (HFI-143-1 to HFI_100_8)	23.7
217 GHz (HFI-217-1 to HFI_100_8)	21.8
353 GHz (HFI-353-1 to HFI_353_8)	19.4
545 GHz (HFI-545-1 to HFI_545_4)	19.4
857 GHz (HFI-857-1 to HFI_857_4)	19.4

Table 7.2-1 Taper of Horns

The feed radiation patterns are defined according to Table 7.2-1 in Grasp8 model.



## 7.2.3 Horns position in the ORDP plane

### 7.2.3.1 LFI Horns

The horns positions used for the analysis are the ones given (see Table 7.2-2 ). 11 detectors are defined by their working center frequencies between 30 GHz to 70 GHz. The positions are given in the ORDP coordinate system ( $X_{rdp}$ ,  $Y_{rdp}$ ,  $Z_{rdp}$ ) and their orientation by the cosine directors.

Detectors N#	Xrdp mm	Yrdp mm	Zrdp mm	Ux	Uy	Uz	Ux	Uy	Uz	Ux	Uy	Uz	frequency GHz
LFI_70_18	-76.38	-69.37	14.54	0.936379	0.299574	-0.182891	-0.320318	0.942398	-0.096346	0.143494	0.1488	0.978401	70
LFI_70_19	-92.41	-43.29	18.66	0.922853	0.32965	-0.19918	-0.342171	0.939123	-0.031084	0.176808	0.096839	0.97947	70
LFI_70_20	-101.86	-17.69	20.86	0.912768	0.359322	-0.194275	-0.359717	0.932423	0.034501	0.193544	0.038393	0.98034	70
LFI_70_21	-101.86	17.69	20.86	0.912768	-0.359322	-0.194275	0.359717	0.932423	-0.034501	0.193544	-0.038393	0.98034	70
LFI_70_22	-92.41	43.29	18.66	0.922853	-0.32965	-0.19918	0.342171	0.939123	0.031084	0.176808	-0.096839	0.97947	70
LFI_70_23	-76.38	69.37	14.54	0.936379	-0.299574	-0.182891	0.320318	0.942398	0.096346	0.143494	-0.1488	0.978401	70
LFI_44_24	-138.41	0.	21.29	0.9666	0.0	-0.256289	0.	1.	0.	0.256289	0.	0.9666	44
LFI_44_25	55.32	133.27	-17.90	-0.262536	-0.923175	-0.280755	0.958343	-0.283384	0.035667	-0.112488	-0.259696	0.959117	44
LFI_44_26	55.32	-133.27	-17.90	-0.262536	0.923175	-0.280755	-0.958343	-0.283384	-0.035667	-0.112488	0.259696	0.959117	44
LFI_30_27	-136.95	54.94	18.60	0.910601	-0.314901	-0.267661	0.331426	0.943315	0.017731	0.246905	-0.104856	0.96335	30
LFI_30_28	-136.95	-54.94	18.60	0.910601	0.314901	-0.267661	-0.331426	0.943315	-0.017731	0.246905	0.104856	0.96335	30

Table 7.2-2 LFI Horns positions and orientations

The overview of the LFI horns is shown in the Figure 7.2-2.

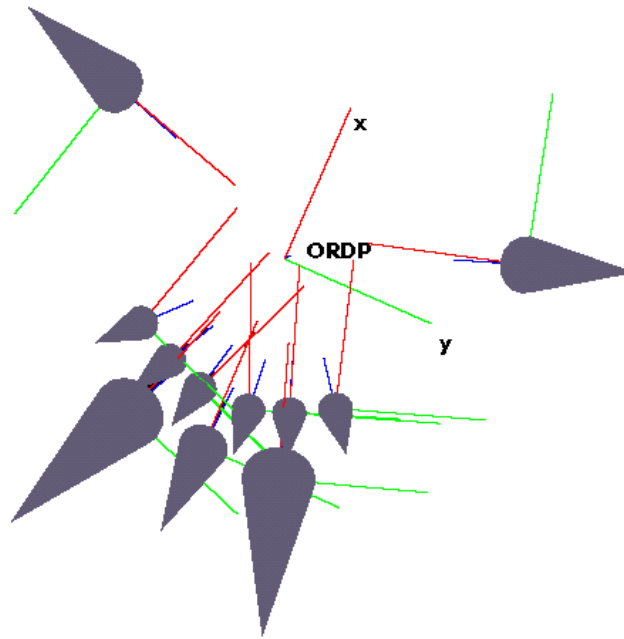


Figure 7.2-2: LFI horns in the ORDP plane



### 7.2.3.2 HFI Horns

The positions of the horns are given in the ORDP coordinate system ( $X_{rdp}$ ,  $Y_{rdp}$ ,  $Z_{rdp}$ ) (see Table 7.2-3) .

Detectors N#	Xrdp mm	Yrdp mm	Zrdp mm	Ux	Uy	Uz	Ux	Uy	Uz	Ux	Uy	Uz	frequency GHz
HFI_100_1	-47.57	-32.966	14.847	0.995407	-0.003320	-0.095675	-0.003320	0.997600	-0.069161	0.095675	0.069161	0.993007	100
HFI_100_2	-55.114	-10.622	16.831	0.993785	-0.001245	-0.111314	-0.001245	0.999750	-0.022304	0.111314	0.022304	0.993535	100
HFI_100_3	-55.114	10.622	16.831	0.993785	0.001245	-0.111314	0.001245	0.999750	0.022304	0.111314	-0.022304	0.993535	100
HFI_100_4	-47.57	32.966	14.847	0.995407	0.003320	-0.095675	0.003320	0.997600	0.069161	0.095675	-0.069161	0.993007	100
HFI_143_1	33.184	-39.106	-1.28	0.997576	0.002875	0.069528	0.002875	0.996591	-0.082449	-0.069528	0.082449	0.994167	143
HFI_143_2	35.142	-16.019	-0.572	0.997306	0.001247	0.073346	0.001247	0.999423	-0.033937	-0.073346	0.033937	0.996729	143
HFI_143_3	34.424	16.013	-0.39	0.997415	-0.001221	0.071848	-0.001221	0.999423	0.033940	-0.071848	-0.033940	0.996838	143
HFI_143_4	33.912	41.141	-1.613	0.997466	-0.003090	0.071078	-0.003090	0.996232	0.086673	-0.071078	-0.086673	0.993698	143
HFI_143_5	48.96	-32.843	-4.919	0.994759	0.003545	0.102182	0.003545	0.997603	-0.069112	-0.102182	0.069112	0.992362	143
HFI_143_6	50.593	-8.581	-4.455	0.994421	0.000958	0.105483	0.000958	0.999835	-0.018119	-0.105483	0.018119	0.994256	143
HFI_143_7	49.882	8.578	-4.263	0.994576	-0.000945	0.104011	-0.000945	0.999835	0.018122	-0.104011	-0.018122	0.994411	143
HFI_143_8	49.672	32.856	-5.108	0.994608	-0.003596	0.103642	-0.003596	0.997602	0.069120	-0.103642	-0.069120	0.992210	143
HFI_217_1	-31.18	-27.749	12.776	0.997992	-0.001858	-0.063313	-0.001858	0.998281	-0.058579	0.063313	0.058579	0.996273	217
HFI_217_2	-29.527	-8.754	13.236	0.998168	-0.000561	-0.060502	-0.000561	0.999828	-0.018533	0.060502	0.018533	0.997996	217
HFI_217_3	-30.307	8.752	13.362	0.998071	0.000576	-0.062081	0.000576	0.999828	0.018535	0.062081	-0.018535	0.997899	217
HFI_217_4	-30.399	27.756	12.651	0.998090	0.001813	-0.061746	0.001813	0.998280	0.058603	0.061746	-0.058603	0.996370	217
HFI_217_5	-16.174	-34.288	9.791	0.999467	-0.001184	-0.032614	-0.001184	0.997369	-0.072487	0.032614	0.072487	0.996836	217
HFI_217_6	-14.291	-15.164	10.422	0.999569	-0.000473	-0.029368	-0.000473	0.999481	-0.032197	0.029368	0.032197	0.999050	217
HFI_217_7	-15.051	15.16	10.563	0.999522	0.000498	-0.030916	0.000498	0.999482	0.032174	0.030916	-0.032174	0.999004	217
HFI_217_8	-15.412	34.298	9.651	0.999517	0.001128	-0.031062	0.001128	0.997367	0.072508	0.031062	-0.072508	0.996884	217
HFI_353_1	-3.268	-58.369	5.117	0.999987	-0.000308	-0.005009	-0.000308	0.992474	-0.122458	0.005009	0.122458	0.992461	353
HFI_353_2	-0.512	-39.964	6.325	1.000000	-0.000011	-0.000262	-0.000011	0.996427	-0.084458	0.000262	0.084458	0.996427	353
HFI_353_3	-0.073	-23.141	7.308	1.000000	0.000003	0.000122	0.000003	0.998792	-0.049138	-0.000122	0.049138	0.998792	353
HFI_353_4	1.231	-5.905	7.552	0.999997	0.000016	0.002562	0.000016	0.999921	-0.012547	-0.002562	0.012547	0.999918	353
HFI_353_5	0.409	10.332	7.649	1.000000	-0.000010	0.000908	-0.000010	0.999758	0.021980	-0.000908	-0.021980	0.999758	353
HFI_353_6	0.451	27.097	6.996	0.999999	-0.000038	0.001309	-0.000038	0.998347	0.057477	-0.001309	-0.057477	0.998346	353
HFI_353_7	-1.536	42.928	6.29	0.999997	0.000101	-0.002234	0.000101	0.995885	0.090631	0.002234	-0.090631	0.995882	353
HFI_353_8	-2.513	58.387	4.964	0.999994	0.000212	-0.003456	0.000212	0.992469	0.122496	0.003456	-0.122496	0.992463	353
HFI_545_1	12.049	-58.768	1.867	0.999650	0.001635	0.026421	0.001635	0.992370	-0.123281	-0.026421	0.123281	0.992020	545
HFI_545_2	14.698	-40.242	3.022	0.999512	0.001329	0.031201	0.001329	0.996378	-0.085027	-0.031201	0.085027	0.995890	545
HFI_545_3	13.702	43.225	3.004	0.999572	-0.001337	0.029230	-0.001337	0.995828	0.091238	-0.029230	-0.091238	0.995400	545
HFI_545_4	12.784	58.788	1.703	0.999609	-0.001729	0.027922	-0.001729	0.992366	0.123312	-0.027922	-0.123312	0.991975	545
HFI_857_1	15.072	-23.799	3.974	0.999501	0.000798	0.031581	0.000798	0.998724	-0.050492	-0.031581	0.050492	0.998225	857
HFI_857_2	16.357	-6.442	4.207	0.999420	0.000233	0.034060	0.000233	0.999906	-0.013691	-0.034060	0.013691	0.999326	857
HFI_857_3	15.568	9.909	4.332	0.999474	-0.000342	0.032430	-0.000342	0.999778	0.021065	-0.032430	-0.021065	0.999252	857
HFI_857_4	15.617	27.287	3.672	0.999462	-0.000950	0.032788	-0.000950	0.998324	0.057862	-0.032788	-0.057862	0.997786	857

Table 7.2-3 Positions of HFI horns

The overview the HFI horns in the focal plane is shown in Figure 7.2-3 and Figure 7.2-4.



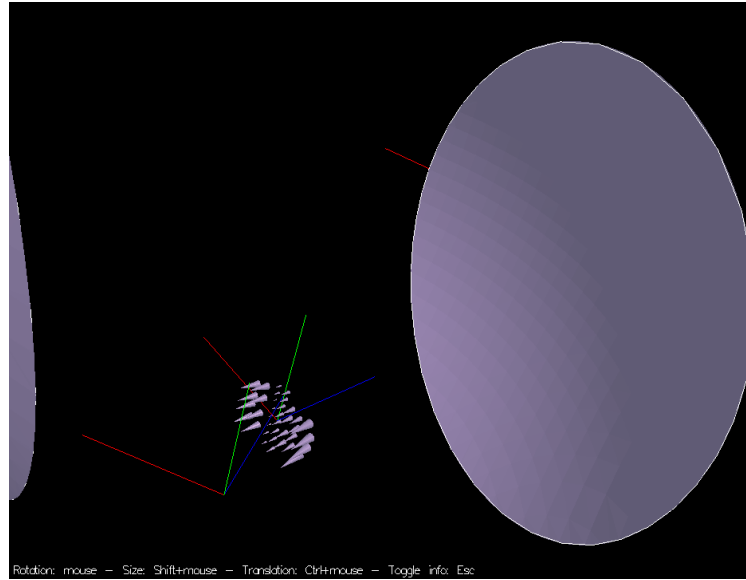


Figure 7.2-3: HFI horns in the ORDP plane

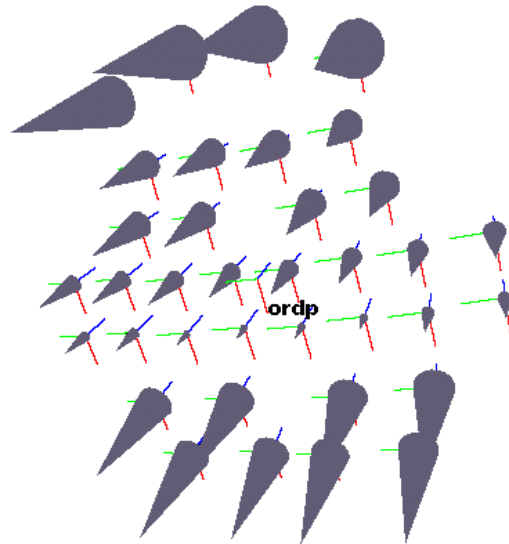


Figure 7.2-4 Detectors view in the focal Plane



## 7.3 Main lobes computation

### 7.3.1 Introduction

The telescope performance evaluation is defined in term of main lobe gain degradation. The gain degradation evaluation is based on different type of inputs (displacement of the reflector and feeds, distortion of the surface.). In order to achieve the computation with a given accuracy and in a reasonable computation time, the convergence parameters and the method of analysis must be optimized and adjusted. These last points are detailed in the following sections.

### 7.3.2 Requirements

The requirements for the Planck telescope performance are recalled in the followig table :

Frequency	Max reduction in gain
GHz	dB
30	0,5
44	0,5
70	0,5
100	0,5
143	0,5
217	1
353	1
545	1,4
857	2,5

Table 7.3-1 Telescope specification : Gain degradation

PTPE-035 The telescope shall achieve a Gain at the defined position of the detectors and operational conditions that do not reduce the theoretical value by more than see Table 7.3-1.



### 7.3.3 Quantification in terms of directivity degradation

#### Directivity degradation:

The horns are placed in the focal plane but not at the focus point. As a consequence, according to the usual definition of the cross-polarisation, the co-polarisation direction is given by the feed horn polarisation. Hence in order to obtain the diagram in co-polarisation and cross-polarisation, the coordinate system of the uv pattern of the telescope main lobe must be re-computed for each horn and each displacement. So as to avoid this additional computation, which could become heavy with regards to the number of detectors and displacements to analyse, the directivity degradation is computed through the power diagram.

The term  $E_x$  given by Grasp8 is normalized to a square root of power ( $P=|E|^2$ ).

Component 1:

$$|E_1| = \sqrt{E_{1r}^2 + E_{1i}^2}$$

Component 2:

$$|E_2| = \sqrt{E_{2r}^2 + E_{2i}^2}$$

Directivity in term of principal component

$$D_{dB} = 20 \log_{10} (\sqrt{|E_1|^2 + |E_2|^2})$$

### 7.3.4 Simulation Tool

For the computation of the RF performance, a method of simulation with a good accuracy must be chosen to reach enough sensitivity to evaluate the impact of small disturbances. More precisely, the computation will have to take into account small displacements (translations and rotations) and surface deformations of small magnitude (a few microns).



As long as small disturbances could have a great impact on directivity, it is necessary ensure the numerical convergence of the results. For instance, according to the Ruze formula, at 857 GHz few microns of surface error could have a large impact in directivity degradation:

delta rms	delta directivity (dB)
1	0,005
2	0,02
3	0,05
4	0,09
5	0,14
6	0,20
7	0,27

Table 7.3-2 Surface error and gain degradation by Ruze

Thus, the sensitivity in directivity that one must be able to reach would be less than 0.01 dB.

Two types of data have to be considered in the computation: Impact of BFE displacement and distortion (rotation, translation, conicity and radius variations) and surface errors on the reflectors.

#### 7.3.4.1 Main lobe and displacement computations

There are two ways to simulate the telescope performance: MGTD (multi-geometrical-theory of diffraction) and PO (physical optics) or a hybrid between the two methods. In the case of main lobe computation the use of PO is more accurate but time-consuming even if a pattern grid is reduced and centered on the main beam. In the purpose of determining the reflector surface discretisation parameters for physical optics, a convergence study on the directivity computation have been performed with an accuracy better than 0.01 dB.

Generally used for fast computation away from the main lobes, full MGTD method is not correct for main lobe computation because of caustic problem. Anyway, it is possible to use MGTD on the sub reflector and PO on the main reflector.

The advantage of doing this is to be faster than the full PO and this approach will gain in accuracy as long as the theory of geometrical diffraction is based on higher frequency approximation.



A preliminary comparison study is summarised in the Table 7.3-3 for LFI and HFI horns. The comparison between the two computations MGTD - PO (Reflection on the sub and PO on the main) and PO-PO is shown. The last column gives the difference in directivity in dB.

One can notice that at higher frequencies there is no difference in directivity (less than 0.006 dB up to 100 GHz). At lower frequencies the difference remains small, around 0.024 dB at 30 GHz, 0.022 dB at 44 GHz and 0.012 dB at 70 GHz). These results are in line with the fact that GTD method is accurate at high frequencies. Therefore, in the case of perfect reflectors, MGTD with PO could be used for the computation of the impact of displacement at higher frequencies.

#### 7.3.4.2 Impact of deformation on surface

When the surface deformation has to be taken into account (high frequency distortion), full Physical Optics method (PO) must be chosen for computation, as it is the only way to handle the distortion on the surface. This means that the surface must be represented in one of the following formats:

- 1) Cloud of points  $(x, y, z)$  representative of the reflector surface
- 2) Equation of the conic (BFE) surface + distortion expanded in term of Zernike polynomials
- 3) Equation of conic (BFE) surface + distortion in term z-axis deviation from the perfect surface  $(x, y, \Delta z)$

In the first format, the grid must be dense enough to avoid any additional grating lobes. These latter could occur if the magnitude of the distortion is important. Moreover, the grid must be close to a regular grid to minimize interpolating errors. Obviously, a compromise must be found with regards to the accuracy and computation time.

If the second format is used, one must ensure higher order Zernike polynomials in the expansion so as to be representative of high frequency distortion. This method could not be applied for deformations, which have a high spatial periodicity as quilting and random surface errors.

If the third format is used, the distortion must be expanded in Z-axis deviation (could be a constraint when measurement gives radial distortion). However, the advantage of this format is to apply interpolation only on the distortion file instead of on the complete surface of the reflector as when the first format is used. Therefore, this last format will be used for simulating the high frequency distortion.



detector	GTD-PO	PO-PO	delta G
LFI_70_18	57,2117	57,2209	-0,0092
LFI_70_19	57,3694	57,3820	-0,0126
LFI_70_20	57,4513	57,4629	-0,0117
LFI_70_21	57,4513	57,4629	-0,0117
LFI_70_22	57,3694	57,3820	-0,0126
LFI_70_23	57,2117	57,2205	-0,0088
LFI_44_24	54,2521	54,2739	-0,0217
LFI_44_25	52,4603	52,4583	0,0020
LFI_44_26	52,4603	52,4583	0,0020
LFI_30_27	50,9666	50,9898	-0,0232
LFI_30_28	50,9666	50,9898	-0,0232
HFI_100_1	61,5997	61,6052	-0,0056
HFI_100_2	61,6568	61,6627	-0,0059
HFI_100_3	61,6568	61,6627	-0,0059
HFI_100_4	61,5997	61,6052	-0,0056
HFI_143_1	63,3077	63,3124	-0,0046
HFI_143_2	63,3577	63,3624	-0,0047
HFI_143_3	63,3654	63,3695	-0,0041
HFI_143_4	63,2852	63,2876	-0,0024
HFI_143_5	63,1215	63,1234	-0,0019
HFI_143_6	63,1942	63,1973	-0,0031
HFI_143_7	63,2046	63,2087	-0,0040
HFI_143_8	63,1083	63,1104	-0,0021
HFI_217_1	66,7002	66,7007	-0,0005
HFI_217_2	66,7143	66,7157	-0,0014
HFI_217_3	66,7186	66,7210	-0,0024
HFI_217_4	66,6984	66,6997	-0,0013
HFI_217_5	66,6210	66,6231	-0,0020
HFI_217_6	66,6246	66,6260	-0,0014
HFI_217_7	66,6289	66,6295	-0,0006
HFI_217_8	66,6173	66,6190	-0,0018
HFI_353_1	69,2531	69,2474	0,0057
HFI_353_2	69,6751	69,6708	0,0043
HFI_353_3	69,7500	69,7470	0,0031
HFI_353_4	69,7265	69,7246	0,0019
HFI_353_5	69,7339	69,7341	-0,0002
HFI_353_6	69,7432	69,7409	0,0023
HFI_353_7	69,6462	69,6429	0,0034
HFI_353_8	69,2464	69,2408	0,0055
HFI_545_1	71,8578	71,8516	0,0062
HFI_545_2	72,9061	72,9011	0,0050
HFI_545_3	72,8181	72,8126	0,0055
HFI_545_4	71,8342	71,8288	0,0053
HFI_857_1	76,6257	76,6232	0,0025
HFI_857_2	76,6672	76,6642	0,0031
HFI_857_3	76,6807	76,6769	0,0038
HFI_857_4	76,5524	76,5492	0,0032

Table 7.3-3 Convergence between PO-PO and MGTD (reflection)-PO

### 7.3.4.3 Pattern windowing

A remark concerning the window size used for the pattern computation. The windows are optimized in order to reduce the computation time. The typical window is defined so as to cover the  $-3$  dBmax with a  $51 \times 51$  points grid (see Figure 7.3-1).

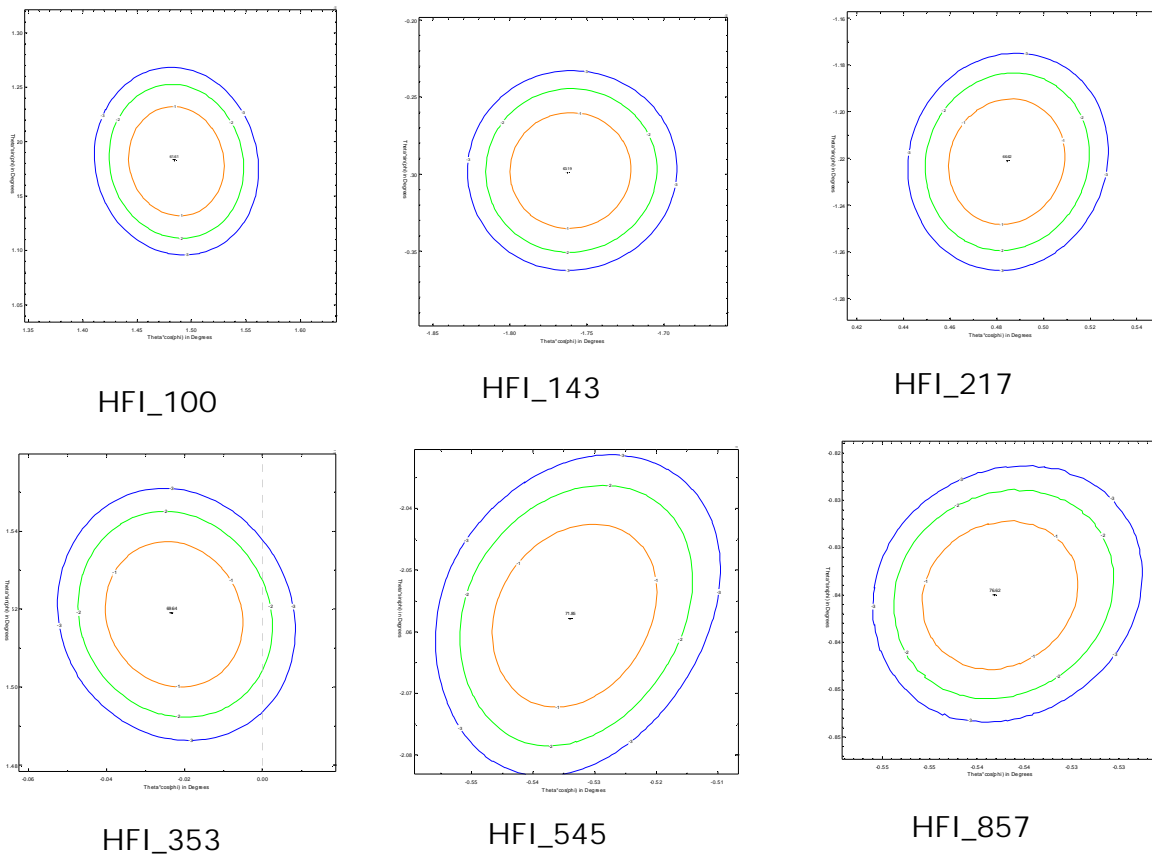


Figure 7.3-1 Patterns HFI examples.





### 7.3.5 LFI radiation pattern

The radiation patterns for LFI horns are shown in Figure 7.3-2. The contour levels correspond to -3 dB below the maximum.

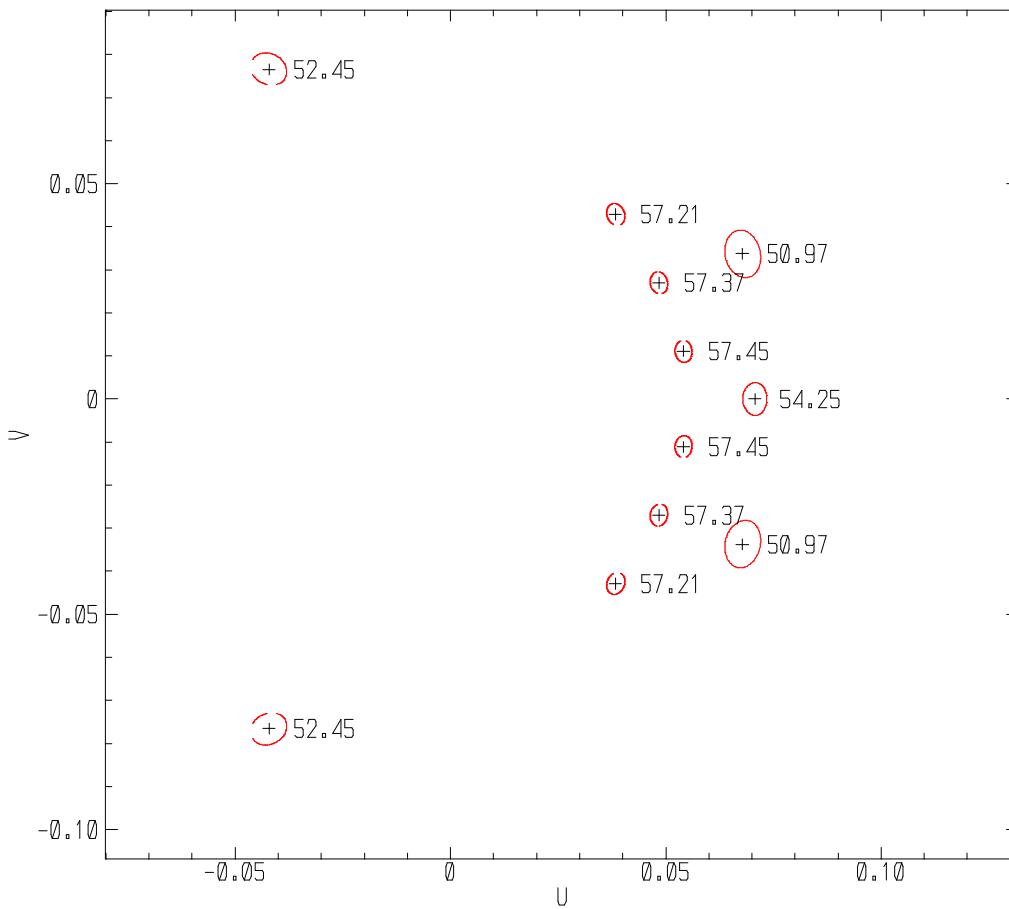


Figure 7.3-2: Radiation pattern of the telescope for LFI horns



### 7.3.6 HFI radiation pattern

In the same way the radiation patterns for HFI horns are plotted in Figure 7.3-3. The contour levels correspond to  $-3$  dB and  $-6$  dB.

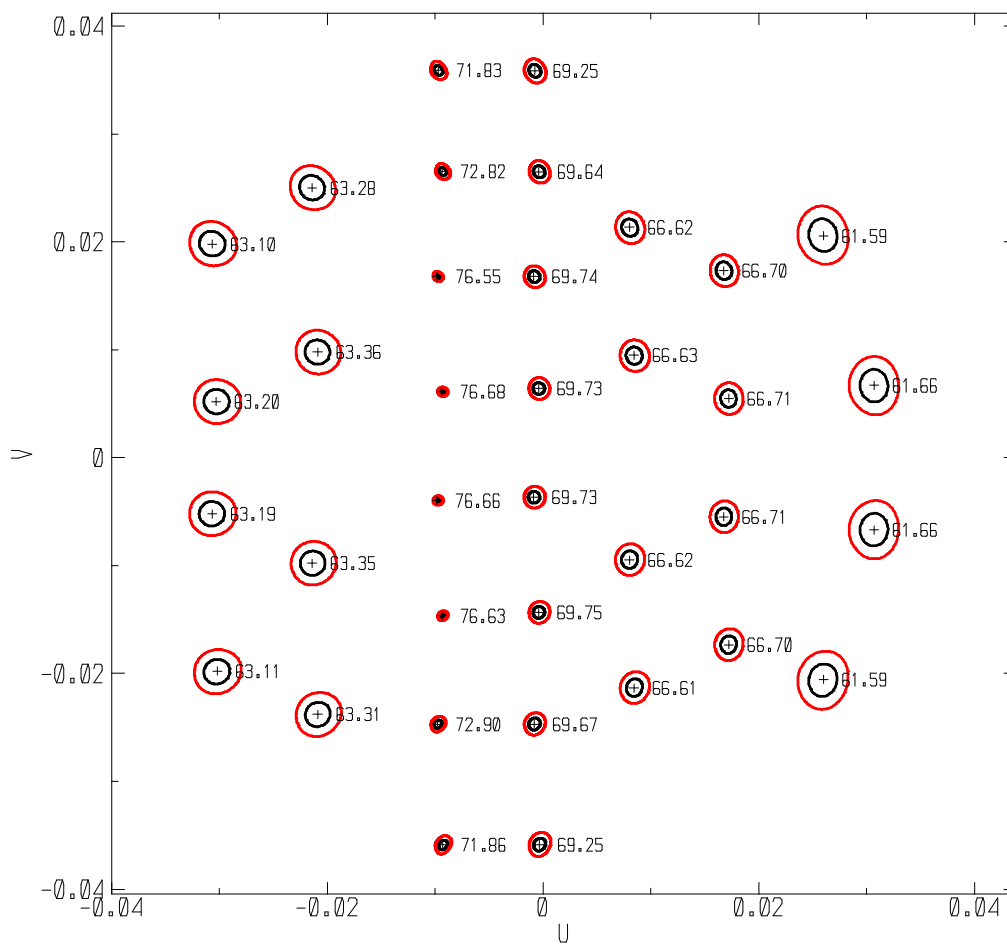


Figure 7.3-3. Radiation pattern of the telescope for HFI horns

## 7.4 Contributors analysis

This part presents the identification of the contributors and their conversion in terms of RF performance degradations. For this purpose, it is necessary to decompose each contributor and to define the best way to insert them in the numerical RF model.

The major part of the inputs for the budget comes from [RD20], [RD21] and [RD22] where the mechanical impact of the contributors have been quantified by simulations (under several load cases of random contributors), surface measurements (videogrammetry, interferometry) and other parts from a specific analysis or allocations.

### 7.4.1 Contributors identification

Two types of contributors could be identified : deterministic (signed) and statistic (not signed) contributors (see Figure 7.4-1).

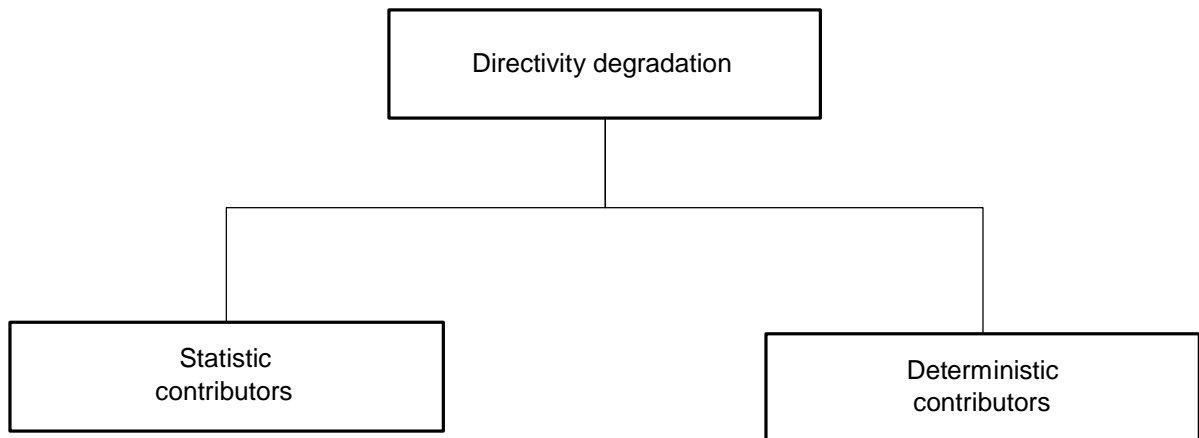


Figure 7.4-1 Contributors identification

For statistic contributors the degradation of the performance will be obtained by a quadratic summation of each degradation and for the deterministic contributors by a summation.

Each contributor is divided into several sub-contributors in order to identify precisely the origin (see [RD23]).

### 7.4.2 Deterministic contributor

The deterministic case at operational is composed of two parts :

- a "deterministic load case"
- others deterministic estimated cases.

The "deterministic load case" (boxes 1, 2, 3, 4, 5 in figure 7.4-2) is built through a numerical model which includes a major part of the contributors.

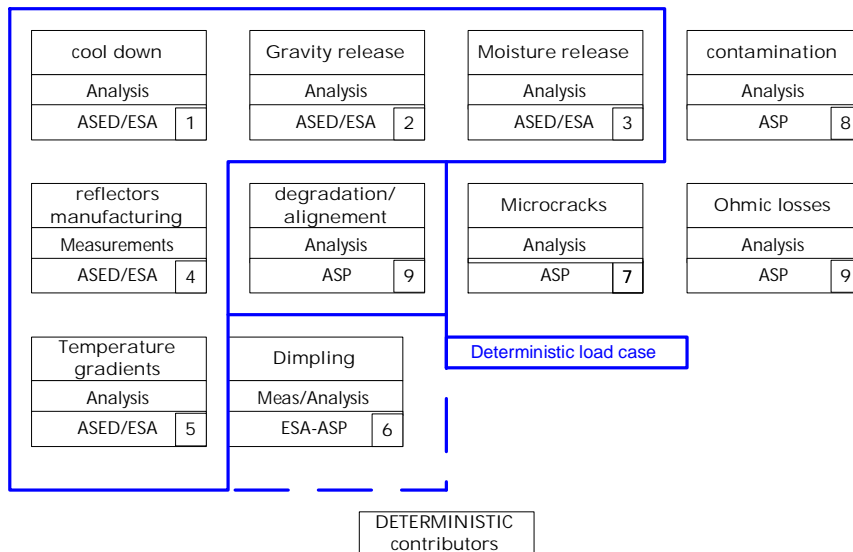


Figure 7.4-2 deterministic contributors

The numerical model must be representative of the telescope at operational. The model is built with different data from measurements, analysis (extrapolation at operational) and optimisation results. The methodology used to establish the geometrical configuration at operational is detailed in [RD6]-[RD7] [RD8] and is recalled in the following steps:

- 1) Measurement of BFE by videogrammetry (ESA) of reflector surface shape at 100 k and extrapolation to 55 k by analysis.
- 2) Optimisation of the best geometrical configuration according to these two BFE. (Alcatel)
- 3) Alignment measurement, deviation measured and extrapolated at operational from configuration defined in 2)
- 4) Measurements of sub reflector surface shape (high frequency distortion) by interferometry
- 5) Measurement of RFQM Mould measurement analysis for the main reflector (ESA/ASED) (nota : this set of data has not been updated for the QR analysis).
- 6) Additional contributor at operational



The numerical model is constructed from step 1 to 6 . This model is used to estimate the performance degradation for the deterministic load case. This degradation (calculated with the deterministic load case) must be added to the three others contributors appearing outside the blue contour (see Figure 7.4-2). The dashed contour of the "dimpling contributor" means that the "dimpling or quilting" contributor has only been considered for the sub reflector (measured and estimated at 55 K) and is included in the deterministic load case. An allocation will be taken for the main reflector in the final budget.

#### 7.4.2.1 Input for deterministic load case

The deterministic load case is obtained by a summation of sub level contributors and is defined by one set of parameters (BFE distortion+ HF distortion + displacements and rotation).

The deterministic load case is defined in following the data format:

- 1) BFE defined by  $\Delta R$  and  $\Delta K$  from the initial conics defining the main and the sub reflectors.
- 2) Position of the BFE vertex in OM1 and OM2 ( $T_x, T_y, T_z, R_x, R_y$ )
- 3) Defocus of the ORDIP plane ( $T_x, T_y, T_z$ )
- 4) Residual distortion (also mentioned as HF -high frequency distortion)

The parameters refer to deviation, displacement and rotation from the theoretical model.



### 7.4.2.2 FM Reflector BFE shape

The shape of the reflectors have been measured and interpolated to 55 k (operational temperature) ([RD21]).

The measurements have been performed by videogrammetry. The clouds of points has been best fitted by a conic and allowed to calculate the BFE of each surface (main and sub reflectors). The values obtained for conicity and radius of curvature defining the BFE are given in Figure 7.4-1. The parameters, interfoci and vertex-focus distance defining the conic is given in Table 7.4-2. The optical configuration can be reconstructed by positioning the real surface defined by the last parameters.

mm		primary reflector			secondary reflector		
		measured	theory	delta	measured	theory	delta
radius of curvature (mm)	R	1439,115	1440	-0,885	643,78	643,972	-0,192
conicity	K	-0,86738	-0,869417	0,002037	-0,21514	-0,215424	0,000284

Table 7.4-1 BFE measured by videogrammetry

Primary reflector (mm)								
a	a		b	b		c	c	
measured	theory	delta	measured	theory	delta	measured	theory	delta
10851,4176	11027,4691	-176,0515	3951,7639	3984,9160	-33,1521	10106,2766	10282,2916	-176,0150
vertex-focus distance						interfoci distance		
a-c	a-c					2*c	2*c	
745,1410	745,1776	-0,0365				20212,5531	20564,5831	-352,0300
secondary reflector (mm)								
a	a		b	b		c	c	
measured	theory	delta	measured	theory	delta	measured	theory	delta
820,2482	820,7898	-0,5416	726,6769	727,0252	-0,3483	380,4573	380,9597	-0,5024
vertex-focus distance						interfoci distance		
a-c	a-c	delta				2*c	2*c	delta
439,7909	439,8302	-0,0392				760,9145	761,9194	-1,0048

Table 7.4-2 Deviation of the actual surface/ theory

The comparison with the theoretical values shows significant discrepancies. The reflector cannot be placed at the theoretical location without degrading the performance. Another optical configuration has been defined.



### 7.4.2.3 Realignment

As previously mentioned, the surfaces of the reflectors present significant deviations with the theoretical ones. According to the alignment method proposed in (RD7), the positions of the reflectors and of the FPU have been optimised in order to improve the image quality by CODE V. The values obtained which ameliorate the optical arrangement are given in Table 7.4-3.

Optimisation results by Code V	Tx	Ty	Tz	Rx	Ry	Rz	coordinate system
	mm	mm	mm	deg	deg	deg	
Primary reflector	-0,64	0	0,015	0	0,0493	0	OM1
secondary reflector	0,25	0	-0,04	0	0,0324	0	OM2
FPU	0	0	2,82	0	0	0	ORDP

Table 7.4-3 Optimisation results

### 7.4.2.4 Reflector high frequency surface distortion

#### 7.4.2.4.1 Main reflector

For the main reflector, the residual surface distortion is given in the format of a cloud of point  $x, y, \Delta z$  where  $\Delta z$  is the deviation of the surface from the ideal reflector in the z-direction. This surface distortion is plotted in

The distortions are obtained from analysis (Contraves simulation and QM mould measurements). In fact this surface has not been updated since the CDR, the measurement of this surface by interferometry is not available yet. Therefore, a hypothesis has been taken to perform the computation: the order of magnitude of the distortions remains unchanged and their impacts on gain degradation remain representative of the flight model (see map in figure 7.4-3).

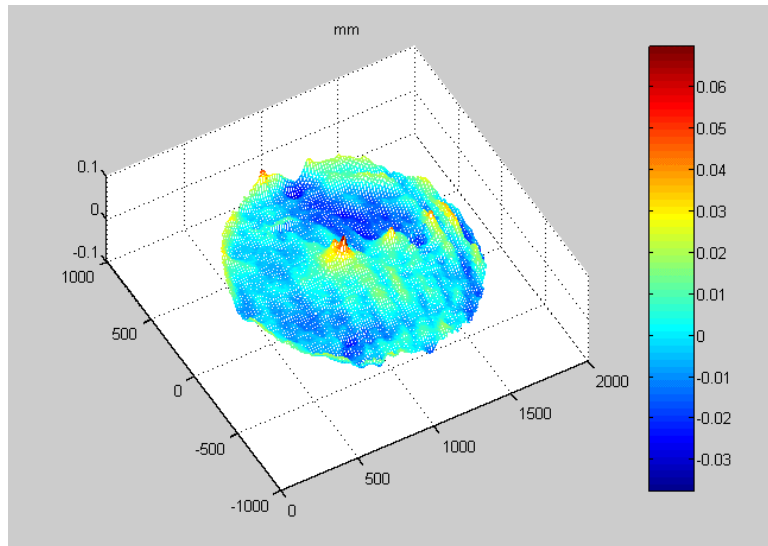


Figure 7.4-3 Residual deformations on the main reflector (unity in figure: mm)



#### 7.4.2.4.2 Sub reflector

The surface of the sub reflector has been measured by interferometry. The data contained in [RD 21] is a cloud of points providing the distortion along the normal at 798558 point on the surface. The cloud of points has been measured in the plane of the reflector in OM2C (mechanical coordinate system) see Figure 7.4-4.

In this state, this data cannot be exported in GRASP8 and need to be re-processed:

- First the distortion must be defined in the coordinate system associated with the definition of the reflector OM2 (more precisely in sub reflector coordinate system which is the OM2 coordinate system (vertex) translated at the focus point and rotated of 180°).
- Secondly, the distortion must be expressed as deviation in the z-axis where the z-axis belongs to the coordinate system of the perfect conic definition.

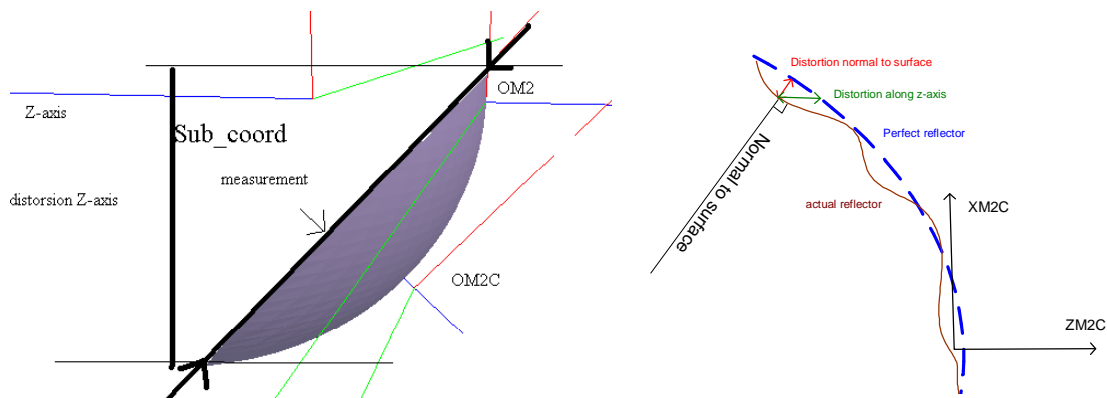


Figure 7.4-4 Sub reflector coordinate systems

The process used to fulfil these two conditions is described in the flow chart of Figure 7.4-5 and the result of this process is depicted in Figure 7.4-5.

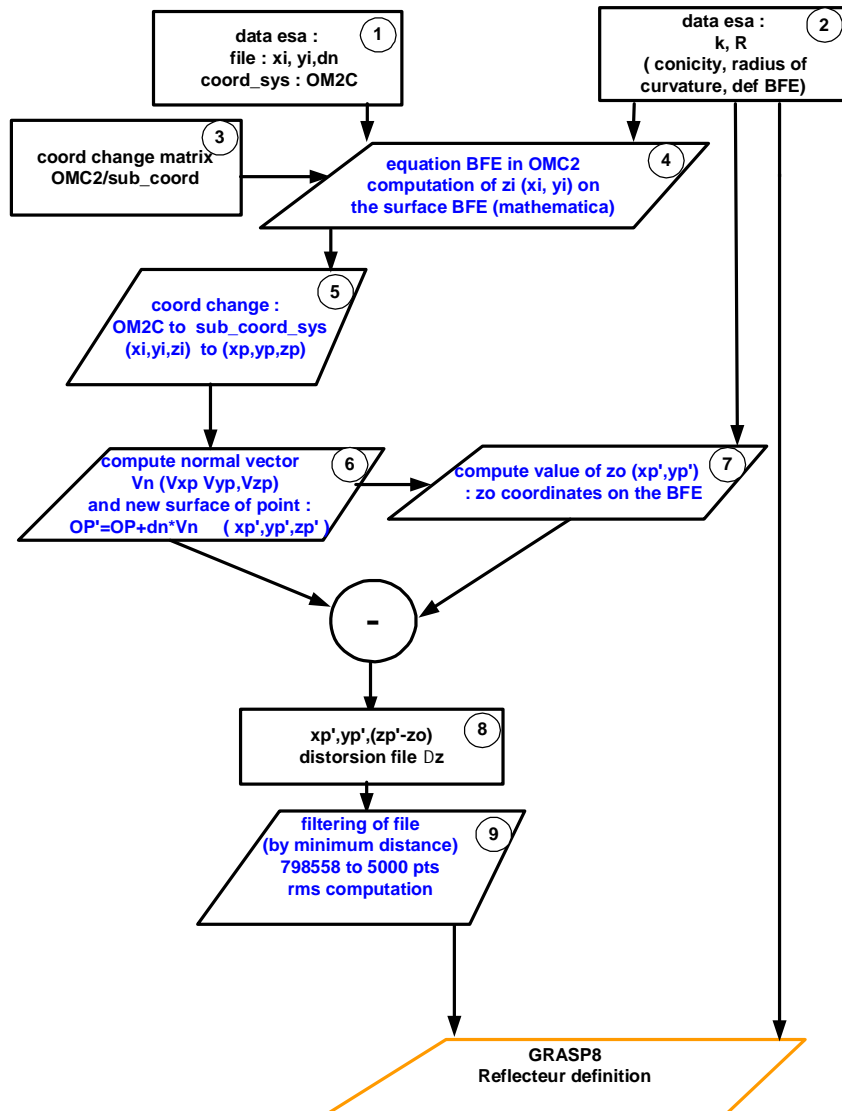


Figure 7.4-5 Process flow chart for the sub reflector distortion file

- 1: data from [RD21] contains 798558 points.
- 2: data recalled in Table 7.4-1.
- 3: data coordinate change matrix [RD20]
- 4: computation of the conic expression in OM2 and zi-coordinate computation
- 5: change coordinate system (xi, yi, zi) to (xp, yp, zp)
- 6: gradient computation: normal vector: real surface shape of the reflector (xp', yp', zp')
- 7: computation of the zo coordinates on the BFE.
- 8: subtract distortion file (xp', yp', zp'-zo)
- 9: filtering the distortion file: 798558 points to 5000 points (minimum distance 4.5 mm)

sub\_filtre  
delta\_sub\_N50\_45s.sfc

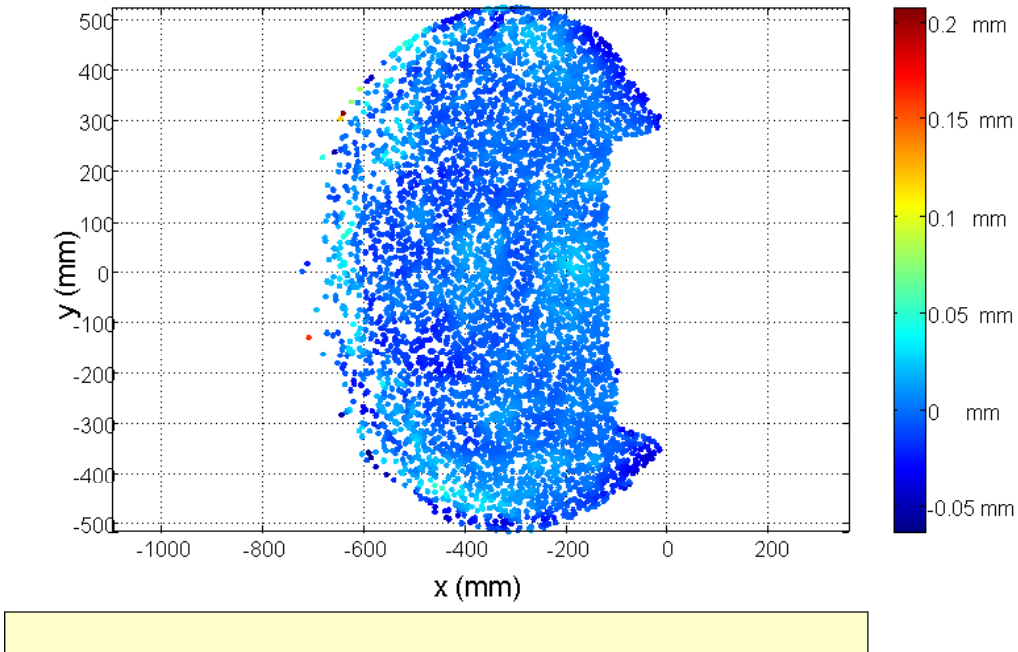


Figure 7.4-6 Residual deformations on the sub reflector (unity in figure mm)



### 7.4.2.5 Degradation (real structure)

As described in the previous chapter, the optimization of the geometrical configuration allows to define a goal for positioning the real reflectors and the FPU. The residual of this achievement is given in Table 7.4-4.

microns	Tx	Ty	Tz	Rx	Ry	dR	dK	coordinate
micronconrad								system
PR	0	0	0	0	0	151	-0,00012	OM1
SR	-1107	-33	-11	497	-1246	118	-0,00005	OM2
FPU	0	0	500	0	0	0		ORDP

Table 7.4-4 Real case degradation

This degradation will be added to the deterministic model.

### 7.4.2.6 Others contributors

The impact of others contributors detailed in [RD23 ] is given in Table 7.4-5.

microns/micron rad	Tx	Ty	Tz	rx	ry	dR	dK	coordinate
valeur delta								system
primary reflector	0,9	-7,8	202,3	-2,09	267,01	-18,5	4,00E-05	OM1
secondary reflector	104,8	-11,8	43,3	-1,3	167,91	14,7	5,30E-06	OM2

Table 7.4-5 Other contributors



#### 7.4.2.7 Global deterministic case

The establishment of the deterministic load case could be followed in the steps:

Case 0: impact of BFE deviation (configuration theoretical): Table 7.4-1.

Case 1 : impact of BFE deviation +realignment (by optimization) : Table 7.4-1 and Table 7.4-3

Case 2 : impact of BFE deviation + realignment (by optimization) + HF distortion : Table 7.4-1, Table 7.4-3, Figure 7.4-3 and Figure 7.4-6.

Case 3 : impact of BFE deviation +realignment (by optimization) +HF distortion + others contributors: Table 7.4-1+Table 7.4-3+Table 7.4-5 +

Figure 7.4-3+Figure 7.4-6 (see also Table 7.4-6)

Case 4 : impact of BFE deviation +realignment (by optimization) +HF distortion +otherz contributors +degradation: Table 7.4-1+Table 7.4-3+ Table 7.4-4+ Table 7.4-5

Figure 7.4-3+Figure 7.4-6 (See also Table 7.4-7).

Case 5 : impact of BFE deviation +realignment (by optimization) +HF distortion + others contributors +degradation (with compensation of defocus of  $-500 \mu\text{m}$  compared to real case 4) :Table 7.4-1+Table 7.4-3+ Table 7.4-4+ Table 7.4-5

Figure 7.4-3+Figure 7.4-6 (See also Table 7.4-7).

microns/micron rad										coordinate
valeur delta	Tx	Ty	Tz	rx	ry	dR	dK			system
primary reflector	-639,1	-7,8	162,3	-2,09	832,5	-903,5	2,08E-03			OM1
secondary reflector	354,8	-11,8	3,3	-1,3	733,4	-177,3	2,89E-04			OM2
FPU	0	0	2820	0	0					ORDP

Table 7.4-6 CASE 3 : contributors: BFE BF distortion + realignment +other IO contributors



microns micronconrad	Tx	Ty	Tz	Rx	Ry	dR	dK	coordinate system
PR	-639,1	-7,8	162,3	-2,09	832,5	-752,5	0,001957	OM1
SR	-752,2	-44,8	-7,7	495,7	-512,6	-59,3	0,000239	OM2
FPU	0	0	3320	0	0	0		ORDP
<b>FPU (autre cas)</b>			<b>2820</b>					<b>ORDP</b>

Table 7.4-7 Contributors: CASE 4 & 5 : BFE BF distortion + realignments + other contributors+degradation (real case)

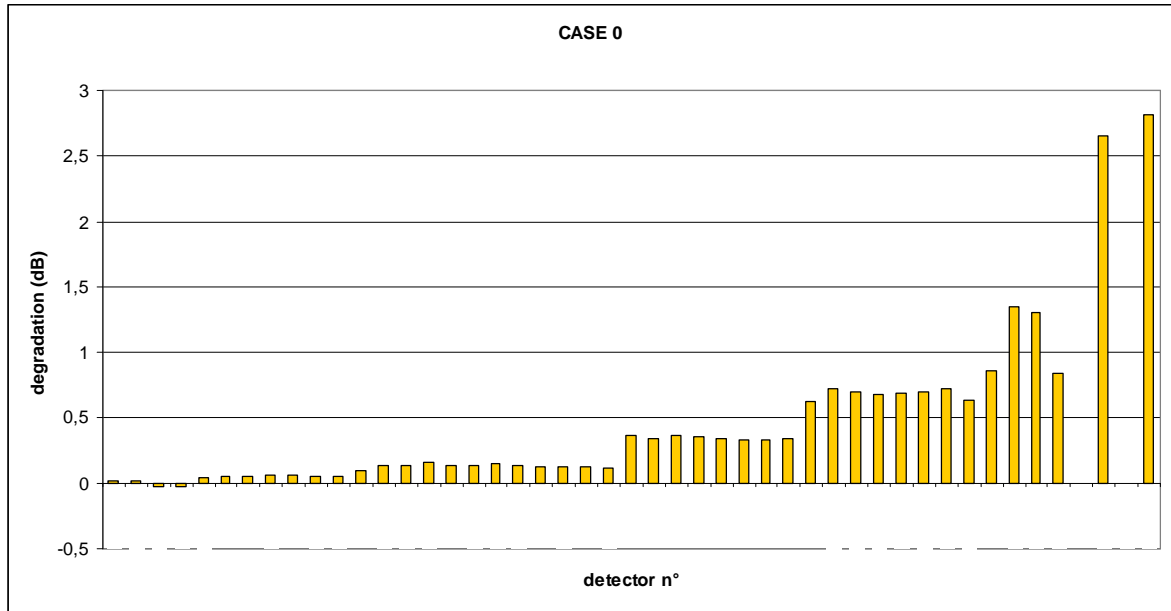


Figure 7.4-7 impact of BFE distortion

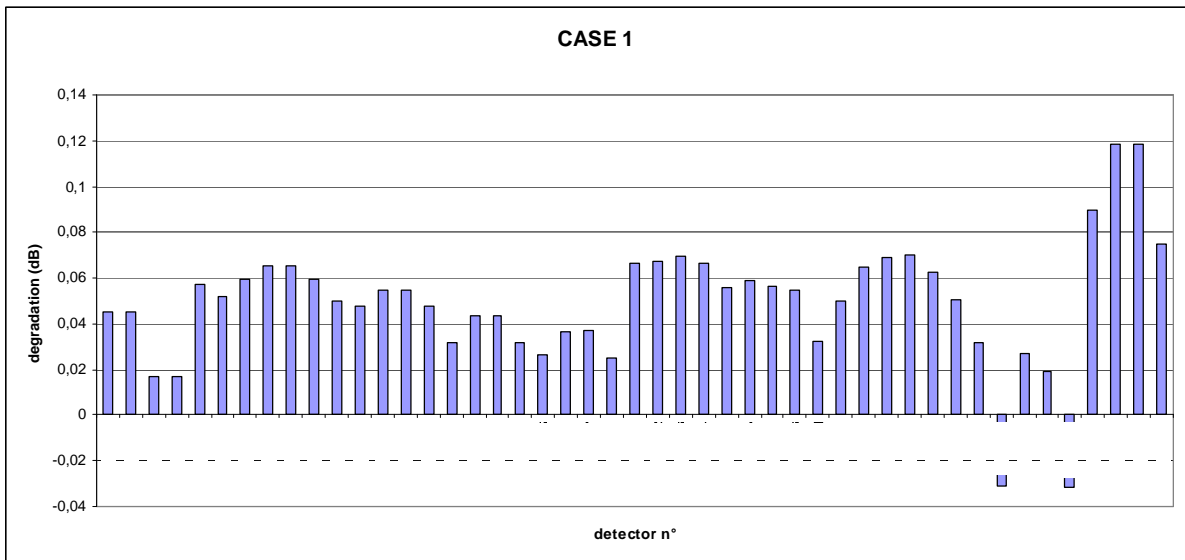


Figure 7.4-8 impact of BFE deviation +realignment

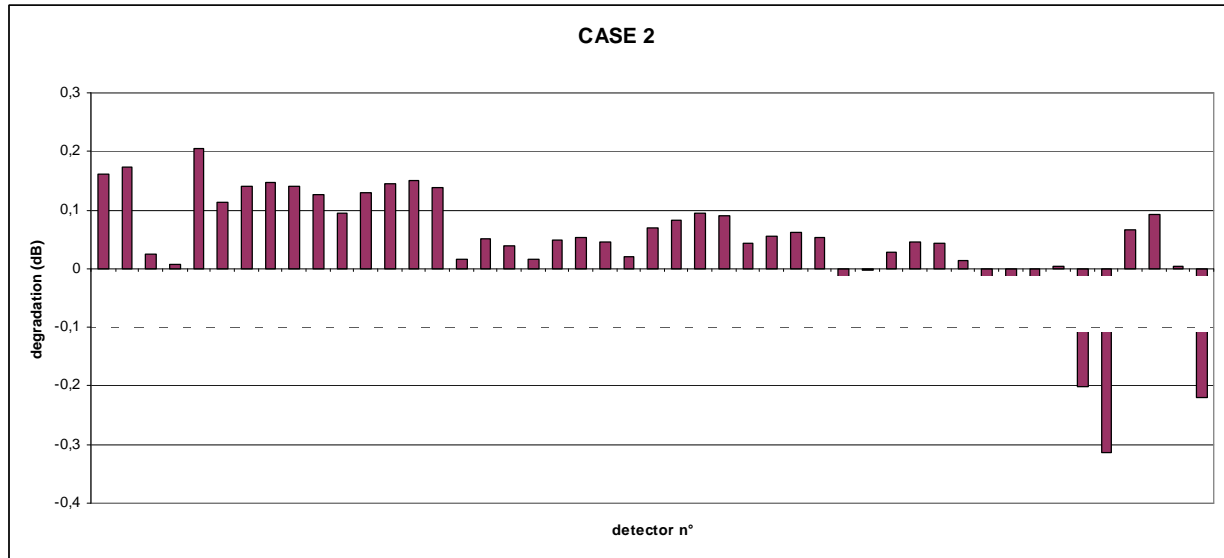


Figure 7.4-9 impact of BFE deviation +realignment (by optimization) +HF distortion

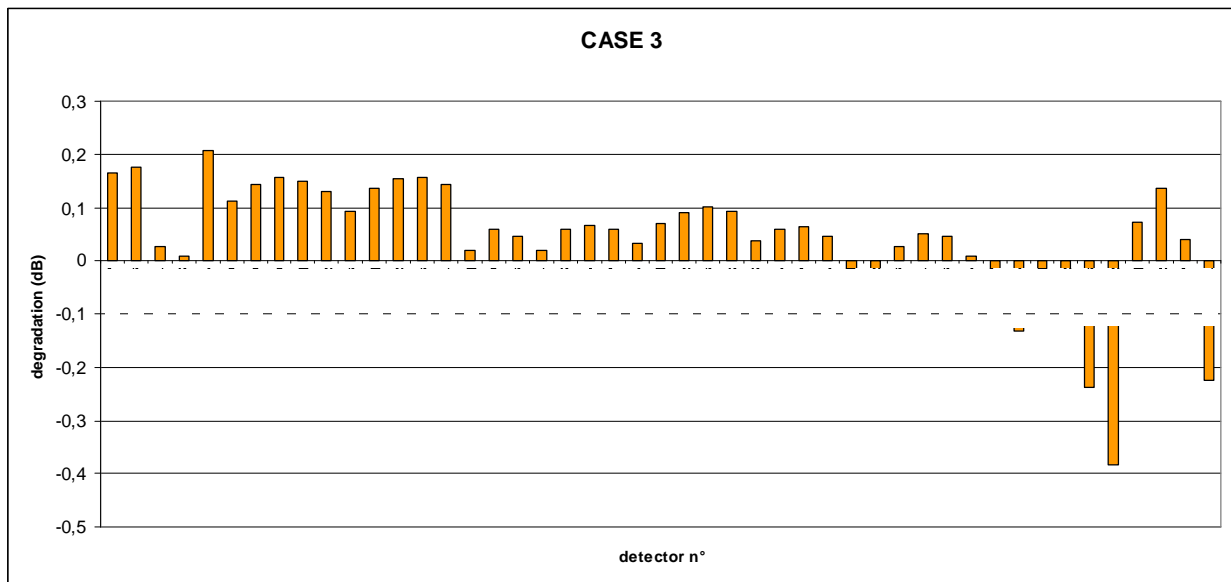


Figure 7.4-10 impact of BFE deviation +realignment (by optimization) +HF distortion +IO contributors



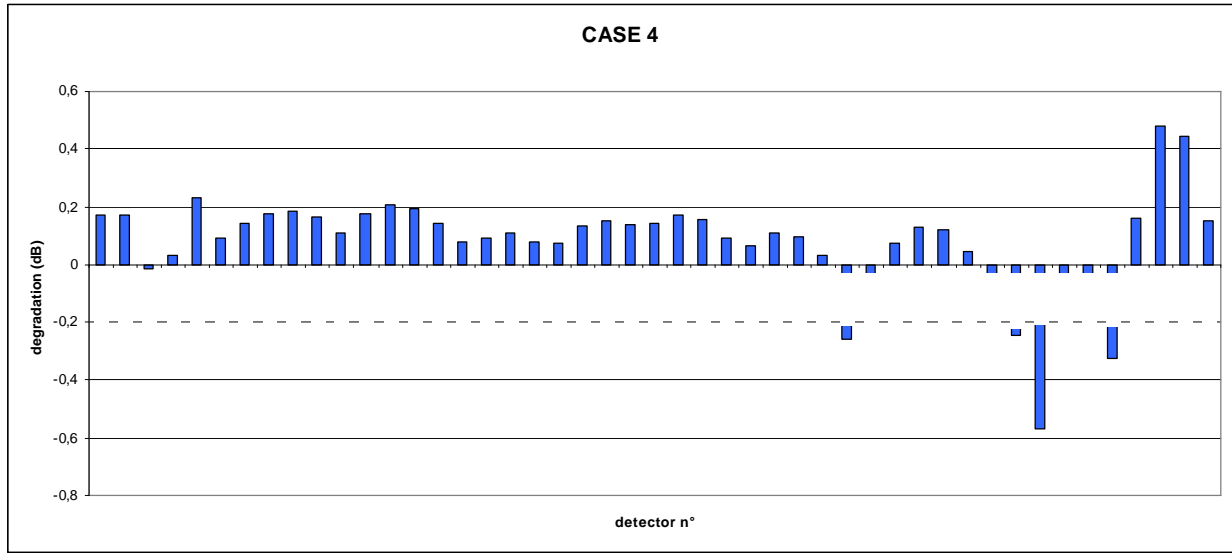


Figure 7.4-11 : impact of BFE deviation +realignment (by optimization) +HF distortion +IO contributors + degradation

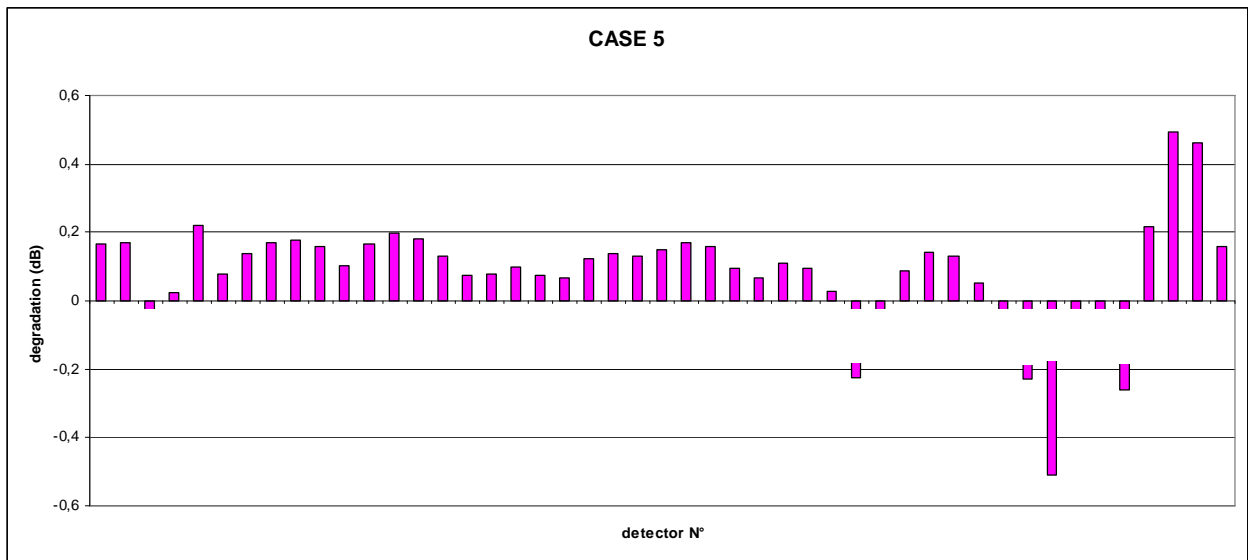


Figure 7.4-12 impact of BFE deviation +realignment (by optimization) +HF distortion +IO contributors+ degradation (with compensation of defocus of -500 compared to real case 4)

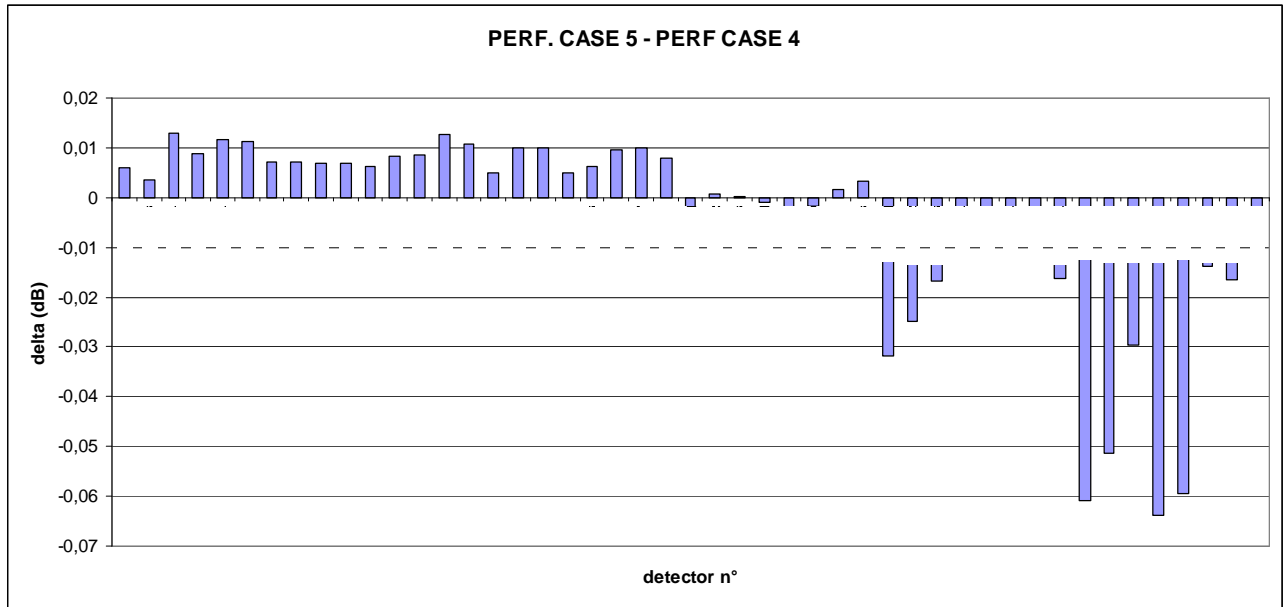


Figure 7.4-13 Improvement if FPU is displaced of -500 microns

CASE 0 : Gain degradation with the flight reflectors: BFE (measured by videogrammetry). The gain degradation is important if any realignment is performed. Moreover a significant depointing angle has been noticed in the patterns, more emphasized at higher frequencies.

CASE 1 : With the flight BFE, the model have been optimised to compensate the surface deviation, the residual gain degradation is around 0.12 dB for HFI-857 horns. The depointing has been corrected.

CASE 2 : The HF surfaces have been added to CASE1, The residual HF distortion degrade the gain at low frequencies and improve the gain at higher frequencies.

CASE 3 : The other IO contributors have been added to CASE 2, one can noticed a slight accentuation in the behaviour observed in CASE2.

CASE 4 : This one constitutes the real case. The alignment-measured data have been inserted in the model.

CASE 5 : This case is an investigation case : a compensation of the FPU by 500 μm translation has been investigated. A realignment of the FPU could improve results for lower frequencies but degrade the budget at higher frequencies.



### 7.4.2.8 Other contributors

Some of the contributors could not be calculated directly (be inserted in the numerical model for instance. A specific analysis is needed in order to evaluate their impact.

#### 7.4.2.8.1 Quilting

The quilting has been taken into account for the sub reflector and the measurement of the surface contain this information. For the main reflector, the reflector surface has not been updated since CDR. As a consequence and to be consequent with the budget, the presence of the quilting must be assessed as for CDR analysis even if his impact is almost negligible. The results are recalled in the Figure 7.4-14.

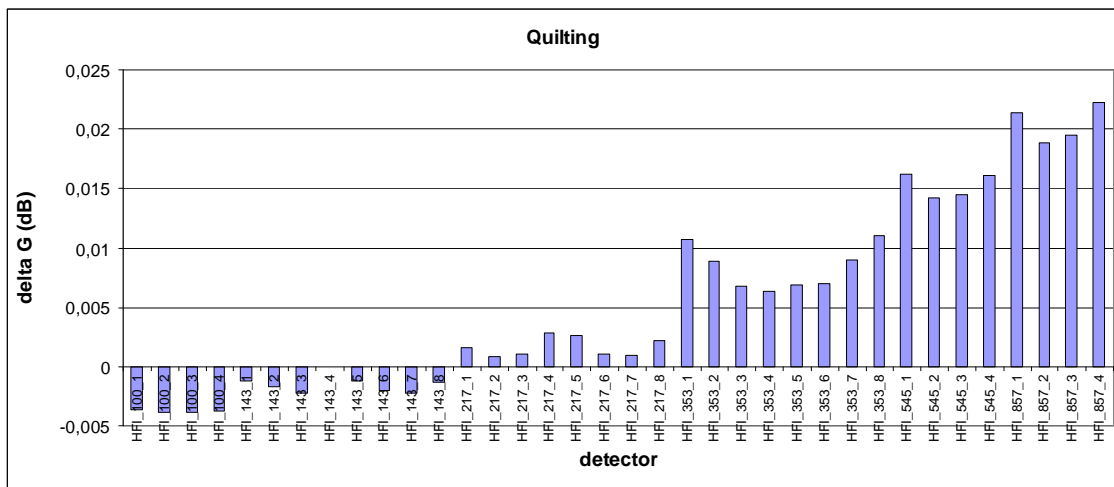


Figure 7.4-14 Degradation due to quilting

The quilting impact is reduced to 0.02 dB at higher frequencies for the two reflectors. In our case, we have considered an allocation for the main reflector of 0.01 dB for all the detectors.



#### 7.4.2.8.2 Ohmic losses

The ohmic losses depend on the surface materials used for the reflectors manufacturing and more precisely on the conductivity of the metal which itself depends on surface finishing and on the nature of the metal. The exact knowledge of the conductivity is difficult to obtain. Some measurement results could be found [1] and [2] up to 377 GHz.

In the scope of the estimation of the ohmic losses, a realistic values for the conductivity has been taken based on the remark in [1]: " the resistivity is twice as high as calculated from nominal DC conductivity" and on the actual quality of the reflector surface: the reflectors are made on pure aluminium.

Based on measurements and empirical assumptions [2]<sup>1</sup>, the reflection losses at a frequency F (in GHz) in submillimeter frequencies range, for bulk aluminium materials is found to be equal to:

$$L = 0.21 \% \sqrt{\frac{F}{100}} \quad (1)$$

which correspond to a conductivity of  $\sigma = 2 \cdot 10^{+7} \text{ S m}^{-1}$  at submillimeter frequencies range ( $\sigma = 4 \cdot 10^{+7} \text{ S m}^{-1}$  at DC)

For other conductivities the formula found in [1] could be used:

$$L = \frac{10.88 \cdot 10^{-3}}{30\text{p}} \sqrt{\frac{10^{10}}{3\text{s}}} \sqrt{\frac{F}{100}} \quad (2)$$

Where F is in GHz.

Different value of conductivity for Aluminium could be found in [1]<sup>2</sup> measured at ambient temperature and at frequencies up to 377 GHz. Ohmic losses decrease with temperature and the reflectors are assumed to be at 50 K.

Table 7.4-8 below resumes the values taken for the budget.

<sup>1</sup> [1] J. W. Zwart, V. O. Heinen, K. Long and N. Stankiewicz : "Surface resistance measurements at 377 GHz", Int. J. IR and Millimeter Waves, Vol. 17, no. 2, pp. 349-357, Dec. 1996.

<sup>2</sup> [2] J. W. Lamb, "Miscellaneous data on materials for millimetre and submillimetre optics", Int. J. IR and Millimeter Waves, Vol. 17, no. 12, pp. 1997-2034, Dec. 1996.



frequency (GHz)	delta directivity (dB)
30	0,0071
44	0,0086
70	0,0109
100	0,0130
143	0,0156
217	0,0192
353	0,0245
545	0,0305
857	0,0382

Table 7.4-8 Gain degradation due to ohmic losses

#### 7.4.2.8.3 Roughness

The roughness also intervenes implicitly in the ohmic losses by increasing the surface resistivity, and hence, reducing the efficiency of the reflector surface.

The roughness could be characterised by a peak-to-peak value and a correlation length. As long as this type of contribution is by nature random with small spatial frequency, its impact could not be computed through the numerical model. Therefore, to estimate the directivity degradation Ruze formula approximated for main peak is used. According to the reflector specification, the surface is assumed to have roughness of 0.2  $\mu\text{m}$  rms.

For a roughness of 0.2  $\mu\text{m}$  rms, it is clearly demonstrated that the roughness has negligible impact (see Table 2-9).

Frequency GHz	WFE inputs (mm)	delta G (dB) (Ruze)
30	0,2	NS
44	0,2	NS
70	0,2	NS
100	0,2	NS
143	0,2	NS
217	0,2	NS
353	0,2	NS
545	0,2	NS
857	0,2	0,0001

Table 7.4-9 Gain degradation due to roughness



#### 7.4.2.8.4 Micro-cracks effect

Microcracks could be defined as fine slots randomly distributed on the surface of the reflectors.

But for the CDR budget, it has been agreed that there is no microcraks on the reflectors.

#### 7.4.2.8.5 Contamination

An allocation is provided on the basis of a 2  $\mu\text{m}$  rms surface error, which is representative of particular contamination:

Frequency GHz	WFE inputs (mm)	delta G (dB) (Ruze)
30	2	NS
44	2	NS
70	2	NS
100	2	0,0001
143	2	0,0002
217	2	0,0004
353	2	0,0009
545	2	0,0023
857	2	0,0056

Table 7.4-10 Gain degradation due to contamination (NS :not significant)

#### 7.4.2.9 Deterministic contributor budget

In Table 2-11 and Figure 2-18, the total budget for the deterministic contributors is presented.



DETECTOR	deterministic case 4 dB	deterministic case 5 dB	quilting main dB	ohmic losses dB	contamination dB	total with case 4 dB	total with case 5 dB
LFI_30_27	0,1718	0,1656	0,0100	0,0071	ns	<b>0,1889</b>	0,1827
LFI_30_28	0,1715	0,1680	0,0100	0,0071	ns	<b>0,1886</b>	0,1851
LFI_44_24	-0,0154	-0,0284	0,0100	0,0086	ns	<b>0,0032</b>	-0,0098
LFI_44_25	0,0335	0,0246	0,0100	0,0086	ns	<b>0,0521</b>	0,0432
LFI_44_26	0,2322	0,2207	0,0100	0,0086	ns	<b>0,2508</b>	0,2393
LFI_70_18	0,0900	0,0786	0,0100	0,0109	ns	<b>0,1109</b>	0,0995
LFI_70_19	0,1438	0,1367	0,0100	0,0109	ns	<b>0,1647</b>	0,1576
LFI_70_20	0,1763	0,1691	0,0100	0,0109	ns	<b>0,1972</b>	0,1900
LFI_70_21	0,1848	0,1780	0,0100	0,0109	ns	<b>0,2057</b>	0,1989
LFI_70_22	0,1642	0,1573	0,0100	0,0109	ns	<b>0,1851</b>	0,1782
LFI_70_23	0,1096	0,1032	0,0100	0,0109	ns	<b>0,1305</b>	0,1241
HFI_100_1	0,1741	0,1659	0,0100	0,0130	0,0001	<b>0,1971</b>	0,1889
HFI_100_2	0,2062	0,1977	0,0100	0,0130	0,0001	<b>0,2292</b>	0,2207
HFI_100_3	0,1941	0,1812	0,0100	0,0130	0,0001	<b>0,2171</b>	0,2042
HFI_100_4	0,1417	0,1308	0,0100	0,0130	0,0001	<b>0,1647</b>	0,1538
HFI_143_1	0,0801	0,0750	0,0100	0,0156	0,0002	<b>0,1057</b>	0,1006
HFI_143_2	0,0906	0,0805	0,0100	0,0156	0,0002	<b>0,1162</b>	0,1061
HFI_143_3	0,1102	0,1002	0,0100	0,0156	0,0002	<b>0,1358</b>	0,1258
HFI_143_4	0,0801	0,0750	0,0100	0,0156	0,0002	<b>0,1057</b>	0,1006
HFI_143_5	0,0733	0,0668	0,0100	0,0156	0,0002	<b>0,0989</b>	0,0924
HFI_143_6	0,1338	0,1242	0,0100	0,0156	0,0002	<b>0,1594</b>	0,1498
HFI_143_7	0,1496	0,1396	0,0100	0,0156	0,0002	<b>0,1752</b>	0,1652
HFI_143_8	0,1373	0,1293	0,0100	0,0156	0,0002	<b>0,1629</b>	0,1549
HFI_217_1	0,1432	0,1520	0,0100	0,0192	0,0004	<b>0,1724</b>	0,1812
HFI_217_2	0,1703	0,1695	0,0100	0,0192	0,0004	<b>0,1995</b>	0,1987
HFI_217_3	0,1572	0,1570	0,0100	0,0192	0,0004	<b>0,1864</b>	0,1862
HFI_217_4	0,0934	0,0942	0,0100	0,0192	0,0004	<b>0,1226</b>	0,1234
HFI_217_5	0,0617	0,0661	0,0100	0,0192	0,0004	<b>0,0909</b>	0,0953
HFI_217_6	0,1104	0,1121	0,0100	0,0192	0,0004	<b>0,1396</b>	0,1413
HFI_217_7	0,0975	0,0959	0,0100	0,0192	0,0004	<b>0,1267</b>	0,1251
HFI_217_8	0,0323	0,0291	0,0100	0,0192	0,0004	<b>0,0615</b>	0,0583
HFI_353_1	-0,2576	-0,2257	0,0100	0,0245	0,0009	<b>-0,2231</b>	-0,1912
HFI_353_2	-0,0600	-0,0352	0,0100	0,0245	0,0009	<b>-0,0255</b>	-0,0007
HFI_353_3	0,0713	0,0881	0,0100	0,0245	0,0009	<b>0,1058</b>	0,1226
HFI_353_4	0,1308	0,1433	0,0100	0,0245	0,0009	<b>0,1653</b>	0,1778
HFI_353_5	0,1210	0,1299	0,0100	0,0245	0,0009	<b>0,1555</b>	0,1644
HFI_353_6	0,0436	0,0518	0,0100	0,0245	0,0009	<b>0,0781</b>	0,0863
HFI_353_7	-0,0875	-0,0758	0,0100	0,0245	0,0009	<b>-0,0530</b>	-0,0413
HFI_353_8	-0,2464	-0,2302	0,0100	0,0245	0,0009	<b>-0,2119</b>	-0,1957
HFI_545_1	-0,5709	-0,5101	0,0100	0,0305	0,0023	<b>-0,5304</b>	-0,4696
HFI_545_2	-0,1831	-0,1318	0,0100	0,0305	0,0023	<b>-0,1426</b>	-0,0913
HFI_545_3	-0,1610	-0,1313	0,0100	0,0305	0,0023	<b>-0,1205</b>	-0,0908
HFI_545_4	-0,3245	-0,2606	0,0100	0,0305	0,0023	<b>-0,2840</b>	-0,2201
HFI_857_1	0,1588	0,2183	0,0100	0,0382	0,0056	<b>0,2070</b>	0,2665
HFI_857_2	0,4789	0,4926	0,0100	0,0382	0,0056	<b>0,5271</b>	0,5408
HFI_857_3	0,4450	0,4616	0,0100	0,0382	0,0056	<b>0,4932</b>	0,5098
HFI_857_4	0,1530	0,1573	0,0100	0,0382	0,0056	<b>0,2012</b>	0,2055

Table 7.4-11 Determinist: Budget (ns : not significant)



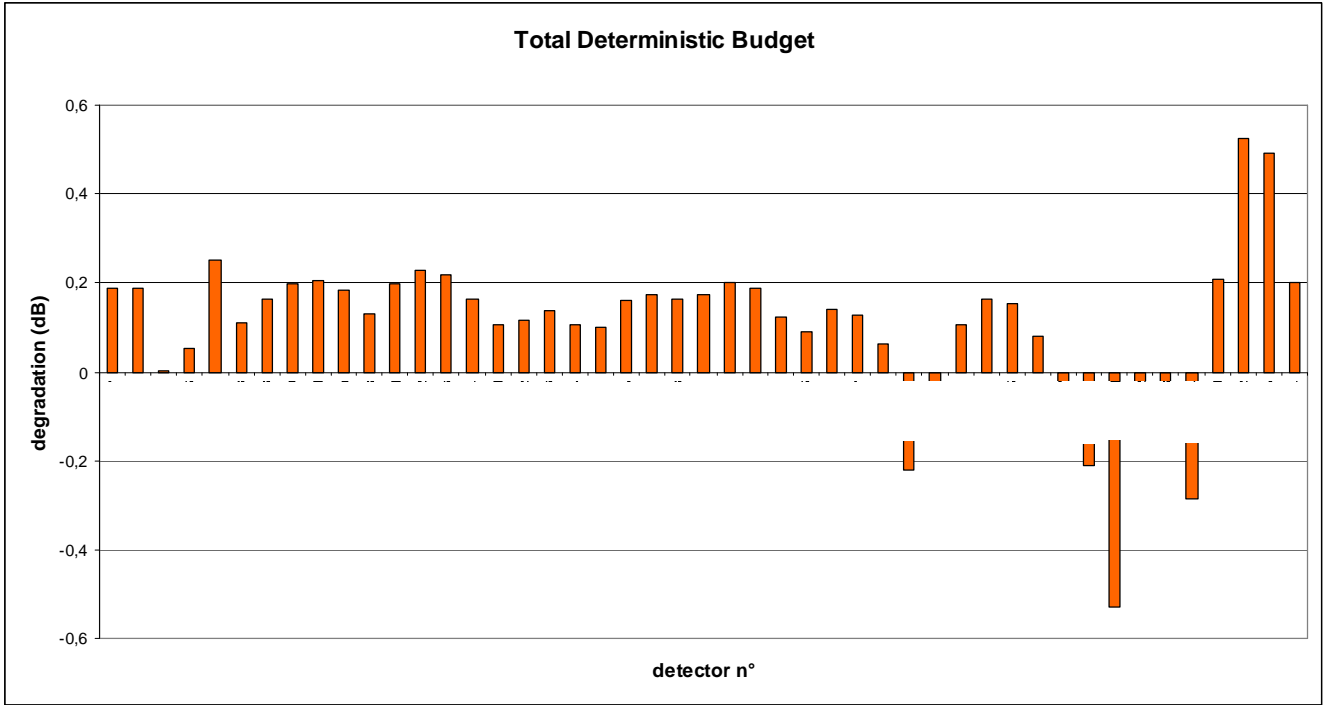


Figure 7.4-15 Determinist: Budget



#### 7.4.2.10 Conclusion

The deterministic budget have been established with updated data (only the main reflector surface has not been updated). The budget shows a maximum of gain degradation of 0.5 dB at 857 GHz and of less than 0.22 dB for the others horns. However, the deterministic configuration gives an improvement compared to theoretical model for HFI 545 horns and few 353 GHz horns.



### 7.4.3 Statistic contributors

#### 7.4.3.1 Origin of inputs

These contributors could be divided into different levels:

- Telescope level
- Focal Plane Unit
- Telescope-FPU integration
- Contingency

The random case at operational is composed of numerous contributors. The data are of two main types: inputs furnished in WFE rms per horn, inputs described in term of BFE random displacements and distortions (translation, rotation, conicity, radius variations). The details of these data are presented in [RD 20]. In this §, only a recall of the inputs is presented followed by the corresponding gain degradation.

This § is divided into two parts: Manufacturing, accuracy budget per Horn and random displacements.

Each part is detailed in the following sections.

#### 7.4.3.2 Manufacturing and accuracy budget per Horn

This section deals with:

- BFE knowledge and structure videogrammetry
- Others contributors: Horns manufacturing, Reflector settling and launch, Reflector coating. /Storage/Optical model

##### 7.4.3.2.1 BFE knowledge and structure videogrammetry

This contributor is the consequence of the measurements uncertainties of the real geometrical configuration of the FM reflectors and their positioning.

The inputs are extracted from optical analysis [RD23] and are recalled in the table below:



RANDOM CASE		BFE Knowledge and structure videogrammetry					
microns	microrad						
REFLECTOR							
	Tx	Ty	Tz	Rx	Ry	dR	dK
PR	100	13	66	140	55	130	0,00010
SR	170	27	200	150	325	25	0,00009
STRUCTURE							
	Tx	Ty	Tz	Rx	Ry	dR	dK
PR	135,9	27,1	26,9	62,5	102,9		
SR	53,4	27,6	32,2	69,5	194,4		
FPU	25	25	40				

Table 7.4-12 Inputs for BFE Knowledge and structure videogrammetry

As the contributors are by nature random, for each deviation (each case of Table 7.4-12) must be computed independently and the degradation induced by each one added by RSS.

For illustration the Table 7.4-12 need  $(7+7+5+5+3) \times 2 \times 47 = 2538$  patterns. computation

The results are presented in the Table 7.4-13 by series a, b, c, d and e corresponding to each line of Table 7.4-12.



detector n°	case a	case b	case c	case d	case e	BFE Know
	dB	dB	dB	dB	dB	dB
lfi_30_27	0,0045	0,0172	0,0045	0,0034	0,0008	0,0187
lfi_30_28	0,0041	0,0173	0,0040	0,0036	0,0007	0,0186
lfi_44_24	0,0136	0,0142	0,0094	0,0067	0,0010	0,0228
lfi_44_25	0,0136	0,0141	0,0094	0,0068	0,0011	0,0228
lfi_44_26	0,0049	0,0318	0,0038	0,0041	0,0008	0,0327
lfi_70_18	0,0134	0,0126	0,0065	0,0051	0,0011	0,0202
lfi_70_19	0,0144	0,0190	0,0058	0,0056	0,0011	0,0252
lfi_70_20	0,0077	0,0287	0,0056	0,0056	0,0009	0,0308
lfi_70_21	0,0073	0,0286	0,0058	0,0054	0,0009	0,0306
lfi_70_22	0,0110	0,0188	0,0053	0,0058	0,0011	0,0232
lfi_70_23	0,0113	0,0126	0,0065	0,0051	0,0011	0,0189
hfi_100_1	0,0163	0,0158	0,0079	0,0064	0,0018	0,0249
hfi_100_2	0,0108	0,0354	0,0069	0,0094	0,0025	0,0389
hfi_100_3	0,0115	0,0354	0,0068	0,0094	0,0023	0,0391
hfi_100_4	0,0226	0,0158	0,0095	0,0057	0,0018	0,0298
hfi_143_1	0,0296	0,0268	0,0128	0,0111	0,0034	0,0435
hfi_143_2	0,0112	0,0287	0,0086	0,0116	0,0035	0,0342
hfi_143_3	0,0098	0,0292	0,0083	0,0068	0,0011	0,0326
hfi_143_4	0,0296	0,0268	0,0128	0,0111	0,0034	0,0435
hfi_143_5	0,0389	0,0419	0,0179	0,0123	0,0011	0,0612
hfi_143_6	0,0202	0,0641	0,0158	0,0139	0,0009	0,0704
hfi_143_7	0,0193	0,0626	0,0153	0,0125	0,0009	0,0684
hfi_143_8	0,0302	0,0451	0,0149	0,0143	0,0027	0,0581
hfi_217_1	0,0236	0,0203	0,0152	0,0097	0,0039	0,0362
hfi_217_2	0,0197	0,0284	0,0189	0,0086	0,0019	0,0404
hfi_217_3	0,0200	0,0285	0,0195	0,0080	0,0016	0,0407
hfi_217_4	0,0281	0,0212	0,0162	0,0090	0,0034	0,0399
hfi_217_5	0,0143	0,0209	0,0081	0,0066	0,0022	0,0275
hfi_217_6	0,0085	0,0081	0,0130	0,0065	0,0030	0,0189
hfi_217_7	0,0130	0,0138	0,0116	0,0062	0,0018	0,0231
hfi_217_8	0,0192	0,0252	0,0081	0,0085	0,0025	0,0339
hfi_353_1	0,0847	0,2232	0,0291	0,0347	0,0046	0,2430
hfi_353_2	0,0461	0,1233	0,0230	0,0188	0,0033	0,1350
hfi_353_3	0,0370	0,0558	0,0390	0,0176	0,0028	0,0795
hfi_353_4	0,0450	0,0648	0,0494	0,0241	0,0027	0,0962
hfi_353_5	0,0437	0,0645	0,0526	0,0254	0,0029	0,0974
hfi_353_6	0,0294	0,0655	0,0397	0,0170	0,0031	0,0838
hfi_353_7	0,0522	0,1340	0,0218	0,0220	0,0039	0,1472
hfi_353_8	0,0831	0,2240	0,0327	0,0329	0,0048	0,2434
hfi_545_1	0,1789	0,4296	0,0757	0,0679	0,0117	0,4765
hfi_545_2	0,1246	0,2483	0,0691	0,0446	0,0119	0,2900
hfi_545_3	0,1111	0,2818	0,0582	0,0474	0,0100	0,3122
hfi_545_4	0,1639	0,4187	0,0635	0,0639	0,0099	0,4587
hfi_857_1	0,2204	0,3651	0,2632	0,1212	0,0259	0,5162
hfi_857_2	0,2484	0,4178	0,2967	0,1440	0,0232	0,5878
hfi_857_3	0,2470	0,4094	0,2947	0,1388	0,0231	0,5790
hfi_857_4	0,2094	0,3942	0,2485	0,1127	0,0276	0,5239

Table 7.4-13 Results for BFE knowledge and structure videogrammetry



### 7.4.3.2.2 Horns manufacturing and others contributors

Frequency	30	44	70	100	143	217	353	545	857
Horn manufacture	13	13	13	10	8	8	5	5	5
Reflector settling launch	1	1	1	1	1	1	1	1	1
Reflector coating/storage	2,5	2,5	2,5	2,5	2,5	2,5	2,5	2,5	2,5
Optical model	2	2	2	2	2	2	2	2	2
									0,6
WFE (RSS) mm	13,4	13,4	13,4	10,5	8,7	8,7	6,0	6,0	6,1
DG (dB) (Ruze)	0,0003	0,0007	0,0017	0,0021	0,0029	0,0068	0,0086	0,0205	0,0512

Table 7.4-14 Inputs in WFE for the others contributors and gain degradation

Table 7.4-14 gives the WFE per horns. [RD23]. The quantification in term of gain degradation is obtained through Ruze formula:

$$\Delta G_{dB} = \frac{10}{\ln(10)} \left( \frac{2p \text{ WFE}}{l} \right)^2$$



### 7.4.3.2.3 Budget for Manufacturing and accuracy

The budget is computed by summing (RSS) of Table 7.4-13 and Table 7.4-14. The gain degradation associated with this contributor is depicted in Figure 7.4-16.

detector n°	BFE Know dB	Other cont. dB	Total dB
lfi_30_27	0,0187	0,0030	<b>0,0189</b>
lfi_30_28	0,0186	0,0030	<b>0,0188</b>
lfi_44_24	0,0228	0,0007	<b>0,0228</b>
lfi_44_25	0,0228	0,0007	<b>0,0228</b>
lfi_44_26	0,0327	0,0007	<b>0,0327</b>
lfi_70_18	0,0202	0,0017	<b>0,0203</b>
lfi_70_19	0,0252	0,0017	<b>0,0252</b>
lfi_70_20	0,0308	0,0017	<b>0,0308</b>
lfi_70_21	0,0306	0,0017	<b>0,0306</b>
lfi_70_22	0,0232	0,0017	<b>0,0232</b>
lfi_70_23	0,0189	0,0017	<b>0,0189</b>
hfi_100_1	0,0249	0,0021	<b>0,0250</b>
hfi_100_2	0,0389	0,0021	<b>0,0389</b>
hfi_100_3	0,0391	0,0021	<b>0,0391</b>
hfi_100_4	0,0298	0,0021	<b>0,0298</b>
hfi_143_1	0,0435	0,0029	<b>0,0436</b>
hfi_143_2	0,0342	0,0029	<b>0,0343</b>
hfi_143_3	0,0326	0,0029	<b>0,0328</b>
hfi_143_4	0,0435	0,0029	<b>0,0436</b>
hfi_143_5	0,0612	0,0029	<b>0,0612</b>
hfi_143_6	0,0704	0,0029	<b>0,0705</b>
hfi_143_7	0,0684	0,0029	<b>0,0685</b>
hfi_143_8	0,0581	0,0029	<b>0,0582</b>
hfi_217_1	0,0362	0,0068	<b>0,0368</b>
hfi_217_2	0,0404	0,0068	<b>0,0409</b>
hfi_217_3	0,0407	0,0068	<b>0,0413</b>
hfi_217_4	0,0399	0,0068	<b>0,0405</b>
hfi_217_5	0,0275	0,0068	<b>0,0283</b>
hfi_217_6	0,0189	0,0068	<b>0,0201</b>
hfi_217_7	0,0231	0,0068	<b>0,0241</b>
hfi_217_8	0,0339	0,0068	<b>0,0346</b>
hfi_353_1	0,2430	0,0086	<b>0,2432</b>
hfi_353_2	0,1350	0,0086	<b>0,1353</b>
hfi_353_3	0,0795	0,0086	<b>0,0800</b>
hfi_353_4	0,0962	0,0086	<b>0,0966</b>
hfi_353_5	0,0974	0,0086	<b>0,0978</b>
hfi_353_6	0,0838	0,0086	<b>0,0843</b>
hfi_353_7	0,1472	0,0086	<b>0,1474</b>
hfi_353_8	0,2434	0,0086	<b>0,2436</b>
hfi_545_1	0,4765	0,0205	<b>0,4769</b>
hfi_545_2	0,2900	0,0205	<b>0,2907</b>
hfi_545_3	0,3122	0,0205	<b>0,3129</b>
hfi_545_4	0,4587	0,0205	<b>0,4591</b>
hfi_857_1	0,5162	0,0512	<b>0,5188</b>
hfi_857_2	0,5878	0,0512	<b>0,5901</b>
hfi_857_3	0,5790	0,0512	<b>0,5813</b>
hfi_857_4	0,5239	0,0512	<b>0,5264</b>

Table 7.4-15 Total budget for Manufacturing and accuracy



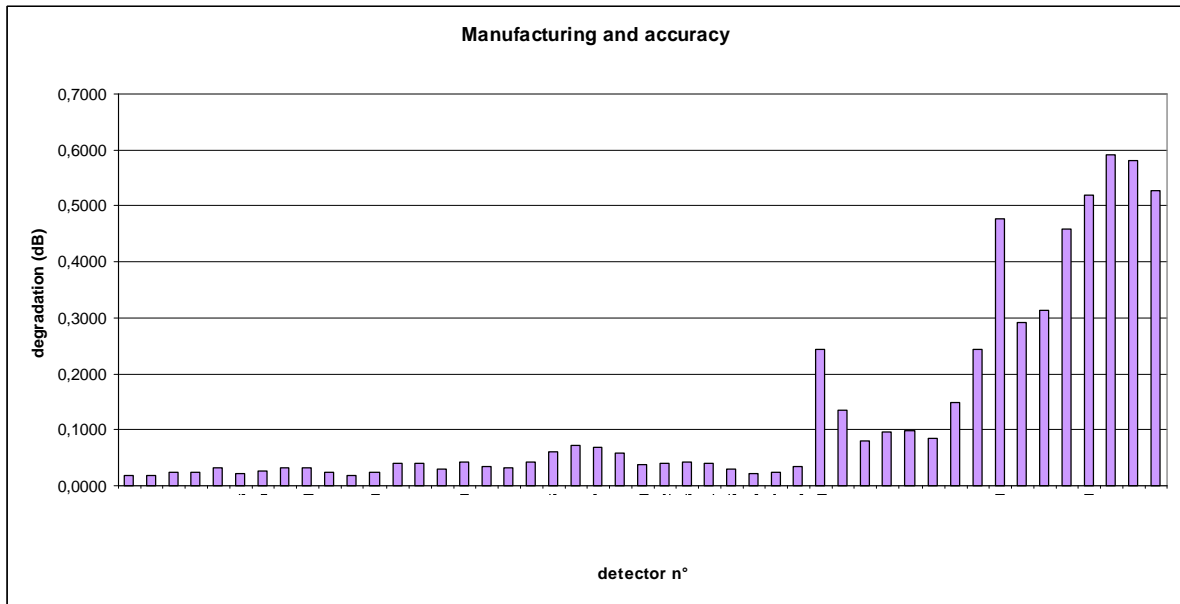


Figure 7.4-16 Budget for Manufacturing and accuracy



### 7.4.3.3 BFE random displacements and distortions

From [RD3 each contributor is expanded in the variations of seven parameters Rx, Ry, Tx, Ty, Tz, ΔK, ΔR in each coordinate system (OM1 , OM1C, OM2, OM2C and ORDP).

This chapter divided into two parts: FPU random displacement and PR and SR displacement case.

#### 7.4.3.3.1 FPU random displacement

Inputs for random displacements: are given in Table 7.4-16

<b>RANDOM</b>	<b>CASE</b>	<b>FPU random budget</b>			
<b>microns</b>	<b>microrad</b>				
<b>REFLECTOR</b>					
	<b>Tx</b>	<b>Ty</b>	<b>Tz</b>	<b>Rx</b>	<b>Ry</b>
<b>FPU</b>	120	107	287	0	0

Table 7.4-16 Inputs for FPU random case

The number of patterns to be calculated is  $3 \times 2 \times 47 = 282$ .

The results corresponding to this case are given in Table 7.4-17 and plotted in Figure 7.4-17.



detector n°	FPU
dB	random
lfi_30_27	0,0049
lfi_30_28	0,0047
lfi_44_24	0,0067
lfi_44_25	0,0069
lfi_44_26	0,0052
lfi_70_18	0,0059
lfi_70_19	0,0054
lfi_70_20	0,0045
lfi_70_21	0,0048
lfi_70_22	0,0058
lfi_70_23	0,006
hfi_100_1	0,0069
hfi_100_2	0,0042
hfi_100_3	0,004
hfi_100_4	0,0069
hfi_143_1	0,0066
hfi_143_2	0,0073
hfi_143_3	0,004
hfi_143_4	0,0066
hfi_143_5	0,004
hfi_143_6	0,0051
hfi_143_7	0,0044
hfi_143_8	0,0056
hfi_217_1	0,0046
hfi_217_2	0,002
hfi_217_3	0,0013
hfi_217_4	0,0038
hfi_217_5	0,0032
hfi_217_6	0,0024
hfi_217_7	0,0022
hfi_217_8	0,0026
hfi_353_1	0,0223
hfi_353_2	0,0206
hfi_353_3	0,0122
hfi_353_4	0,013
hfi_353_5	0,0141
hfi_353_6	0,0145
hfi_353_7	0,018
hfi_353_8	0,0235
hfi_545_1	0,0728
hfi_545_2	0,0643
hfi_545_3	0,0669
hfi_545_4	0,071
hfi_857_1	0,1559
hfi_857_2	0,1378
hfi_857_3	0,1391
hfi_857_4	0,16

Table 7.4-17 FPU random Budget

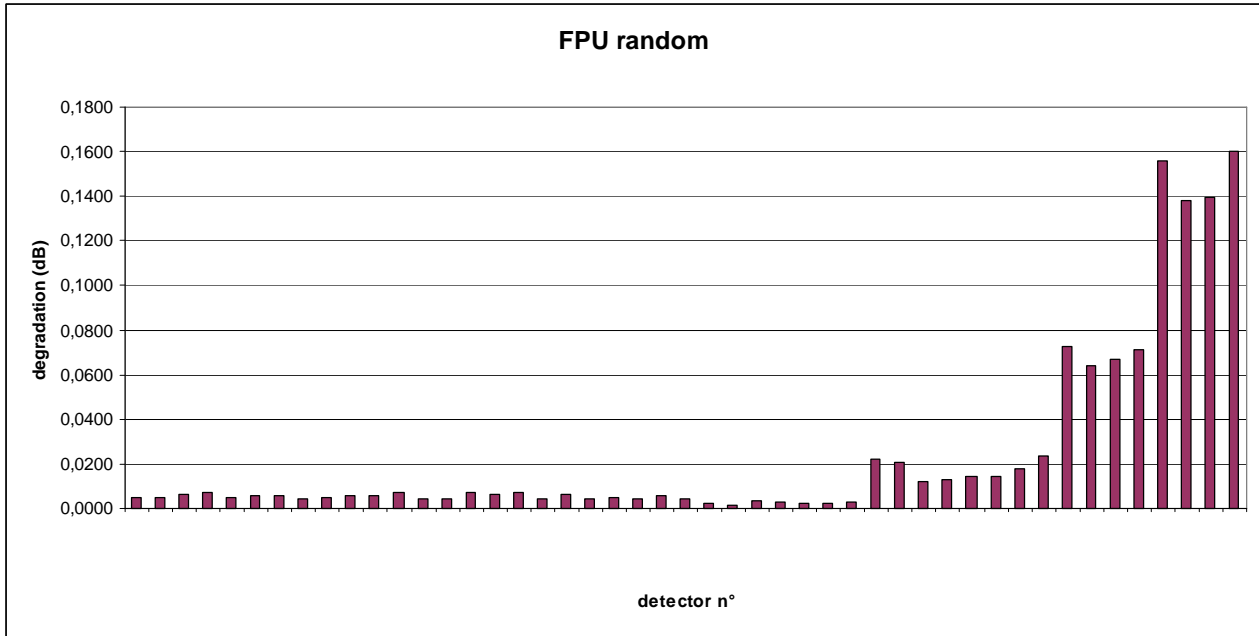


Figure 7.4-17 FPU random budget



#### 7.4.3.3.2 BFE deviation, PR and SR displacements

The contributors are listed in Table 2-14 and Table 2-15 with the details on data organisation. Each contributor impact is computed as defined in Table 2-16.

In order to facilitate the computation each line have been numbered by C1 to C68 (case 1 to 68). Each line has been calculated according to the description in Table 7.4-20. The results of these calculations are shown in the Table 7.4-21 to Table 7.4-27. The number of computation is almost =  $(24 \times 4 + 16 + 26) \times 2 \times 47 = 12972$  patterns.



	case n°	Tx μm	Ty μm	Tz μm	Rx μrad	Ry μrad	dR μm	dK	Correlated?	Refocus ?	Nature	Rep		
PR	QM Videogram,	C1	48,0	0,0	168,0	0,0	69,1	0,0	0	No	Yes	2sig	OM1C	
PR	QM T scaling	C2	-4,8	0,0	-2,7	0,0	0,1	0,0	0	Yes(*)	Yes	2sig	OM1C	
PR	QM T know	C3	-1,0	0,0	-0,6	0,0	0,0	0,0	0	Yes(*)	Yes	2sig	OM1C	
PR	CTE non-unif	Frame	1,8	0,1	-2,1	0,0	-0,7	0,0	0	Yes(*)	Yes	2sig	OM1C	
PR	CTE non-unif	Pr pan	-7,0	0,0	-3,4	0,0	-9,4	0,0	0	Yes(*)	Yes	2sig	OM1C	
PR	CTE non-unif	SR pan	-0,1	0,0	-0,2	0,0	-0,1	0,0	0	Yes(*)	Yes	2sig	OM1C	
PR	CTE non-unif	Fr st1	-0,2	0,8	-7,0	-6,9	0,3	0,0	0	Yes(*)	Yes	2sig	OM1C	
PR	CTE non-unif	Fr st2	-0,2	-0,8	-6,9	9,0	0,3	0,0	0	Yes(*)	Yes	2sig	OM1C	
PR	CTE non-unif	BBS	-0,2	0,0	7,7	0,0	-8,2	0,0	0	Yes(*)	Yes	2sig	OM1C	
PR	CTE non-unif	BTS	-0,2	0,0	6,9	0,0	-7,4	0,0	0	Yes(*)	Yes	2sig	OM1C	
PR	CTE non-unif	Sr st1	0,0	0,1	0,0	-0,1	0,0	0,0	0	Yes(*)	Yes	2sig	OM1C	
PR	CTE non-unif	SR st2	0,0	-0,1	0,0	0,1	0,0	0,0	0	Yes(*)	Yes	2sig	OM1C	
PR	CTE non-unif	Low st	-0,2	0,0	0,0	0,0	-0,4	0,0	0	Yes(*)	Yes	2sig	OM1C	
PR	CS IF load	C14	3,3	-0,5	-1,1	0,2	8,6	0,0	0	No	No	2sig	OM1C	
PR	Baffle IF load	C15	1,8	0,0	9,6	-0,1	-0,7	0,0	0	No	Yes	2sig	OM1C	
PR	FPU IF load	C16	3,9	0,0	-0,9	0,0	11,5	0,0	0	No	No	2sig	OM1C	
PR	PR, SR, JFET	C17	-0,7	0,0	0,0	0,0	-1,0	0,0	0	No	Yes	2sig	OM1C	
PR	Gravity release	C18	5,7	0,0	-11,5	0,0	20,0	0,0	0	No	No	2sig	OM1C	
PR	Moist release	Struc	-4,6	0,0	2,1	0,0	-9,3	0,0	0	No	No	2sig	OM1C	
PR	Moist release	refl	C20	-12,0	0,0	1,4	0,0	12,3	-13,2	0	Yes	No	2sig	OM1
PR	Alignment	C21	60,8	152,0	121,6	22,4	7,2	0,0	0	No	No	2sig	OM1C	
PR	CS planarity	E	C22	-0,6	0,0	-37,2	0,0	92,6	0,0	0	Yes(*)	Yes	2sig	OM1C
PR	CS planarity	N-E	C23	-31,7	53,6	1,6	-21,7	-48,2	0,0	0	Yes(*)	No	2sig	OM1C
PR	CS planarity	N-W	C24	4,2	-8,5	47,4	50,3	-4,1	0,0	0	Yes(*)	No	2sig	OM1C
PR	CS planarity	W	C25	0,4	0,0	-0,8	0,0	1,4	0,0	0	Yes(*)	No	2sig	OM1C
PR	CS planarity	S-W	C26	4,2	8,5	47,4	-50,3	-4,1	0,0	0	Yes(*)	No	2sig	OM1C
PR	CS planarity	S-E	C27	-31,7	-53,6	1,6	21,7	-48,2	0,0	0	Yes(*)	No	2sig	OM1C
PR	TTA	E	C28	-1,1	0,0	-8,1	0,0	18,7	0,0	0	Yes(*)	No	2sig	OM1C
PR	TTA	N-E	C29	-6,3	10,8	-0,2	-4,0	-7,8	0,0	0	Yes(*)	No	2sig	OM1C
PR	TTA	N-W	C30	0,3	-0,4	7,8	7,5	-1,7	0,0	0	Yes(*)	No	2sig	OM1C
PR	TTA	W	C31	0,1	0,0	0,2	0,0	0,2	0,0	0	Yes(*)	No	2sig	OM1C
PR	TTA	S-W	C32	0,3	0,4	7,8	-7,5	-1,7	0,0	0	Yes(*)	No	2sig	OM1C
PR	TTA	S-E	C33	-6,3	-10,8	-0,2	4,0	-7,8	0,0	0	Yes(*)	No	2sig	OM1C
PR	Structure launch	C34	20,0	20,0	20,0	20,0	20,0	0,0	0	No	No	2sig	OM1C	
PR	Structure creeping	C35	20,0	20,0	20,0	20,0	20,0	0,0	0	No	No	2sig	OM1C	
PR	Structure lifetime	C36	20,0	20,0	20,0	20,0	20,0	0,0	0	No	No	2sig	OM1C	
PR	dT in-orbit	Struc	C37	-6,3	0,8	-1,8	0,8	0,1	0,0	0	Yes(*)	No	2sig	OM1C
PR	dT in-orbit	refl	C38	7,0	0,0	1,6	0,0	-0,2	-9,0	-0	Yes(*)	No	2sig	OM1
PR	ISMA	Rad	C39	11,1	0,0	-0,6	0,0	-8,5	6,6	-0	Yes	No	2sig	OM1
PR	ISMA	Tang	C40	0,0	-1,4	0,0	0,0	0,0	0,0	0	Yes	No	2sig	OM1
PR	ISMA	Out-of-pl	C41	25,4	0,0	-73,0	0,0	0,0	0,8	-0	Yes	No	2sig	OM1
PR	ISMA	Rotation	C42	0,0	1,7	0,0	0,0	0,0	0,0	0	Yes	No	2sig	OM1
PR	ISM-B	Rad	C43	-11,1	0,0	-0,6	0,0	8,5	6,6	-0	Yes	No	2sig	OM1
PR	ISM-B	Tang	C44	0,0	-1,4	0,0	0,0	0,0	0,0	0	Yes	No	2sig	OM1
PR	ISM-B	Out-of-pl	C45	25,4	0,0	-73,0	0,0	0,0	0,8	-0	Yes	No	2sig	OM1
PR	ISM-B	Rotation	C46	0,0	0,9	0,0	0,0	0,0	0,0	0	Yes	No	2sig	OM1
PR	FEM acc	C47	1,0	1,0	1,0	1,0	1,0	1,0	0	No	No	2sig	OM1	

Table 7.4-18 Input parameters for the sensitivity analysis. Random case



SR	QM Videogram,		C48	52,0	0,0	55,2	0,0	175,7	0,0	0	No	Yes	2sig	OM2C
SR	QM T scaling		C2	6,9	0,0	4,7	0,0	31,6	0,0	0	Yes(*)	Yes	2sig	OM2C
SR	QM T know		C3	1,5	0,0	1,0	0,0	6,7	0,0	0	Yes(*)	Yes	2sig	OM2C
SR	CTE non-unif	Frame	C4	-5,1	0,0	3,4	0,0	23,6	0,0	0	Yes(*)	Yes	2sig	OM2C
SR	CTE non-unif	Pr pan	C5	-0,5	0,0	-0,8	0,0	-0,7	0,0	0	Yes(*)	Yes	2sig	OM2C
SR	CTE non-unif	SR pan	C6	1,4	0,0	-1,4	0,0	-5,2	0,0	0	Yes(*)	Yes	2sig	OM2C
SR	CTE non-unif	Fr st1	C7	0,0	0,0	0,0	0,0	0,0	0,0	0	Yes(*)	Yes	2sig	OM2C
SR	CTE non-unif	Fr st2	C8	0,0	0,0	0,0	0,0	0,0	0,0	0	Yes(*)	Yes	2sig	OM2C
SR	CTE non-unif	BBS	C9	0,0	0,0	-0,1	0,0	-0,1	0,0	0	Yes(*)	Yes	2sig	OM2C
SR	CTE non-unif	BTS	C10	1,0	0,9	-2,4	-9,9	-8,2	0,0	0	Yes(*)	Yes	2sig	OM2C
SR	CTE non-unif	Sr st1	C11	1,0	0,9	-2,4	-9,9	-8,2	0,0	0	Yes(*)	Yes	2sig	OM2C
SR	CTE non-unif	SR st2	C12	1,0	-0,9	-2,4	10,0	-8,2	0,0	0	Yes(*)	Yes	2sig	OM2C
SR	CTE non-unif	Low st	C13	0,0	0,0	0,1	0,0	0,1	0,0	0	Yes(*)	Yes	2sig	OM2C
SR	CS IF load		C49	12,1	0,1	4,0	0,3	-25,0	0,0	0	No	No	2sig	OM2C
SR	Baffle IF load		C50	-10,5	0,0	-18,6	0,1	7,9	0,0	0	No	No	2sig	OM2C
SR	FPU IF load		C51	0,5	0,0	1,4	0,0	0,6	0,0	0	No	No	2sig	OM2C
SR	PR, SR, JFET		C52	-0,5	0,0	-0,5	0,0	-0,4	0,0	0	No	Yes	2sig	OM2C
SR	Gravity release		C53	4,0	0,0	0,6	0,0	-8,5	0,0	0	No	No	2sig	OM2C
SR	Moist release	Struc	C54	1,5	0,0	0,5	0,0	-2,7	0,0	0	No	No	2sig	OM2C
SR	Moist release	ref	C55	6,5	0,0	-0,2	0,0	-11,0	1,4	0	Yes	No		OM2
SR	alignment		C56	65,9	152,0	70,0	22,4	10,0	0,0	0	No	Yes	2sig	OM2C
SR	CS planarity	E	C22	1,4	0,0	3,4	0,0	4,3	0,0	0	Yes(*)	No	2sig	OM2C
SR	CS planarity	N-E	C23	-2,0	-0,6	-2,0	-0,4	0,5	0,0	0	Yes(*)	No	2sig	OM2C
SR	CS planarity	N-W	C24	-10,7	-0,8	14,9	29,6	61,0	0,0	0	Yes(*)	No	2sig	OM2C
SR	CS planarity	W	C25	-46,9	0,0	36,1	0,0	-150,0	0,0	0	Yes(*)	No	2sig	OM2C
SR	CS planarity	S-W	C26	-10,7	0,8	14,9	-29,6	61,0	0,0	0	Yes(*)	No	2sig	OM2C
SR	CS planarity	S-E	C27	-2,0	0,6	-2,0	0,4	0,5	0,0	0	Yes(*)	No	2sig	OM2C
SR	TTA	E	C28	0,2	0,0	0,5	0,0	-0,4	0,0	0	Yes(*)	No	2sig	OM2C
SR	TTA	N-E	C29	0,0	0,1	0,6	0,8	1,2	0,0	0	Yes(*)	No	2sig	OM2C
SR	TTA	N-W	C30	-1,9	-0,6	2,5	4,1	9,4	0,0	0	Yes(*)	No	2sig	OM2C
SR	TTA	W	C31	-7,1	0,0	4,6	0,0	-21,0	0,0	0	Yes(*)	No	2sig	OM2C
SR	TTA	S-W	C32	-1,9	0,6	2,5	-4,1	9,4	0,0	0	Yes(*)	No	2sig	OM2C
SR	TTA	S-E	C33	0,0	-0,1	0,6	-0,8	1,2	0,0	0	Yes(*)	No	2sig	OM2C
SR	Structure launch		C57	20,0	20,0	20,0	20,0	20,0	0,0	0	No	No	2sig	OM2C
SR	Structure creeping		C58	20,0	20,0	20,0	20,0	20,0	0,0	0	No	No	2sig	OM2C
SR	Structure lifetime		C59	20,0	20,0	20,0	20,0	20,0	0,0	0	No	No	2sig	OM2C
SR	dT in-orbit	Struc	C37	8,5	-0,3	5,5	0,6	37,3	0,0	0	Yes(*)	No	2sig	OM2C
SR	dT in-orbit	refl	C38	-3,3	-0,1	-0,7	-0,2	-0,6	4,0	0	Yes(*)	No	2sig	OM2
SR	ISM-A	Rad	C60	-11,5	0,0	-1,5	0,0	-15,5	-2,0	0	Yes	No	2sig	OM2
SR	ISM-A	Tang	C61	0,0	-46,0	0,0	0,0	0,0	0,0	0	Yes	No	2sig	OM2
SR	ISM-A	Out-of-pl	C62	-34,0	0,0	60,0	0,0	0,0	0,3	-0	Yes	No	2sig	OM2
SR	ISM-A	Rotation	C63	0,0	6,0	0,0	0,0	0,0	0,0	0	Yes	No	2sig	OM2
SR	ISM-B	Rad	C64	11,5	0,0	-1,5	0,0	15,5	-2,0	0	Yes	No	2sig	OM2
SR	ISM-B	Tang	C65	0,0	-46,0	-0,1	0,0	0,0	0,0	0	Yes	No	2sig	OM2
SR	ISM-B	Out-of-pl	C66	-34,0	0,0	60,0	0,0	0,0	0,3	-0	Yes	No	2sig	OM2
SR	ISM-B	Rotation	C67	0,0	6,0	0,0	0,0	0,0	0,0	0	Yes	No	2sig	OM2
SR	FEM acc		C68	1,0	1,0	1,0	1,0	1,0	1,0	0	No	No	2sig	OM2

Table 7.4-19 Input parameters for sensitivity analysis: Random case



		case	Tx	Ty	Tz	Rx	Ry	dR	dK	Correlated?	Refocus ?	Nature	Rep
		n°	µm	µm	µm	µrad	µrad	µm					
PR	QM Videogram,	C1	48,0	0,0	168,0	0,0	69,1	0,0	0	No	Yes	2sig	OM1C
PR	QM T scaling	C2	-4,8	0,0	-2,7	0,0	0,1	0,0	0	Yes(*)	Yes	2sig	OM1C
PR	QM T know	C3	-1,0	0,0	-0,6	0,0	0,0	0,0	0	Yes(*)	Yes	2sig	OM1C

1 2 3 4 5 6 7 8 9 10 11

Table 7.4-20 Descriptions of the columns

- 1 : SR (secondary reflector), PR (primary reflector) or FPU (focal plane unit)
- 2 : sub load case name
- 3 : case identification CX
- 4 : translation variation: Tx, Ty, Tz
- 5 : rotation variation: Rx, Ry
- 6 : radius variation dR
- 7 : conicity variation dK
- 8 : correlation type : No, Yes, Yes (\*) :

No : means that the gain degradation of all individual variation and his opposite variation (translation, rotation, radius or conicity) have been computed. The total gain degradation is obtained by a RSS summation of individual degradation due to each variation (or his opposite variation if it constitute the worst case).

Yes : means that the gain degradation of the set of variations (translations, rotation, radius and conicity) and his opposite set) for the PR or the SR have been computed. The worst case between the set of variation and the opposite has been taken as gain degradation for this case.

Yes(\*) : means that the gain degradation of the set of variations (translations, rotations, radius and conicity) and his opposite set) the SR and PR have been computed. The worst case between the set of variation and the opposite has been taken as gain degradation for this case.

9 : Refocus compensation. Random decentring cases are with (Yes) or without refocus (No). As the RF routine is without refocus, the magnitude of the refocus cases has been decreased to take into account the sensitivity difference.

- 10 : Error type
- 11 : Coordinate system ( OM1, OM2, OM1C, OM2C, ORDP)





detector n°	case1	case2	case3	case4	case5	case6	case7	case8	case9	case10
	dB	dB	dB	dB	dB	dB	dB	dB	dB	dB
lfi 70 18	0.0036	0.0006	0.0002	0.0004	0.0006	0.0003	0.0003	0.0003	0.0001	0.0003
lfi 70 19	0.0036	0.0008	0.0002	0.0014	0.0010	0.0003	0.0007	0.0006	0.0004	0.0014
lfi 70 20	0.0071	0.0013	0.0002	0.0025	0.0021	0.0006	0.0007	0.0003	0.0008	0.0016
lfi 70 21	0.0071	0.0013	0.0002	0.0025	0.0021	0.0006	0.0002	0.0008	0.0008	0.0012
lfi 70 22	0.0036	0.0008	0.0002	0.0014	0.0010	0.0003	0.0004	0.0009	0.0004	0.0005
lfi 70 23	0.0036	0.0006	0.0002	0.0004	0.0006	0.0003	0.0002	0.0004	0.0001	0.0005
lfi 44 24	0.0052	0.0005	0.0001	0.0013	0.0010	0.0003	0.0003	0.0004	0.0002	0.0004
lfi 44 25	0.0039	0.0004	0.0001	0.0002	0.0006	0.0000	0.0007	0.0006	0.0004	0.0005
lfi 44 26	0.0039	0.0004	0.0001	0.0003	0.0006	0.0000	0.0004	0.0009	0.0004	0.0012
lfi 30 27	0.0030	0.0006	0.0001	0.0009	0.0006	0.0002	0.0001	0.0002	0.0003	0.0004
lfi 30 28	0.0030	0.0006	0.0001	0.0009	0.0006	0.0002	0.0002	0.0001	0.0003	0.0006
hfi 100 1	0.0030	0.0022	0.0004	0.0011	0.0015	0.0008	0.0012	0.0020	0.0017	0.0007
hfi 100 2	0.0083	0.0031	0.0005	0.0032	0.0035	0.0012	0.0017	0.0012	0.0019	0.0050
hfi 100 3	0.0083	0.0031	0.0005	0.0032	0.0035	0.0012	0.0007	0.0021	0.0019	0.0027
hfi 100 4	0.0030	0.0022	0.0004	0.0011	0.0015	0.0008	0.0015	0.0017	0.0017	0.0038
hfi 143 1	0.0035	0.0015	0.0005	0.0009	0.0006	0.0010	0.0021	0.0025	0.0015	0.0033
hfi 143 2	0.0066	0.0028	0.0008	0.0038	0.0032	0.0014	0.0009	0.0009	0.0018	0.0026
hfi 143 3	0.0056	0.0003	0.0003	0.0020	0.0007	0.0006	0.0004	0.0006	0.0013	0.0003
hfi 143 4	0.0035	0.0015	0.0005	0.0009	0.0006	0.0010	0.0021	0.0025	0.0015	0.0033
hfi 143 5	0.0090	0.0009	0.0001	0.0025	0.0014	0.0002	0.0004	0.0004	0.0006	0.0013
hfi 143 6	0.0153	0.0010	0.0002	0.0037	0.0025	0.0002	0.0009	0.0008	0.0007	0.0016
hfi 143 7	0.0146	0.0005	0.0001	0.0032	0.0018	0.0002	0.0005	0.0012	0.0006	0.0006
hfi 143 8	0.0092	0.0025	0.0005	0.0025	0.0028	0.0012	0.0005	0.0003	0.0018	0.0027
hfi 217 1	0.0114	0.0027	0.0009	0.0023	0.0026	0.0016	0.0020	0.0021	0.0024	0.0048
hfi 217 2	0.0099	0.0012	0.0006	0.0030	0.0021	0.0012	0.0007	0.0024	0.0006	0.0021
hfi 217 3	0.0102	0.0008	0.0005	0.0028	0.0019	0.0011	0.0018	0.0015	0.0004	0.0003
hfi 217 4	0.0120	0.0023	0.0009	0.0016	0.0022	0.0014	0.0015	0.0020	0.0020	0.0031
hfi 217 5	0.0200	0.0008	0.0006	0.0018	0.0024	0.0012	0.0007	0.0004	0.0007	0.0015
hfi 217 6	0.0120	0.0018	0.0005	0.0014	0.0012	0.0012	0.0008	0.0008	0.0023	0.0006
hfi 217 7	0.0102	0.0006	0.0006	0.0018	0.0008	0.0013	0.0005	0.0015	0.0007	0.0017
hfi 217 8	0.0197	0.0006	0.0006	0.0007	0.0014	0.0015	0.0016	0.0017	0.0020	0.0009
hfi 353 1	0.0838	0.0022	0.0014	0.0090	0.0083	0.0027	0.0036	0.0027	0.0021	0.0040
hfi 353 2	0.0559	0.0023	0.0008	0.0034	0.0045	0.0019	0.0036	0.0029	0.0017	0.0032
hfi 353 3	0.0415	0.0014	0.0008	0.0010	0.0013	0.0015	0.0022	0.0014	0.0012	0.0012
hfi 353 4	0.0357	0.0009	0.0007	0.0023	0.0005	0.0019	0.0020	0.0013	0.0023	0.0018
hfi 353 5	0.0328	0.0018	0.0008	0.0015	0.0010	0.0013	0.0028	0.0027	0.0028	0.0037
hfi 353 6	0.0430	0.0011	0.0008	0.0014	0.0012	0.0013	0.0034	0.0029	0.0006	0.0025
hfi 353 7	0.0612	0.0010	0.0012	0.0050	0.0043	0.0019	0.0032	0.0032	0.0011	0.0007
hfi 353 8	0.0842	0.0033	0.0004	0.0074	0.0090	0.0017	0.0021	0.0032	0.0020	0.0040
hfi 545 1	0.1421	0.0046	0.0014	0.0144	0.0152	0.0044	0.0091	0.0019	0.0030	0.0107
hfi 545 2	0.1164	0.0021	0.0007	0.0055	0.0073	0.0024	0.0078	0.0006	0.0015	0.0041
hfi 545 3	0.1234	0.0020	0.0008	0.0072	0.0076	0.0015	0.0013	0.0073	0.0007	0.0026
hfi 545 4	0.1405	0.0050	0.0019	0.0139	0.0154	0.0046	0.0015	0.0098	0.0032	0.0021
hfi 857 1	0.1937	0.0014	0.0007	0.0011	0.0004	0.0005	0.0100	0.0031	0.0068	0.0032
hfi 857 2	0.1643	0.0023	0.0017	0.0088	0.0064	0.0033	0.0067	0.0039	0.0086	0.0097
hfi 857 3	0.1706	0.0020	0.0006	0.0083	0.0048	0.0031	0.0058	0.0095	0.0079	0.0120
hfi 857 4	0.2025	0.0013	0.0010	0.0005	0.0035	0.0006	0.0042	0.0135	0.0058	0.0098

Table 7.4-21 random case (1 to 10)



detector n°	case11	case12	case13	case14	case15	case16	case17	case18	case19	case20
	dB	dB	dB	dB	dB	dB	dB	dB	dB	dB
lfi_70_18	0.0006	0.0001	0.0000	0.0001	0.0001	0.0003	0.0000	0.0009	0.0001	0.0004
lfi_70_19	0.0010	0.0004	0.0000	0.0006	0.0002	0.0008	0.0001	0.0013	0.0006	0.0004
lfi_70_20	0.0011	0.0004	0.0001	0.0013	0.0005	0.0017	0.0001	0.0021	0.0014	0.0000
lfi_70_21	0.0006	0.0009	0.0001	0.0013	0.0005	0.0017	0.0001	0.0021	0.0014	0.0000
lfi_70_22	0.0002	0.0009	0.0000	0.0006	0.0002	0.0008	0.0001	0.0013	0.0006	0.0004
lfi_70_23	0.0000	0.0005	0.0000	0.0001	0.0001	0.0003	0.0000	0.0009	0.0001	0.0004
lfi_44_24	0.0004	0.0003	0.0000	0.0005	0.0003	0.0007	0.0001	0.0014	0.0005	0.0005
lfi_44_25	0.0007	0.0008	0.0000	0.0003	0.0002	0.0004	0.0000	0.0008	0.0003	0.0005
lfi_44_26	0.0008	0.0007	0.0000	0.0003	0.0002	0.0004	0.0000	0.0008	0.0003	0.0005
lfi_30_27	0.0002	0.0003	0.0000	0.0004	0.0002	0.0005	0.0001	0.0008	0.0004	0.0003
lfi_30_28	0.0004	0.0001	0.0000	0.0004	0.0002	0.0005	0.0001	0.0008	0.0004	0.0003
hfi_100_1	0.0009	0.0024	0.0001	0.0022	0.0004	0.0020	0.0002	0.0015	0.0024	0.0018
hfi_100_2	0.0030	0.0005	0.0001	0.0028	0.0008	0.0036	0.0003	0.0029	0.0031	0.0013
hfi_100_3	0.0006	0.0025	0.0001	0.0028	0.0008	0.0036	0.0003	0.0029	0.0031	0.0013
hfi_100_4	0.0027	0.0011	0.0001	0.0022	0.0004	0.0020	0.0002	0.0015	0.0024	0.0018
hfi_143_1	0.0036	0.0016	0.0001	0.0016	0.0004	0.0008	0.0002	0.0009	0.0014	0.0006
hfi_143_2	0.0015	0.0008	0.0002	0.0024	0.0009	0.0029	0.0004	0.0036	0.0026	0.0020
hfi_143_3	0.0012	0.0009	0.0001	0.0009	0.0003	0.0003	0.0001	0.0019	0.0007	0.0007
hfi_143_4	0.0036	0.0016	0.0001	0.0016	0.0004	0.0008	0.0002	0.0009	0.0014	0.0006
hfi_143_5	0.0007	0.0008	0.0000	0.0009	0.0001	0.0008	0.0000	0.0028	0.0010	0.0015
hfi_143_6	0.0010	0.0012	0.0000	0.0005	0.0003	0.0015	0.0001	0.0039	0.0008	0.0003
hfi_143_7	0.0011	0.0010	0.0000	0.0006	0.0004	0.0010	0.0000	0.0034	0.0007	0.0006
hfi_143_8	0.0017	0.0011	0.0001	0.0026	0.0008	0.0027	0.0003	0.0023	0.0029	0.0005
hfi_217_1	0.0039	0.0026	0.0002	0.0024	0.0008	0.0027	0.0004	0.0021	0.0026	0.0015
hfi_217_2	0.0010	0.0027	0.0001	0.0007	0.0010	0.0015	0.0003	0.0028	0.0010	0.0003
hfi_217_3	0.0029	0.0012	0.0001	0.0004	0.0009	0.0012	0.0003	0.0027	0.0006	0.0003
hfi_217_4	0.0020	0.0031	0.0002	0.0019	0.0005	0.0023	0.0004	0.0018	0.0020	0.0010
hfi_217_5	0.0008	0.0012	0.0001	0.0008	0.0003	0.0018	0.0002	0.0032	0.0011	0.0004
hfi_217_6	0.0009	0.0014	0.0001	0.0019	0.0002	0.0009	0.0002	0.0010	0.0017	0.0017
hfi_217_7	0.0008	0.0014	0.0001	0.0009	0.0011	0.0006	0.0003	0.0018	0.0009	0.0002
hfi_217_8	0.0018	0.0015	0.0002	0.0020	0.0014	0.0015	0.0004	0.0025	0.0019	0.0008
hfi_353_1	0.0035	0.0016	0.0005	0.0052	0.0049	0.0061	0.0010	0.0133	0.0057	0.0021
hfi_353_2	0.0037	0.0025	0.0001	0.0039	0.0030	0.0042	0.0002	0.0079	0.0041	0.0023
hfi_353_3	0.0010	0.0020	0.0001	0.0014	0.0015	0.0020	0.0003	0.0024	0.0019	0.0034
hfi_353_4	0.0023	0.0027	0.0001	0.0014	0.0013	0.0011	0.0003	0.0027	0.0019	0.0032
hfi_353_5	0.0028	0.0025	0.0002	0.0017	0.0024	0.0012	0.0005	0.0033	0.0018	0.0015
hfi_353_6	0.0013	0.0016	0.0002	0.0008	0.0029	0.0010	0.0005	0.0044	0.0010	0.0021
hfi_353_7	0.0019	0.0013	0.0004	0.0033	0.0040	0.0031	0.0008	0.0084	0.0035	0.0020
hfi_353_8	0.0014	0.0013	0.0002	0.0055	0.0033	0.0073	0.0003	0.0120	0.0060	0.0037
hfi_545_1	0.0099	0.0042	0.0003	0.0084	0.0074	0.0113	0.0009	0.0209	0.0089	0.0038
hfi_545_2	0.0044	0.0030	0.0003	0.0038	0.0060	0.0053	0.0005	0.0114	0.0042	0.0064
hfi_545_3	0.0009	0.0032	0.0002	0.0047	0.0055	0.0056	0.0002	0.0121	0.0049	0.0058
hfi_545_4	0.0012	0.0069	0.0007	0.0084	0.0079	0.0118	0.0014	0.0213	0.0091	0.0036
hfi_857_1	0.0028	0.0043	0.0003	0.0029	0.0097	0.0031	0.0006	0.0125	0.0038	0.0131
hfi_857_2	0.0024	0.0048	0.0005	0.0051	0.0088	0.0051	0.0012	0.0131	0.0063	0.0126
hfi_857_3	0.0048	0.0018	0.0003	0.0030	0.0084	0.0037	0.0006	0.0112	0.0044	0.0134
hfi_857_4	0.0045	0.0040	0.0006	0.0035	0.0109	0.0037	0.0009	0.0143	0.0045	0.0142

Table 7.4-22 random case (11 to 20)



detector n°	case21 dB	case22 dB	case23 dB	case24 dB	case25 dB	case26 dB	case27 dB	case28 dB	case29 dB	case30 dB
lfi 70 18	0.0120	0.0041	0.0051	0.0029	0.0008	0.0054	0.0003	0.0007	0.0007	0.0007
lfi 70 19	0.0118	0.0015	0.0006	0.0062	0.0031	0.0019	0.0042	0.0010	0.0001	0.0015
lfi 70 20	0.0081	0.0041	0.0035	0.0057	0.0049	0.0022	0.0058	0.0020	0.0013	0.0015
lfi 70 21	0.0081	0.0041	0.0058	0.0016	0.0049	0.0062	0.0035	0.0020	0.0019	0.0009
lfi 70 22	0.0118	0.0015	0.0042	0.0023	0.0031	0.0060	0.0006	0.0010	0.0013	0.0003
lfi 70 23	0.0120	0.0041	0.0003	0.0052	0.0008	0.0025	0.0051	0.0007	0.0005	0.0004
lfi 44 24	0.0057	0.0035	0.0043	0.0040	0.0063	0.0047	0.0043	0.0008	0.0006	0.0007
lfi 44 25	0.0166	0.0037	0.0067	0.0081	0.0034	0.0064	0.0004	0.0008	0.0012	0.0012
lfi 44 26	0.0166	0.0037	0.0004	0.0061	0.0034	0.0076	0.0067	0.0008	0.0003	0.0009
lfi 30 27	0.0057	0.0007	0.0021	0.0019	0.0033	0.0048	0.0011	0.0005	0.0007	0.0003
lfi 30 28	0.0057	0.0007	0.0011	0.0048	0.0033	0.0018	0.0021	0.0005	0.0003	0.0005
hfi 100 1	0.0160	0.0012	0.0060	0.0104	0.0052	0.0043	0.0034	0.0017	0.0034	0.0017
hfi 100 2	0.0092	0.0041	0.0052	0.0073	0.0053	0.0020	0.0096	0.0023	0.0029	0.0044
hfi 100 3	0.0092	0.0041	0.0096	0.0011	0.0053	0.0081	0.0052	0.0023	0.0040	0.0009
hfi 100 4	0.0160	0.0012	0.0034	0.0039	0.0052	0.0095	0.0060	0.0017	0.0016	0.0037
hfi 143 1	0.0225	0.0001	0.0076	0.0085	0.0023	0.0069	0.0053	0.0004	0.0006	0.0043
hfi 143 2	0.0107	0.0068	0.0068	0.0016	0.0064	0.0083	0.0042	0.0031	0.0029	0.0016
hfi 143 3	0.0112	0.0043	0.0044	0.0090	0.0054	0.0031	0.0068	0.0011	0.0006	0.0018
hfi 143 4	0.0225	0.0001	0.0076	0.0085	0.0023	0.0069	0.0053	0.0004	0.0006	0.0043
hfi 143 5	0.0258	0.0079	0.0126	0.0031	0.0077	0.0159	0.0045	0.0015	0.0015	0.0008
hfi 143 6	0.0152	0.0114	0.0116	0.0069	0.0105	0.0130	0.0109	0.0025	0.0012	0.0020
hfi 143 7	0.0150	0.0109	0.0113	0.0120	0.0108	0.0085	0.0120	0.0019	0.0011	0.0015
hfi 143 8	0.0256	0.0090	0.0029	0.0157	0.0068	0.0016	0.0110	0.0020	0.0025	0.0027
hfi 217 1	0.0232	0.0014	0.0074	0.0072	0.0038	0.0092	0.0071	0.0020	0.0038	0.0043
hfi 217 2	0.0116	0.0075	0.0041	0.0094	0.0033	0.0028	0.0081	0.0024	0.0008	0.0019
hfi 217 3	0.0118	0.0082	0.0088	0.0022	0.0034	0.0091	0.0046	0.0022	0.0014	0.0033
hfi 217 4	0.0227	0.0009	0.0059	0.0095	0.0038	0.0066	0.0068	0.0018	0.0032	0.0030
hfi 217 5	0.0167	0.0081	0.0090	0.0026	0.0058	0.0091	0.0054	0.0022	0.0011	0.0013
hfi 217 6	0.0094	0.0019	0.0007	0.0020	0.0018	0.0014	0.0018	0.0020	0.0021	0.0013
hfi 217 7	0.0105	0.0030	0.0021	0.0025	0.0017	0.0023	0.0012	0.0012	0.0009	0.0018
hfi 217 8	0.0182	0.0069	0.0047	0.0103	0.0065	0.0031	0.0078	0.0007	0.0020	0.0030
hfi 353 1	0.0577	0.0370	0.0332	0.0418	0.0405	0.0313	0.0390	0.0072	0.0060	0.0073
hfi 353 2	0.0396	0.0146	0.0140	0.0207	0.0241	0.0172	0.0172	0.0027	0.0032	0.0057
hfi 353 3	0.0281	0.0021	0.0016	0.0093	0.0169	0.0097	0.0028	0.0010	0.0012	0.0012
hfi 353 4	0.0243	0.0094	0.0076	0.0047	0.0134	0.0050	0.0071	0.0022	0.0014	0.0014
hfi 353 5	0.0239	0.0083	0.0044	0.0039	0.0115	0.0042	0.0052	0.0014	0.0027	0.0028
hfi 353 6	0.0300	0.0031	0.0074	0.0113	0.0191	0.0130	0.0057	0.0010	0.0005	0.0014
hfi 353 7	0.0419	0.0183	0.0209	0.0193	0.0291	0.0262	0.0176	0.0039	0.0029	0.0030
hfi 353 8	0.0597	0.0360	0.0382	0.0277	0.0405	0.0438	0.0319	0.0058	0.0072	0.0035
hfi 545 1	0.1396	0.0565	0.0356	0.0976	0.0727	0.0277	0.0781	0.0107	0.0062	0.0168
hfi 545 2	0.1102	0.0185	0.0069	0.0660	0.0582	0.0131	0.0395	0.0031	0.0015	0.0110
hfi 545 3	0.1165	0.0253	0.0446	0.0146	0.0632	0.0730	0.0130	0.0053	0.0098	0.0026
hfi 545 4	0.1407	0.0559	0.0771	0.0196	0.0718	0.1024	0.0350	0.0108	0.0155	0.0032
hfi 857 1	0.1624	0.0288	0.0309	0.0749	0.0946	0.0140	0.0101	0.0054	0.0060	0.0118
hfi 857 2	0.1222	0.0575	0.0464	0.0374	0.0743	0.0115	0.0360	0.0119	0.0085	0.0049
hfi 857 3	0.1302	0.0554	0.0313	0.0189	0.0780	0.0396	0.0466	0.0115	0.0044	0.0022
hfi 857 4	0.1763	0.0187	0.0226	0.0174	0.1019	0.0854	0.0250	0.0045	0.0073	0.0035

Table 7.4-23 random case (21 to 30)



detector n°	case31	case32	case33	case34	case35	case36	case37	case38	case39	case40
	dB	dB	dB	dB	dB	dB	dB	dB	dB	dB
lfi 70 18	0.0007	0.0004	0.0005	0.0020	0.0020	0.0020	0.0007	0.0004	0.0004	0.0001
lfi 70 19	0.0007	0.0003	0.0013	0.0031	0.0031	0.0031	0.0011	0.0001	0.0001	0.0001
lfi 70 20	0.0011	0.0009	0.0019	0.0032	0.0032	0.0032	0.0017	0.0003	0.0003	0.0001
lfi 70 21	0.0011	0.0015	0.0013	0.0032	0.0032	0.0032	0.0014	0.0003	0.0003	0.0001
lfi 70 22	0.0007	0.0015	0.0001	0.0031	0.0031	0.0031	0.0007	0.0001	0.0001	0.0001
lfi 70 23	0.0007	0.0007	0.0007	0.0020	0.0020	0.0020	0.0006	0.0004	0.0004	0.0001
lfi 44 24	0.0006	0.0007	0.0006	0.0018	0.0018	0.0018	0.0006	0.0001	0.0001	0.0000
lfi 44 25	0.0005	0.0009	0.0003	0.0031	0.0031	0.0031	0.0008	0.0004	0.0004	0.0001
lfi 44 26	0.0005	0.0012	0.0012	0.0031	0.0031	0.0031	0.0003	0.0004	0.0004	0.0001
lfi 30 27	0.0006	0.0005	0.0003	0.0012	0.0012	0.0012	0.0006	0.0002	0.0002	0.0000
lfi 30 28	0.0006	0.0003	0.0007	0.0012	0.0012	0.0012	0.0007	0.0002	0.0002	0.0000
hfi 100 1	0.0010	0.0037	0.0016	0.0053	0.0053	0.0053	0.0013	0.0010	0.0010	0.0002
hfi 100 2	0.0021	0.0009	0.0040	0.0054	0.0054	0.0054	0.0040	0.0014	0.0014	0.0002
hfi 100 3	0.0021	0.0044	0.0029	0.0054	0.0054	0.0054	0.0034	0.0014	0.0014	0.0002
hfi 100 4	0.0010	0.0017	0.0034	0.0053	0.0053	0.0053	0.0022	0.0010	0.0010	0.0002
hfi 143 1	0.0019	0.0021	0.0027	0.0058	0.0058	0.0058	0.0018	0.0013	0.0013	0.0003
hfi 143 2	0.0022	0.0014	0.0024	0.0053	0.0053	0.0053	0.0030	0.0009	0.0009	0.0000
hfi 143 3	0.0011	0.0018	0.0002	0.0036	0.0036	0.0036	0.0004	0.0009	0.0009	0.0000
hfi 143 4	0.0019	0.0021	0.0027	0.0058	0.0058	0.0058	0.0018	0.0013	0.0013	0.0003
hfi 143 5	0.0006	0.0008	0.0016	0.0050	0.0050	0.0050	0.0008	0.0005	0.0005	0.0001
hfi 143 6	0.0004	0.0012	0.0012	0.0045	0.0045	0.0045	0.0016	0.0008	0.0008	0.0000
hfi 143 7	0.0006	0.0021	0.0011	0.0041	0.0041	0.0041	0.0007	0.0006	0.0006	0.0000
hfi 143 8	0.0022	0.0012	0.0040	0.0062	0.0062	0.0062	0.0023	0.0011	0.0011	0.0001
hfi 217 1	0.0018	0.0041	0.0038	0.0059	0.0059	0.0059	0.0034	0.0022	0.0022	0.0004
hfi 217 2	0.0009	0.0029	0.0017	0.0049	0.0049	0.0049	0.0018	0.0018	0.0018	0.0001
hfi 217 3	0.0011	0.0022	0.0004	0.0048	0.0048	0.0048	0.0009	0.0016	0.0016	0.0001
hfi 217 4	0.0014	0.0036	0.0031	0.0048	0.0048	0.0048	0.0022	0.0014	0.0014	0.0004
hfi 217 5	0.0005	0.0016	0.0013	0.0043	0.0043	0.0043	0.0010	0.0006	0.0006	0.0001
hfi 217 6	0.0019	0.0013	0.0013	0.0037	0.0037	0.0037	0.0009	0.0014	0.0014	0.0002
hfi 217 7	0.0012	0.0017	0.0004	0.0035	0.0035	0.0035	0.0013	0.0014	0.0014	0.0001
hfi 217 8	0.0025	0.0022	0.0017	0.0056	0.0056	0.0056	0.0004	0.0011	0.0011	0.0001
hfi 353 1	0.0055	0.0045	0.0059	0.0164	0.0164	0.0164	0.0025	0.0019	0.0019	0.0001
hfi 353 2	0.0045	0.0052	0.0053	0.0104	0.0104	0.0104	0.0029	0.0031	0.0031	0.0003
hfi 353 3	0.0018	0.0022	0.0024	0.0041	0.0041	0.0041	0.0014	0.0012	0.0012	0.0002
hfi 353 4	0.0018	0.0022	0.0016	0.0048	0.0048	0.0048	0.0008	0.0006	0.0006	0.0002
hfi 353 5	0.0029	0.0033	0.0016	0.0061	0.0061	0.0061	0.0005	0.0032	0.0032	0.0003
hfi 353 6	0.0023	0.0031	0.0007	0.0062	0.0062	0.0062	0.0004	0.0019	0.0019	0.0001
hfi 353 7	0.0042	0.0049	0.0035	0.0106	0.0106	0.0106	0.0014	0.0024	0.0024	0.0001
hfi 353 8	0.0052	0.0066	0.0066	0.0159	0.0159	0.0159	0.0044	0.0016	0.0016	0.0000
hfi 545 1	0.0103	0.0033	0.0155	0.0325	0.0325	0.0325	0.0073	0.0035	0.0035	0.0011
hfi 545 2	0.0079	0.0013	0.0079	0.0213	0.0213	0.0213	0.0039	0.0029	0.0029	0.0003
hfi 545 3	0.0086	0.0122	0.0011	0.0216	0.0216	0.0216	0.0015	0.0038	0.0038	0.0010
hfi 545 4	0.0100	0.0167	0.0053	0.0326	0.0326	0.0326	0.0047	0.0037	0.0037	0.0010
hfi 857 1	0.0105	0.0015	0.0053	0.0275	0.0275	0.0275	0.0045	0.0082	0.0082	0.0014
hfi 857 2	0.0089	0.0025	0.0055	0.0229	0.0229	0.0229	0.0015	0.0092	0.0092	0.0008
hfi 857 3	0.0095	0.0059	0.0087	0.0221	0.0221	0.0221	0.0011	0.0089	0.0089	0.0009
hfi 857 4	0.0131	0.0154	0.0059	0.0293	0.0293	0.0293	0.0037	0.0092	0.0092	0.0008

Table 7.4-24 random case (31 to 40)



detector n°	case41	case42	case43	case44	case45	case46	case47	case48	case49	case50
	dB	dB	dB	dB	dB	dB	dB	dB	dB	dB
lfi_70_18	0.0015	0.0001	0.0005	0.0001	0.0015	0.0001	0.0001	0.0022	0.0005	0.0005
lfi_70_19	0.0023	0.0002	0.0001	0.0001	0.0023	0.0001	0.0001	0.0057	0.0015	0.0009
lfi_70_20	0.0039	0.0001	0.0002	0.0001	0.0039	0.0001	0.0001	0.0091	0.0027	0.0015
lfi_70_21	0.0039	0.0001	0.0002	0.0001	0.0039	0.0001	0.0001	0.0091	0.0027	0.0015
lfi_70_22	0.0023	0.0002	0.0001	0.0001	0.0023	0.0001	0.0001	0.0057	0.0015	0.0009
lfi_70_23	0.0015	0.0001	0.0005	0.0001	0.0015	0.0001	0.0001	0.0022	0.0005	0.0005
lfi_44_24	0.0037	0.0000	0.0002	0.0000	0.0037	0.0000	0.0001	0.0088	0.0014	0.0009
lfi_44_25	0.0008	0.0002	0.0004	0.0001	0.0008	0.0001	0.0001	0.0032	0.0005	0.0008
lfi_44_26	0.0008	0.0002	0.0004	0.0001	0.0008	0.0001	0.0001	0.0032	0.0005	0.0008
lfi_30_27	0.0017	0.0000	0.0002	0.0000	0.0017	0.0000	0.0000	0.0041	0.0010	0.0007
lfi_30_28	0.0017	0.0000	0.0002	0.0000	0.0017	0.0000	0.0000	0.0041	0.0010	0.0007
hfi_100_1	0.0018	0.0003	0.0010	0.0002	0.0018	0.0002	0.0003	0.0073	0.0022	0.0019
hfi_100_2	0.0047	0.0002	0.0012	0.0002	0.0047	0.0001	0.0003	0.0096	0.0048	0.0030
hfi_100_3	0.0047	0.0002	0.0012	0.0002	0.0047	0.0001	0.0003	0.0096	0.0048	0.0030
hfi_100_4	0.0018	0.0003	0.0010	0.0002	0.0018	0.0002	0.0003	0.0073	0.0022	0.0019
hfi_143_1	0.0025	0.0004	0.0011	0.0003	0.0025	0.0002	0.0003	0.0042	0.0021	0.0024
hfi_143_2	0.0039	0.0000	0.0008	0.0000	0.0039	0.0000	0.0003	0.0110	0.0045	0.0030
hfi_143_3	0.0047	0.0001	0.0010	0.0000	0.0047	0.0000	0.0001	0.0107	0.0014	0.0011
hfi_143_4	0.0025	0.0004	0.0011	0.0003	0.0025	0.0002	0.0003	0.0042	0.0021	0.0024
hfi_143_5	0.0064	0.0001	0.0006	0.0001	0.0064	0.0001	0.0001	0.0138	0.0020	0.0008
hfi_143_6	0.0094	0.0001	0.0009	0.0000	0.0094	0.0000	0.0001	0.0204	0.0032	0.0012
hfi_143_7	0.0098	0.0001	0.0008	0.0000	0.0098	0.0000	0.0001	0.0201	0.0026	0.0013
hfi_143_8	0.0046	0.0001	0.0008	0.0001	0.0046	0.0001	0.0002	0.0149	0.0041	0.0031
hfi_217_1	0.0035	0.0005	0.0020	0.0004	0.0035	0.0003	0.0006	0.0053	0.0034	0.0030
hfi_217_2	0.0007	0.0001	0.0018	0.0001	0.0007	0.0001	0.0003	0.0106	0.0025	0.0016
hfi_217_3	0.0009	0.0002	0.0017	0.0001	0.0009	0.0001	0.0002	0.0108	0.0021	0.0015
hfi_217_4	0.0036	0.0004	0.0012	0.0004	0.0036	0.0003	0.0006	0.0049	0.0028	0.0027
hfi_217_5	0.0074	0.0001	0.0009	0.0001	0.0074	0.0001	0.0003	0.0089	0.0019	0.0017
hfi_217_6	0.0024	0.0002	0.0012	0.0002	0.0024	0.0001	0.0003	0.0062	0.0026	0.0031
hfi_217_7	0.0032	0.0002	0.0014	0.0001	0.0032	0.0001	0.0003	0.0051	0.0013	0.0017
hfi_217_8	0.0085	0.0002	0.0010	0.0001	0.0085	0.0001	0.0004	0.0101	0.0019	0.0029
hfi_353_1	0.0377	0.0001	0.0018	0.0001	0.0377	0.0000	0.0008	0.0661	0.0099	0.0094
hfi_353_2	0.0231	0.0004	0.0027	0.0003	0.0231	0.0002	0.0006	0.0344	0.0055	0.0068
hfi_353_3	0.0150	0.0002	0.0008	0.0002	0.0150	0.0001	0.0004	0.0174	0.0018	0.0045
hfi_353_4	0.0101	0.0002	0.0003	0.0002	0.0101	0.0001	0.0004	0.0138	0.0012	0.0045
hfi_353_5	0.0088	0.0003	0.0032	0.0003	0.0088	0.0002	0.0006	0.0144	0.0023	0.0050
hfi_353_6	0.0156	0.0001	0.0018	0.0001	0.0156	0.0001	0.0004	0.0210	0.0020	0.0052
hfi_353_7	0.0257	0.0001	0.0020	0.0001	0.0257	0.0001	0.0006	0.0405	0.0057	0.0072
hfi_353_8	0.0391	0.0001	0.0019	0.0000	0.0391	0.0000	0.0005	0.0665	0.0103	0.0091
hfi_545_1	0.0657	0.0013	0.0034	0.0011	0.0657	0.0007	0.0014	0.1127	0.0182	0.0167
hfi_545_2	0.0472	0.0004	0.0020	0.0003	0.0472	0.0002	0.0008	0.0703	0.0102	0.0145
hfi_545_3	0.0520	0.0012	0.0031	0.0010	0.0520	0.0007	0.0013	0.0790	0.0105	0.0142
hfi_545_4	0.0648	0.0012	0.0033	0.0010	0.0648	0.0007	0.0015	0.1127	0.0178	0.0164
hfi_857_1	0.0650	0.0017	0.0080	0.0014	0.0650	0.0010	0.0023	0.0931	0.0086	0.0246
hfi_857_2	0.0424	0.0010	0.0085	0.0008	0.0424	0.0006	0.0020	0.0737	0.0077	0.0227
hfi_857_3	0.0469	0.0011	0.0085	0.0009	0.0469	0.0006	0.0017	0.0780	0.0066	0.0241
hfi_857_4	0.0707	0.0012	0.0080	0.0008	0.0707	0.0004	0.0016	0.1024	0.0111	0.0273

Table 7.4-25 random case (41 to 50)



detector n°	case51	case52	case53	case54	case55	case56	case57	case58	case59	case60
	dB	dB	dB	dB	dB	dB	dB	dB	dB	dB
lfi_70_18	0.0000	0.0000	0.0004	0.0001	0.0002	0.0113	0.0014	0.0014	0.0014	0.0002
lfi_70_19	0.0001	0.0000	0.0005	0.0002	0.0005	0.0113	0.0030	0.0030	0.0030	0.0002
lfi_70_20	0.0001	0.0001	0.0008	0.0003	0.0011	0.0076	0.0034	0.0034	0.0034	0.0004
lfi_70_21	0.0001	0.0001	0.0008	0.0003	0.0011	0.0076	0.0034	0.0034	0.0034	0.0004
lfi_70_22	0.0001	0.0000	0.0005	0.0002	0.0005	0.0113	0.0030	0.0030	0.0030	0.0002
lfi_70_23	0.0000	0.0000	0.0004	0.0001	0.0002	0.0113	0.0014	0.0014	0.0014	0.0002
lfi_44_24	0.0001	0.0000	0.0004	0.0001	0.0004	0.0066	0.0017	0.0017	0.0017	0.0002
lfi_44_25	0.0001	0.0000	0.0001	0.0000	0.0003	0.0187	0.0029	0.0029	0.0029	0.0003
lfi_44_26	0.0001	0.0000	0.0001	0.0000	0.0003	0.0187	0.0029	0.0029	0.0029	0.0003
lfi_30_27	0.0000	0.0000	0.0004	0.0001	0.0004	0.0048	0.0013	0.0013	0.0013	0.0001
lfi_30_28	0.0000	0.0000	0.0004	0.0001	0.0004	0.0048	0.0013	0.0013	0.0013	0.0001
hfi_100_1	0.0001	0.0001	0.0010	0.0003	0.0018	0.0183	0.0054	0.0054	0.0054	0.0002
hfi_100_2	0.0002	0.0001	0.0017	0.0005	0.0025	0.0090	0.0061	0.0061	0.0061	0.0006
hfi_100_3	0.0002	0.0001	0.0017	0.0005	0.0025	0.0090	0.0061	0.0061	0.0061	0.0006
hfi_100_4	0.0001	0.0001	0.0010	0.0003	0.0018	0.0183	0.0054	0.0054	0.0054	0.0002
hfi_143_1	0.0001	0.0001	0.0014	0.0004	0.0020	0.0246	0.0046	0.0046	0.0046	0.0003
hfi_143_2	0.0002	0.0002	0.0020	0.0008	0.0022	0.0120	0.0056	0.0056	0.0056	0.0007
hfi_143_3	0.0000	0.0000	0.0008	0.0002	0.0012	0.0097	0.0031	0.0031	0.0031	0.0002
hfi_143_4	0.0001	0.0001	0.0014	0.0004	0.0020	0.0246	0.0046	0.0046	0.0046	0.0003
hfi_143_5	0.0000	0.0000	0.0003	0.0001	0.0007	0.0237	0.0043	0.0043	0.0043	0.0003
hfi_143_6	0.0001	0.0000	0.0003	0.0001	0.0003	0.0127	0.0045	0.0045	0.0045	0.0004
hfi_143_7	0.0001	0.0000	0.0004	0.0001	0.0009	0.0121	0.0039	0.0039	0.0039	0.0004
hfi_143_8	0.0002	0.0001	0.0018	0.0005	0.0027	0.0254	0.0059	0.0059	0.0059	0.0006
hfi_217_1	0.0002	0.0002	0.0020	0.0008	0.0028	0.0229	0.0054	0.0054	0.0054	0.0006
hfi_217_2	0.0001	0.0001	0.0013	0.0005	0.0006	0.0130	0.0043	0.0043	0.0043	0.0003
hfi_217_3	0.0001	0.0001	0.0015	0.0004	0.0002	0.0132	0.0040	0.0040	0.0040	0.0003
hfi_217_4	0.0002	0.0002	0.0017	0.0008	0.0025	0.0226	0.0043	0.0043	0.0043	0.0005
hfi_217_5	0.0001	0.0001	0.0015	0.0004	0.0011	0.0136	0.0038	0.0038	0.0038	0.0003
hfi_217_6	0.0001	0.0001	0.0016	0.0004	0.0027	0.0086	0.0031	0.0031	0.0031	0.0003
hfi_217_7	0.0001	0.0001	0.0018	0.0005	0.0003	0.0097	0.0033	0.0033	0.0033	0.0003
hfi_217_8	0.0002	0.0001	0.0021	0.0006	0.0013	0.0154	0.0043	0.0043	0.0043	0.0007
hfi_353_1	0.0007	0.0005	0.0044	0.0018	0.0022	0.0462	0.0136	0.0136	0.0136	0.0028
hfi_353_2	0.0004	0.0002	0.0030	0.0006	0.0026	0.0266	0.0080	0.0080	0.0080	0.0002
hfi_353_3	0.0003	0.0001	0.0012	0.0005	0.0016	0.0195	0.0053	0.0053	0.0053	0.0005
hfi_353_4	0.0003	0.0002	0.0022	0.0006	0.0025	0.0198	0.0047	0.0047	0.0047	0.0007
hfi_353_5	0.0004	0.0002	0.0018	0.0008	0.0038	0.0184	0.0050	0.0050	0.0050	0.0010
hfi_353_6	0.0004	0.0002	0.0020	0.0009	0.0019	0.0217	0.0055	0.0055	0.0055	0.0008
hfi_353_7	0.0006	0.0003	0.0030	0.0014	0.0017	0.0309	0.0087	0.0087	0.0087	0.0018
hfi_353_8	0.0005	0.0002	0.0029	0.0006	0.0025	0.0459	0.0142	0.0142	0.0142	0.0018
hfi_545_1	0.0010	0.0004	0.0071	0.0021	0.0028	0.1314	0.0303	0.0303	0.0303	0.0029
hfi_545_2	0.0010	0.0004	0.0047	0.0011	0.0030	0.0992	0.0215	0.0215	0.0215	0.0016
hfi_545_3	0.0010	0.0004	0.0033	0.0007	0.0019	0.1030	0.0215	0.0215	0.0215	0.0015
hfi_545_4	0.0011	0.0006	0.0074	0.0028	0.0029	0.1335	0.0294	0.0294	0.0294	0.0027
hfi_857_1	0.0018	0.0007	0.0029	0.0011	0.0116	0.1367	0.0302	0.0302	0.0302	0.0042
hfi_857_2	0.0018	0.0008	0.0031	0.0019	0.0131	0.1012	0.0253	0.0253	0.0253	0.0049
hfi_857_3	0.0017	0.0006	0.0016	0.0015	0.0120	0.1080	0.0269	0.0269	0.0269	0.0057
hfi_857_4	0.0022	0.0009	0.0029	0.0020	0.0104	0.1485	0.0337	0.0337	0.0337	0.0048

Table 7.4-26 random case (51 to 60)



detector N°	case61	case62	case63	case64	case65	case66	case67	case68
	dB	dB	dB	dB	dB	dB	dB	dB
lfi_70_18	0,0039	0,0015	0,0003	0,0003	0,0039	0,0015	0,0003	0,0001
lfi_70_19	0,0039	0,0027	0,0006	0,0002	0,0039	0,0027	0,0006	0,0001
lfi_70_20	0,0022	0,0040	0,0004	0,0003	0,0022	0,0040	0,0004	0,0002
lfi_70_21	0,0022	0,0040	0,0004	0,0003	0,0022	0,0040	0,0004	0,0002
lfi_70_22	0,0039	0,0027	0,0006	0,0002	0,0039	0,0027	0,0006	0,0001
lfi_70_23	0,0039	0,0015	0,0003	0,0003	0,0039	0,0015	0,0003	0,0001
lfi_44_24	0,0001	0,0031	0,0001	0,0002	0,0001	0,0031	0,0001	0,0001
lfi_44_25	0,0055	0,0029	0,0007	0,0004	0,0055	0,0029	0,0007	0,0001
lfi_44_26	0,0055	0,0029	0,0007	0,0004	0,0055	0,0029	0,0007	0,0001
lfi_30_27	0,0018	0,0023	0,0001	0,0002	0,0018	0,0023	0,0001	0,0001
lfi_30_28	0,0018	0,0023	0,0001	0,0002	0,0018	0,0023	0,0001	0,0001
hfi_100_1	0,0039	0,0016	0,0013	0,0001	0,0039	0,0016	0,0013	0,0003
hfi_100_2	0,0007	0,0064	0,0010	0,0005	0,0008	0,0064	0,0010	0,0003
hfi_100_3	0,0007	0,0064	0,0010	0,0005	0,0007	0,0064	0,0010	0,0003
hfi_100_4	0,0039	0,0016	0,0013	0,0001	0,0040	0,0016	0,0013	0,0003
hfi_143_1	0,0067	0,0018	0,0018	0,0005	0,0067	0,0018	0,0018	0,0004
hfi_143_2	0,0024	0,0039	0,0002	0,0007	0,0024	0,0039	0,0002	0,0004
hfi_143_3	0,0020	0,0025	0,0002	0,0003	0,0020	0,0025	0,0002	0,0001
hfi_143_4	0,0067	0,0018	0,0018	0,0005	0,0067	0,0018	0,0018	0,0004
hfi_143_5	0,0069	0,0035	0,0002	0,0003	0,0069	0,0035	0,0002	0,0001
hfi_143_6	0,0017	0,0056	0,0005	0,0003	0,0017	0,0056	0,0005	0,0001
hfi_143_7	0,0017	0,0059	0,0005	0,0003	0,0017	0,0059	0,0005	0,0001
hfi_143_8	0,0074	0,0045	0,0002	0,0004	0,0074	0,0045	0,0002	0,0003
hfi_217_1	0,0067	0,0045	0,0018	0,0005	0,0067	0,0045	0,0018	0,0006
hfi_217_2	0,0038	0,0021	0,0011	0,0008	0,0038	0,0021	0,0011	0,0003
hfi_217_3	0,0038	0,0025	0,0011	0,0007	0,0038	0,0025	0,0011	0,0002
hfi_217_4	0,0061	0,0038	0,0019	0,0004	0,0060	0,0038	0,0019	0,0006
hfi_217_5	0,0037	0,0054	0,0007	0,0004	0,0037	0,0054	0,0007	0,0003
hfi_217_6	0,0028	0,0036	0,0007	0,0001	0,0028	0,0036	0,0007	0,0003
hfi_217_7	0,0033	0,0031	0,0007	0,0006	0,0033	0,0031	0,0007	0,0003
hfi_217_8	0,0050	0,0067	0,0007	0,0006	0,0050	0,0067	0,0007	0,0004
hfi_353_1	0,0049	0,0329	0,0005	0,0022	0,0050	0,0329	0,0005	0,0011
hfi_353_2	0,0033	0,0230	0,0013	0,0003	0,0033	0,0230	0,0013	0,0006
hfi_353_3	0,0011	0,0195	0,0016	0,0007	0,0011	0,0195	0,0016	0,0004
hfi_353_4	0,0008	0,0167	0,0015	0,0009	0,0008	0,0167	0,0015	0,0004
hfi_353_5	0,0009	0,0150	0,0011	0,0011	0,0009	0,0150	0,0011	0,0007
hfi_353_6	0,0016	0,0196	0,0015	0,0019	0,0015	0,0196	0,0015	0,0005
hfi_353_7	0,0021	0,0259	0,0011	0,0022	0,0021	0,0259	0,0011	0,0008
hfi_353_8	0,0068	0,0339	0,0004	0,0009	0,0068	0,0339	0,0004	0,0005
hfi_545_1	0,0332	0,0587	0,0055	0,0022	0,0333	0,0587	0,0055	0,0015
hfi_545_2	0,0232	0,0553	0,0041	0,0038	0,0232	0,0553	0,0041	0,0010
hfi_545_3	0,0247	0,0570	0,0033	0,0030	0,0247	0,0570	0,0033	0,0013
hfi_545_4	0,0337	0,0585	0,0044	0,0018	0,0336	0,0585	0,0044	0,0018
hfi_857_1	0,0259	0,0983	0,0043	0,0071	0,0259	0,0983	0,0043	0,0023
hfi_857_2	0,0101	0,0843	0,0005	0,0060	0,0102	0,0843	0,0005	0,0025
hfi_857_3	0,0117	0,0891	0,0008	0,0083	0,0116	0,0891	0,0008	0,0020
hfi_857_4	0,0290	0,1029	0,0047	0,0072	0,0288	0,1029	0,0047	0,0024

Table 7.4-27 random case (61 to 68)



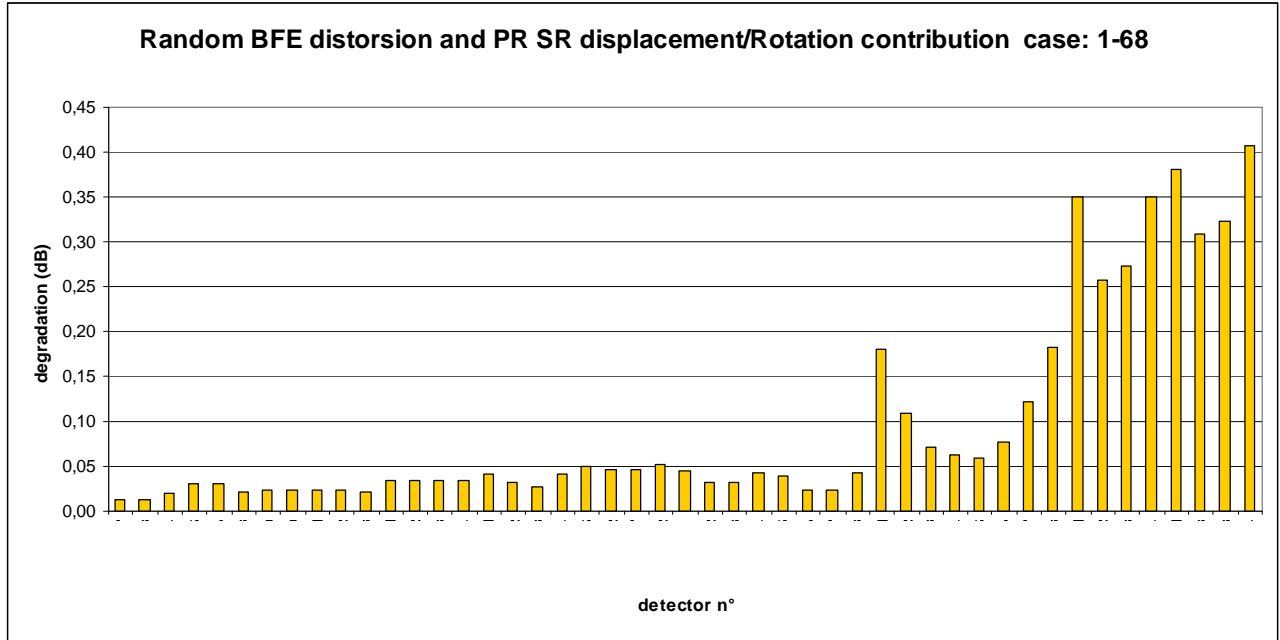


Figure 7.4-18 Budget for Random BFE distortion and PR SR displacements/rotations





#### 7.4.3.4 Total random case

The complete budget for the random contributors is presented in the Table below. The last column corresponds to the RSS of and Table 7.4-28.



detector n°	BFE know. accuracy other cont.	FPU random	Random BFE distorsion and displacements contribution case: 1-68	TOTAL RANDOM BUDGET
	dB	dB	dB	dB
LFI_30_27	0,0189	0,0049	0,0128	<b>0,0234</b>
LFI_30_28	0,0188	0,0047	0,0128	<b>0,0233</b>
LFI_44_24	0,0228	0,0067	0,0196	<b>0,0309</b>
LFI_44_25	0,0228	0,0069	0,0312	<b>0,0393</b>
LFI_44_26	0,0327	0,0052	0,0310	<b>0,0454</b>
LFI_70_18	0,0203	0,0059	0,0209	<b>0,0297</b>
LFI_70_19	0,0252	0,0054	0,0228	<b>0,0344</b>
LFI_70_20	0,0308	0,0045	0,0240	<b>0,0393</b>
LFI_70_21	0,0306	0,0048	0,0240	<b>0,0392</b>
LFI_70_22	0,0232	0,0058	0,0227	<b>0,0330</b>
LFI_70_23	0,0189	0,0060	0,0208	<b>0,0287</b>
HFI_100_1	0,0250	0,0069	0,0342	<b>0,0430</b>
HFI_100_2	0,0389	0,0042	0,0333	<b>0,0514</b>
HFI_100_3	0,0391	0,0040	0,0331	<b>0,0514</b>
HFI_100_4	0,0298	0,0069	0,0342	<b>0,0459</b>
HFI_143_1	0,0436	0,0066	0,0417	<b>0,0607</b>
HFI_143_2	0,0343	0,0073	0,0327	<b>0,0480</b>
HFI_143_3	0,0328	0,0040	0,0271	<b>0,0427</b>
HFI_143_4	0,0436	0,0066	0,0417	<b>0,0607</b>
HFI_143_5	0,0612	0,0040	0,0493	<b>0,0787</b>
HFI_143_6	0,0705	0,0051	0,0469	<b>0,0848</b>
HFI_143_7	0,0685	0,0044	0,0462	<b>0,0827</b>
HFI_143_8	0,0582	0,0056	0,0517	<b>0,0781</b>
HFI_217_1	0,0368	0,0046	0,0455	<b>0,0587</b>
HFI_217_2	0,0409	0,0020	0,0320	<b>0,0520</b>
HFI_217_3	0,0413	0,0013	0,0323	<b>0,0524</b>
HFI_217_4	0,0405	0,0038	0,0428	<b>0,0591</b>
HFI_217_5	0,0283	0,0032	0,0400	<b>0,0491</b>
HFI_217_6	0,0201	0,0024	0,0238	<b>0,0312</b>
HFI_217_7	0,0241	0,0022	0,0233	<b>0,0336</b>
HFI_217_8	0,0346	0,0026	0,0433	<b>0,0555</b>
HFI_353_1	0,2432	0,0223	0,1806	<b>0,3038</b>
HFI_353_2	0,1353	0,0206	0,1083	<b>0,1745</b>
HFI_353_3	0,0800	0,0122	0,0717	<b>0,1081</b>
HFI_353_4	0,0966	0,0130	0,0625	<b>0,1157</b>
HFI_353_5	0,0978	0,0141	0,0589	<b>0,1151</b>
HFI_353_6	0,0843	0,0145	0,0777	<b>0,1155</b>
HFI_353_7	0,1474	0,0180	0,1214	<b>0,1918</b>
HFI_353_8	0,2436	0,0235	0,1817	<b>0,3048</b>
HFI_545_1	0,4769	0,0728	0,3502	<b>0,5962</b>
HFI_545_2	0,2907	0,0643	0,2567	<b>0,3931</b>
HFI_545_3	0,3129	0,0669	0,2741	<b>0,4213</b>
HFI_545_4	0,4591	0,0710	0,3503	<b>0,5818</b>
HFI_857_1	0,5188	0,1559	0,3798	<b>0,6616</b>
HFI_857_2	0,5901	0,1378	0,3088	<b>0,6801</b>
HFI_857_3	0,5813	0,1391	0,3235	<b>0,6796</b>
HFI_857_4	0,5264	0,1600	0,4072	<b>0,6844</b>

Table 7.4-28 Total Random budget

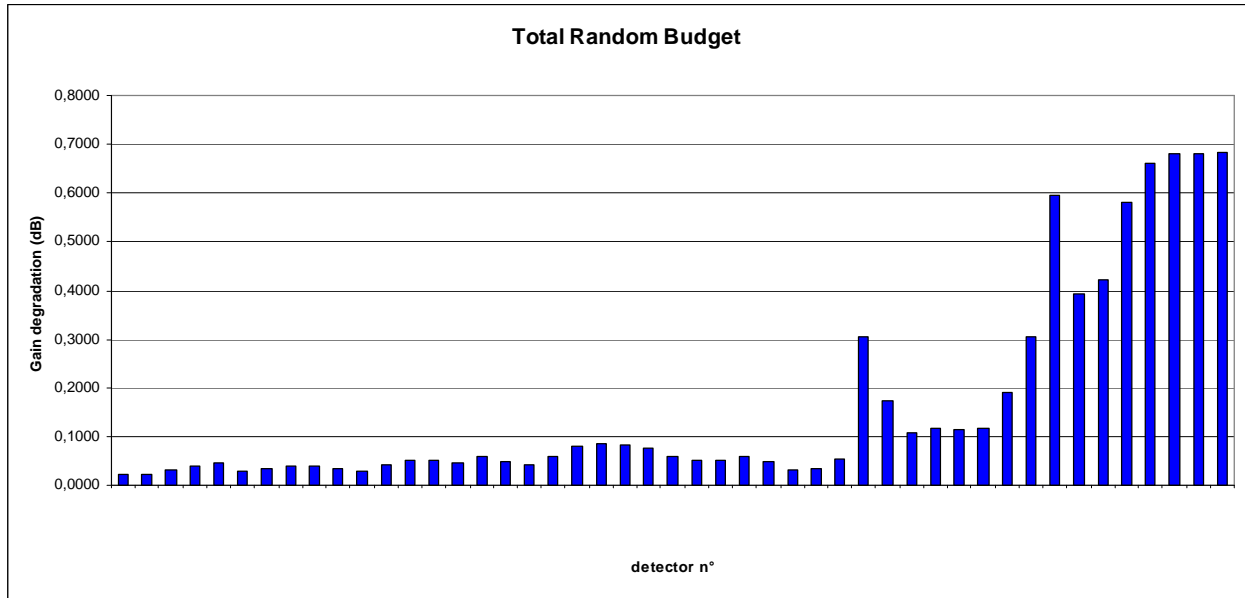


Figure 7.4-19 Total Random Budget

A major contributor appears in the random budget compared to previous CDR budget. The post : “BFE knowlegde and accuracy” is an important contributor. Paradoxically, inherent to a better knowledge of the deterministic case (by videogrammetry measurements) induced a significant uncertainties.



#### 7.4.4 Complete Budget

The RF main lobe performance budget of Planck Telescope is shown in the following Table 7.4-29 and the following Figure 7.4-20. The column "Total Budget" is obtained by summing Table 7.4-11 and Table 7.4-24.

detector n°	Total	Total	Total Budget	Specifications
	Deterministe	Random		
	dB	dB	dB	dB
LFI_30_27	0,1889	0,0234	<b>0,2123</b>	0,5
LFI_30_28	0,1886	0,0233	<b>0,2119</b>	0,5
LFI_44_24	0,0032	0,0309	<b>0,0341</b>	0,5
LFI_44_25	0,0521	0,0393	<b>0,0914</b>	0,5
LFI_44_26	0,2508	0,0454	<b>0,2961</b>	0,5
LFI_70_18	0,1109	0,0297	<b>0,1405</b>	0,5
LFI_70_19	0,1647	0,0344	<b>0,1991</b>	0,5
LFI_70_20	0,1972	0,0393	<b>0,2365</b>	0,5
LFI_70_21	0,2057	0,0392	<b>0,2450</b>	0,5
LFI_70_22	0,1851	0,0330	<b>0,2181</b>	0,5
LFI_70_23	0,1305	0,0287	<b>0,1592</b>	0,5
HFI_100_1	0,1971	0,0430	<b>0,2401</b>	0,5
HFI_100_2	0,2292	0,0514	<b>0,2806</b>	0,5
HFI_100_3	0,2171	0,0514	<b>0,2685</b>	0,5
HFI_100_4	0,1647	0,0459	<b>0,2106</b>	0,5
HFI_143_1	0,1057	0,0607	<b>0,1664</b>	0,5
HFI_143_2	0,1162	0,0480	<b>0,1642</b>	0,5
HFI_143_3	0,1358	0,0427	<b>0,1785</b>	0,5
HFI_143_4	0,1057	0,0607	<b>0,1664</b>	0,5
HFI_143_5	0,0989	0,0787	<b>0,1776</b>	0,5
HFI_143_6	0,1594	0,0848	<b>0,2442</b>	0,5
HFI_143_7	0,1752	0,0827	<b>0,2579</b>	0,5
HFI_143_8	0,1629	0,0781	<b>0,2410</b>	0,5
HFI_217_1	0,1724	0,0587	<b>0,2312</b>	1
HFI_217_2	0,1995	0,0520	<b>0,2515</b>	1
HFI_217_3	0,1864	0,0524	<b>0,2388</b>	1
HFI_217_4	0,1226	0,0591	<b>0,1816</b>	1
HFI_217_5	0,0909	0,0491	<b>0,1400</b>	1
HFI_217_6	0,1396	0,0312	<b>0,1708</b>	1
HFI_217_7	0,1267	0,0336	<b>0,1603</b>	1
HFI_217_8	0,0615	0,0555	<b>0,1170</b>	1
HFI_353_1	-0,2231	0,3038	<b>0,0807</b>	1
HFI_353_2	-0,0255	0,1745	<b>0,1490</b>	1
HFI_353_3	0,1058	0,1081	<b>0,2138</b>	1
HFI_353_4	0,1653	0,1157	<b>0,2810</b>	1
HFI_353_5	0,1555	0,1151	<b>0,2705</b>	1
HFI_353_6	0,0781	0,1155	<b>0,1937</b>	1
HFI_353_7	-0,0530	0,1918	<b>0,1387</b>	1
HFI_353_8	-0,2119	0,3048	<b>0,0929</b>	1
HFI_545_1	-0,5304	0,5962	<b>0,0658</b>	1,4
HFI_545_2	-0,1426	0,3931	<b>0,2505</b>	1,4
HFI_545_3	-0,1205	0,4213	<b>0,3008</b>	1,4
HFI_545_4	-0,2840	0,5818	<b>0,2978</b>	1,4
HFI_857_1	0,2070	0,6616	<b>0,8686</b>	2,5
HFI_857_2	0,5271	0,6801	<b>1,2072</b>	2,5
HFI_857_3	0,4932	0,6796	<b>1,1729</b>	2,5
HFI_857_4	0,2012	0,6844	<b>0,8856</b>	2,5

Table 7.4-29 Complete Budget

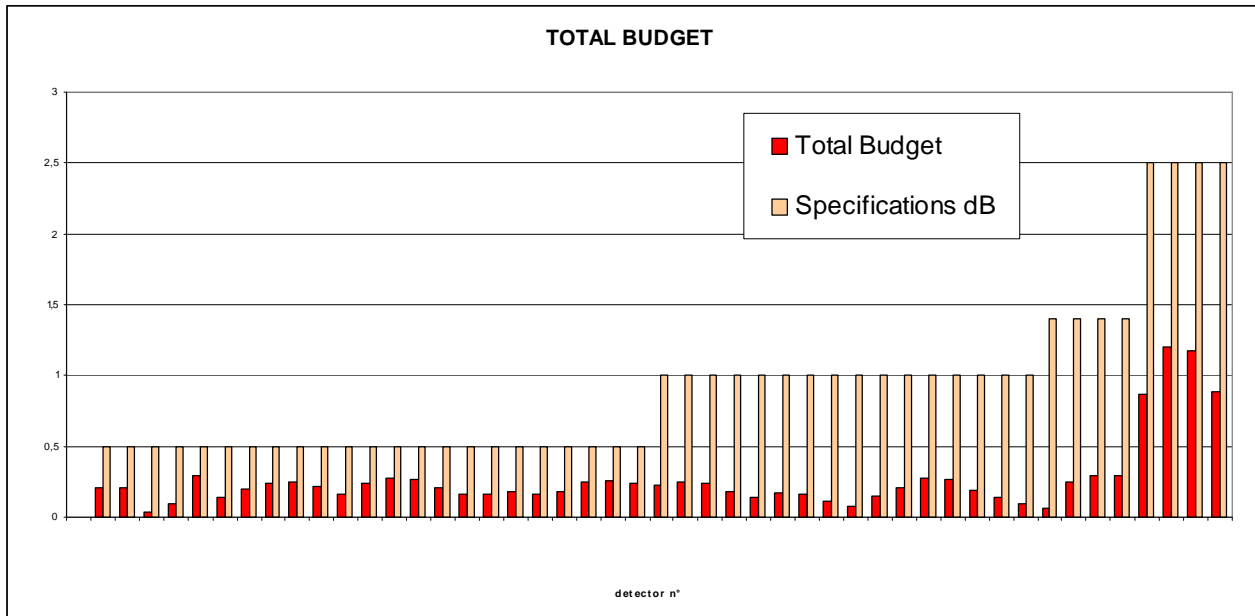


Figure 7.4-20 Total RF Budget of Planck Telescope



### 7.4.5 Ellipticity of LFI horns

The table below gives the value of beam ellipticity :

	theory	deterministe	
	R=a/b	R=a/b	DR/R
			%
lfi_20_27	1,35224	1,32328	2,14157
lfi_30_28	1,35218	1,31356	2,85643
lfi_44_24	1,34416	1,29661	3,53786
lfi_44_25	1,25483	1,25009	0,37745
lfi_44_26	1,25459	1,25774	0,25115
lfi_70_18	1,27488	1,25857	1,27912
lfi_70_19	1,28046	1,25771	1,77663
lfi_70_20	1,28697	1,25427	2,54033
lfi_70_21	1,28699	1,25829	2,22987
lfi_70_22	1,28047	1,25564	1,93898
lfi_70_23	1,27401	1,26050	1,06075

Figure 7.4-21 : Ellipticity variation

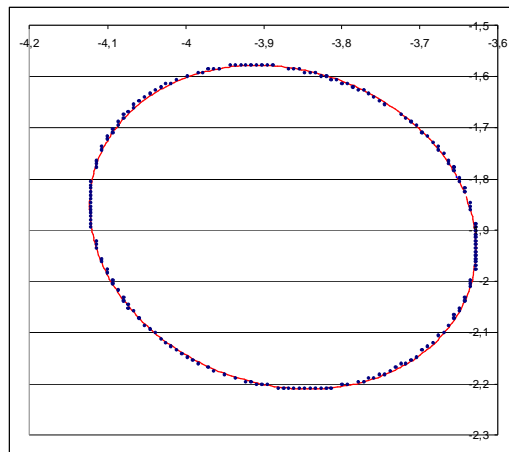


Figure 7.4-22 : Example : LFI\_30\_28 horn (deterministic case and best fit)

In figure 7.4-22, the best fit ellipse and the 3 dB contour are plotted.

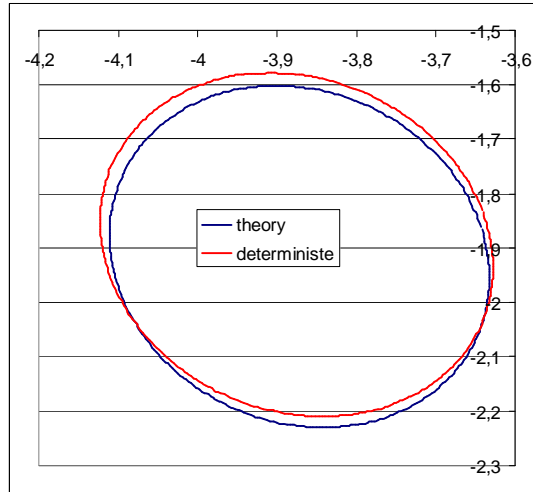


Figure -7.4-23 Comparison between the two best fit ellipses LFI\_30\_28



## 7.5 Conclusion

In this chapter, the RF main lobe performance of Planck Telescope budget is presented. The deterministic model and the inputs for random budget have been updated since CDR. The modifications are in the sense of knowledge enhancements of the telescope at operational:

For deterministic case:

- BFE measurement data (videogrammetry)
- Sub-reflector data HF(interferometry)
- Optimisation-Realignment
- Alignment data of Flight model

For random case:

- Manufacturing and accuracy ( videogrammetry measurement uncertainties)
- FPU random displacement

Although the degradation of the budget since the CDR budget, compared to the specifications, the margin remains comfortable.





## 8. CONCLUSION

For the requirement toward the Earth Sun and Moon, the results of the computation performed in the frame of the RF expertise (ideal reflector surfaces, no dust, sharp edges) show a significant margin (see section 6.4)

For the self spacecraft emission a significant margin is obtained. The most critical surface is the reflector then the other elements in the optical cavity. the results are synthesized in section 4.

On final the main lobe performance degradation is well below the allowed degradation. Anyhow the only deviation with a requirement is the beam ellipticity of the LFI horns (see section 7.4.4.) (see RFW H-P-221000-ASP-RD-0024).

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