

This technote deals with the choice of material in order to provide for thermal insulation while maintaining a (relative) high stiffness. This document compares Titanium Ta6V with Stainless Steel-321. This in order to be able to decide whether ss-321 or Ta6V is the material with the better overall properties.

### Temperature laws

The temperature law for this type of stainless steel is (MSSL data, in line with general literature):

$$K_{ss} = 0.1T - 0.1 \text{ [W/m K] and } 4 \text{ K} < T < 15 \text{ K}$$

Lionel Duband provided us with this temperature law for Ta6V (derived from his measurements, in line with general literature)

$$K_{ti} = -4.045 \cdot 10^{-4} T^2 + 7.61 \cdot 10^{-2} T - 4.48 \cdot 10^{-2} \text{ [W/m K] and } 2 \text{ K} < T < 50 \text{ K}$$

### Selection criterion

In order to be able to compare both materials we need to normalise them with regard to stiffness and then look at the ratio. That is:

$$K_{ti} \cdot E_{ss}/E_{ti} : K_{ss}$$

This means that the cross sectional area of the titanium design needs to be  $E_{ss}/E_{ti}$  times bigger than a stainless steel cross sectional area to provide for the same stiffness. We are assuming here that for the critical sections of the supports the cross-sectional area is driving the overall stiffness. This is the case both for the A-frames as well for the cone. The criterion is therefore

$$K_{ti} \cdot E_{ss}/E_{ti} > K_{ss} \rightarrow \text{stainless is effectively a better insulator}$$

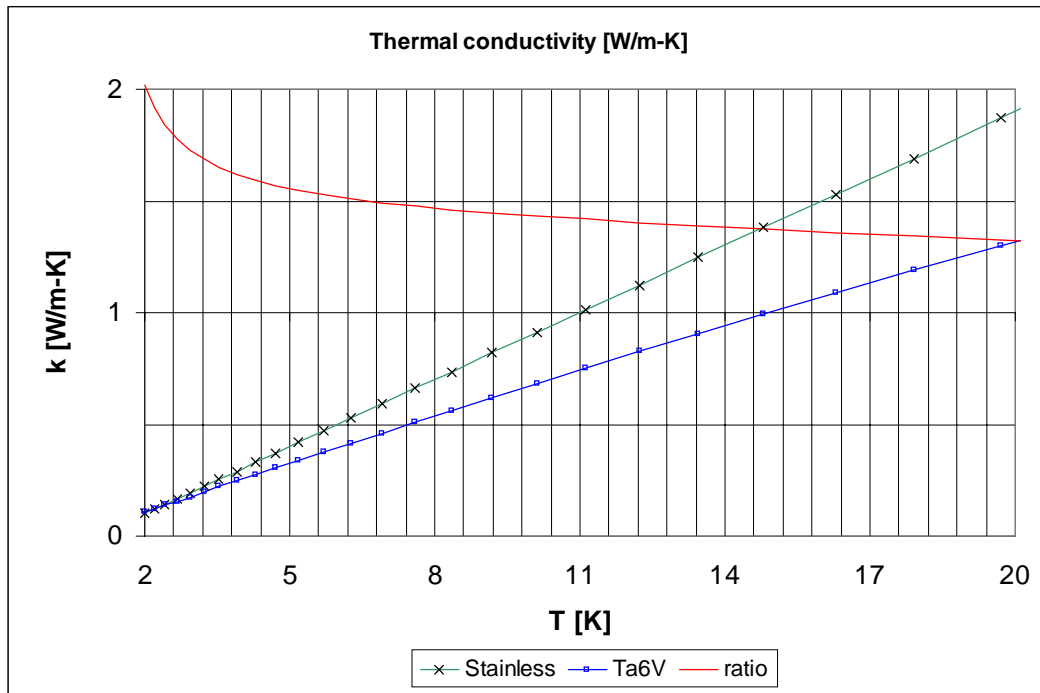
$$K_{ti} \cdot E_{ss}/E_{ti} < K_{ss} \rightarrow \text{titanium is effectively a better insulator}$$

So in all this criterion effectively compares the thermal conductance of both materials normalised with regard to stiffness.

The assumed stiffness for stainless steel at  $T < 15 \text{ K}$  is 225 GPa and for Titanium 115 GPa (+10% stiffness added to compensate for drop in temperature, effectively this change in stiffness cancels out in the weighting function)

## The results

Hereafter a plot is given with the conductivity's and the ratio  $(K_{Ti} \cdot E_{ss}) / (E_{Ti} \cdot K_{ss})$



Thermal conduction compared (ratio)

From the graph it becomes clear that since the ratio is above 1 throughout the temperature range 4-15 K at these temperatures, stainless steel is the better thermal insulator. At about 2 Kelvin (cross-over in thermal conduction) the ratio is about 2, which is the ratio of both stiffnesses (stainless steel is about twice as stiff as titanium)

## Conclusion

Therefore the conclusion is that stainless steel is the better choice of material for the instrument supports in the temperature range 4 K to 15 K.