



## Technical Note on the ICC Work Package: Fourier Transformation

### Prepared by:

Peter Davis (University of Lethbridge)  
peter.davis@uleth.ca

Trevor Fulton (University of Lethbridge)  
trevor.fulton@uleth.ca

### Approved by:

David Naylor (University of Lethbridge)  
naylor@uleth.ca

### Document History:

Issue	Date
0.1 draft	5 March 2004
<u>Version 1.0</u>	<u>May 13, 2004</u>



Table of Contents:

- 1. Distribution List ..... 2
- 2. Reference Documents ..... 2
- 3. Applicable Documents ..... 3
- 4. Acronyms ..... 3
- 5. Objective of this document ..... 4
- 6. Objective of Work Package ..... 4
- 7. Input ..... 4
- 8. Output ..... 5
- 9. Milestones ..... 5
- 10. Involved parties ..... 5
  - 10.1. SPIRE teams ..... 5
  - 10.2. Institutions ..... 5
- 11. Implementation options ..... 6
  - 11.1. Interpolation of the stage position ..... 6
  - 11.2. Phasecorrection ..... 7
  - 11.3. Fourier Transformation ..... 7
  - 11.4. Apodization ..... 78
- 12. Open Issues ..... 8
- 13. Checkpoints ..... 8

## 1. Distribution List

~~Eric Vachon (CSA)~~

Dave Clements (ICL)

Matt Fox (ICL)

Ken Ganga (IPAC)

Bernhard Schulz (IPAC)

Jean-Paul Baluteau (LAM)

Didier Ferrand (LAM)

Christian Surace (LAM)

Steve Guest (RAL)

Ken King (RAL)

Tanya Lim (RAL)

Sunil Sidher (RAL)



Bruce Swinyard (RAL)

## 2. Reference Documents

ID	Title	Author
RD1	SPIRE ICC Consolidated WorkPlan, 1.0 draft 2	Ken King
<u>RD2</u>	<u>Operating Modes for the SPIRE Instrument, SPIRE-RAL-PRJ-000320</u>	<u>Bruce Swinyard</u>

## 3. Applicable Documents

ID	Title	Author
Kunis, Potts, Steidl 2002	Fast Fourier transform at nonequispaced knots, A user's guide to a C-library <a href="http://www.math.mu-luebeck.de/potts/nfft/">http://www.math.mu-luebeck.de/potts/nfft/</a>	Stefan Kunis, Daniel Potts, University of Lübeck, Germany and Gabriele Steidl, University of Mannheim, Germany
Potts, Steidl, Tasche 2001	Fast Fourier transforms for nonequispaced data: A tutorial. In J. J. Benedetto and P. J. S. G. Ferreira, editors, Modern Sampling Theory: Mathematics and Applications, pages 247 - 270, Boston	Daniel Potts, Gabriele Steidl, and Manfred Tasche, University of Lübeck, Germany
Spencer 2003	Phase Correction and Apodization	Locke Spencer, University of Lethbridge
Tahic 2004	Apodization, Powerpoint Presentation	Margaret Tahic, University of Lethbridge

## 4. Acronyms

CALT	Calibration Team
CSA	Canadian Space Agency
DRCU	Detector Read-out and Control Unit
FFT	Fast Fourier Transformation
FT	Fourier Transformation
HCSS	Herschel Common Software System
IA	Interactive Analysis
ICC	Instrument Control Centre



ICL	Imperial College London
IPAC	Infrared Processing and Analysis Center
ISDT	Instrument Software Development Team
JAC	Joint Astronomy Centre
JPL	Jet Propulsion Laboratory
LAM	Laboratoire d'Astrophysique de Marseille
OBST	Observations and Data Processing Team
RAL	Rutherford Appleton Laboratory
SMEC	Spectrometer Mechanical Unit
TBC	To be confirmed
TM	Telemetry
UoL	University of Lethbridge
ZPD	Zero Path Difference
<u>SDS</u>	<u>Spectrometer Detector Spectrum</u>
<u>SDT</u>	<u>Spectrometer Detector Timeline</u>
<u>OPD</u>	<u>Optical Path Difference</u>
<u>FOV</u>	<u>Field of view</u>

## 5. Objective of this document

This document provides a comprehensive and detailed overview of the processes that go into the delivery of the ICC Work Package Fourier Transformation. It aims to collect and consolidate contributions from all involved groups and individuals.

## 6. Objective of Work Package

“Provide data processing steps and software modules to convert photometrically corrected detector data timeline into a spectrum using converted SMEC Data.

This involves assigning an Optical Path Difference to each detector sample, interpolating into an equally sample dataset (TBC), phase correction, apodization, and Fourier transformation.” (RD1, 36)

## 7. Input

1. Spec Detector Timeline (SDT) from the task ‘Crosstalk’

2. SMEC timeline

It is also assumed that additional metadata will be available, such as the operating parameters of the spectrometer.



- ~~1. IA Development System~~
- ~~2. Calibration information to convert from SMEC encoder position to Optical Path Difference~~
- ~~3. TM data (ingested into the HCSS) containing test SMEC data~~
- ~~4. Processed test detector and SMEC data products~~

## 8. Output

- ~~1. Data Product Definitions~~
- ~~2. Processing modules~~
- ~~3. Conversion Data/Tables for each instrument model~~
  1. Spec Detector Spectrum (SDS) into the task 'Correct for Telescope'
  2. Quality Control Bitmap for the SDS (and SDT?)

## 9. Milestones

July 2004: Definition of Data Products

January 2005: Delivery of Processing Modules

January 2005: Delivery of Conversion Data/Tables

## 10. Involved parties

### 10.1. SPIRE teams

- Other users of input data: DRCU, in particular photometer bolometer arrays, spectrometer bolometer arrays, and SMEC (JPL ???; LAM, Jean-Paul Baluteau, ...)
- Other users of output data: DRCU, in particular bolometer arrays (JPL ???; IPAC, LAM, Jean-Paul Baluteau, ...)
- OBST (ICL, Matt Fox)
- Quality Control (ICL, Dave Clements)
- Trend Analysis (RAL, Sunil Sidher?)
- CALT (RAL, Tanya Lim)
- ISDT (RAL, Steve Guest)

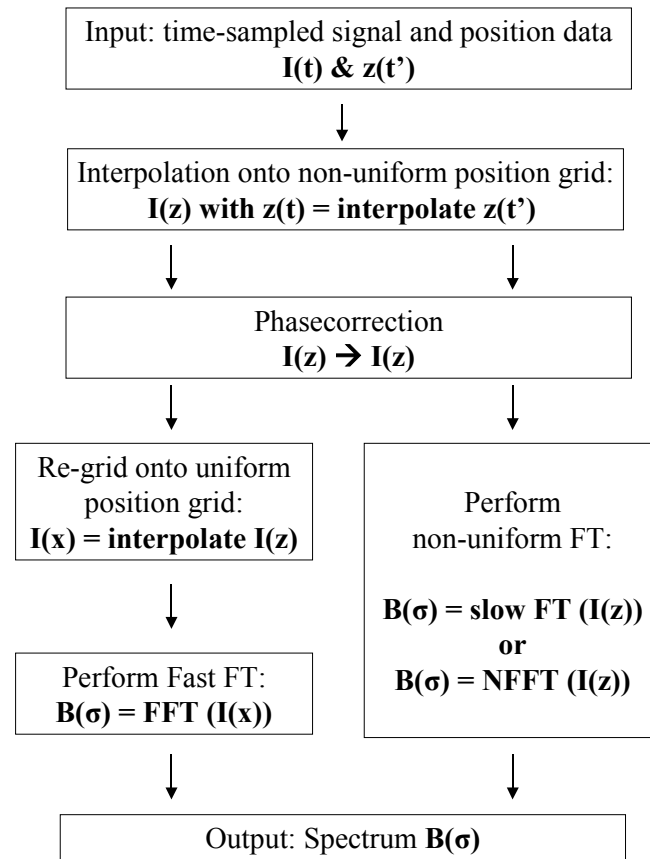
### 10.2. Institutions

- ICL: Matt Fox (OBST, photometer deglitching), Dave Clements (Quality Control)
- LAM: Jean-Paul Baluteau et al. (spectrometer deglitching, SMEC data)
- RAL: Tanya Lim (CALT), Steve Guest (ISDT), Sunil Sidher? (Trend Analysis)
- Other providers/users of in/output data (JPL!?, ...)

## 11. Implementation options

Data reduction for the SPIRE FTS data is a linear process with three mandatory and one optional step: Interpolation of the stage position, phasecorrection, Fourier Transformation are necessary elements of this process. Apodization is an option depending on user.

The two qualitatively different operational modes for the spectrometer, continuous scan and step-and-integrate (see RD2), will require slightly different processing. The following sections are written with the continuous scan mode in mind. See the section on open issues for special considerations on step-and-integrate.



**Figure 1: Process options to perform the FT**

### 11.1. Interpolation of the stage position

Data from the DRCU are time-sampled where the position of the stage is measured at  $\sim 240\text{Hz}$ :  $z(t')$  and the detectors are read out at a rate of  $\sim 80\text{Hz}$ :  $I(t)$ , i.e., position is sampled more frequently than signal<sup>1</sup>. The first step is therefore to interpolate the position so that for each signal reading a position is made available:  $I(z)$ . Please note that the

<sup>1</sup> This document uses  $z$  to refer to non-uniform position data and  $x$  to refer to uniform, i.e. equidistant position data.



resulting interferogram will be non-uniform, i.e. the position grid is not equidistant ( $z \neq i \cdot \Delta z$  with  $i \in \mathbb{Z}$ ).

This is a good point to convert mechanical position into optical path difference. A routine to identify ZPD or the central maximum will be necessary for this. An early conversion has the advantage of avoiding later confusion. However, it should be noted that the details of determining ZPD will have an impact on the resulting phase and therefore phase correction.

The OPD is not the same for all the detectors and depends on their angle  $\beta$  from the optical axis:  $OPD(\beta) = OPD(0) \times \cos(\beta)$  Where  $\beta_{\max} = (FOV/2) \times (D/d)$  with  $D =$  telescope diameter (3300 mm) and  $d =$  pupil diameter (25 mm). So for a detector at the edge of the FOV (2.6')  $\beta = 2.86$  degree.

## 11.2. Phase correction

An important step in the data reduction is the phase correction. Beamsplitters, discrete time-sampling, direction of the stage, and electronic filtering all introduce **significant** phase errors to the ~~raw~~ data. A routine to correct for the phase errors needs to be developed. Two approaches seem to be possible: ~~It is possible to e~~Either study and model all components that contribute to the phase error and develop a phase correction on this basis or ~~to~~ analyze the phase resulting from the measurements and use the empirical data as the basis for phase correction (Spencer 2003)<sup>2</sup>. The latter option assumes that some double-sided portion for each interferogram is available. It will be necessary to distinguish between single-sided and double-sided interferograms.

Phase correction is shown in Figure 1 as a processing step that operates on non-uniform data. It may be preferable to correct for phase errors on equidistant data if available.

## 11.3. Fourier Transformation

At this juncture, one can either re-grid the non-uniform interferogram onto a uniform interferogram  $I(x)$  and then use a standard FFT or perform an FT on the non-uniform interferogram (see **Error! Reference source not found.**Figure 1). The former option may cause problems because the re-gridding may introduce artifacts. The latter option assumes to compute an FT which is a slow operation of  $O(n^2)$  if a fast implementation for the non-uniform FT is not feasible. Efficient algorithms to perform a non-uniform FT have been proposed (Potts, Steidl, Tasche 2001) and implemented in a C-library (Kunis, Potts, Steidl 2002). Their adequacy for the problem at hand is to be verified.

## 11.4. Apodization

Data products can be enhanced under certain circumstances by applying apodization functions to the interferogram. Apodization functions reduce ringing while losing spectral resolution at the same time.

---

<sup>2</sup> To date, the LAM has pursued the modeling and the UoL the empirical approach.



Optional apodization will be based on the Norton-Beer expansion of apodization functions to allow the selection of a suitable apodization function based on the reduction of spectral resolution (see Tahic 2004).

NB: The apodization function can be applied to the non-uniform or the uniform interferogram for the re-gridding option for the FT (see section 11.3). It will be necessary to explore which one of these two options is preferable.

## 12. Open Issues

- Is NFFT an efficient and precise software package to perform an FT on non-uniformly sampled data? If so, is it feasible to translate the relevant parts of this package into Java?
- How to perform the phasecorrection?
- Does phasecorrection have a problem with non-uniform interferograms?
- Should apodization functions be applied to the uniform or the non-uniform interferograms?
- The Quality Control bitmap for the interferograms (SDT) does not translate naturally into a bitmap for the spectrum (SDS). Shall we freeze and push along the bitmap for the interferograms and create a second bitmap for the spectra?
- As far as step-and-integrate is concerned: Is it better to average signals for each stage position and then FT the resulting interferogram or should n different FTs be performed and then averaged? Or should we not average and output n different spectra?
- Does this task have to meet performance requirements?

## 13. Checkpoints

Other users/OBST:

- Have all providers of input data agreed on its format?
- Have all users of the end product agreed on its format?

Quality Control:

- Are adequate flags for data quality and processing quality provided?

Trend Analysis:

- Are adequate flags for long-term trends in the data quality and processing quality provided?

CALT:

- Have all necessary calibration tables been identified?
- Can all necessary calibration tables be provided by the scheduled tests/operations?

ISDT:





- Are all software requirements (coding conventions, exception handling, test procedures, documentation, benchmarking) met?